

HW  
25/06/2021

Exercise 6.2

- 1) In Fig. 6.28, find the value of  $x$  and  $y$  and then show that  $AB \parallel CD$ .

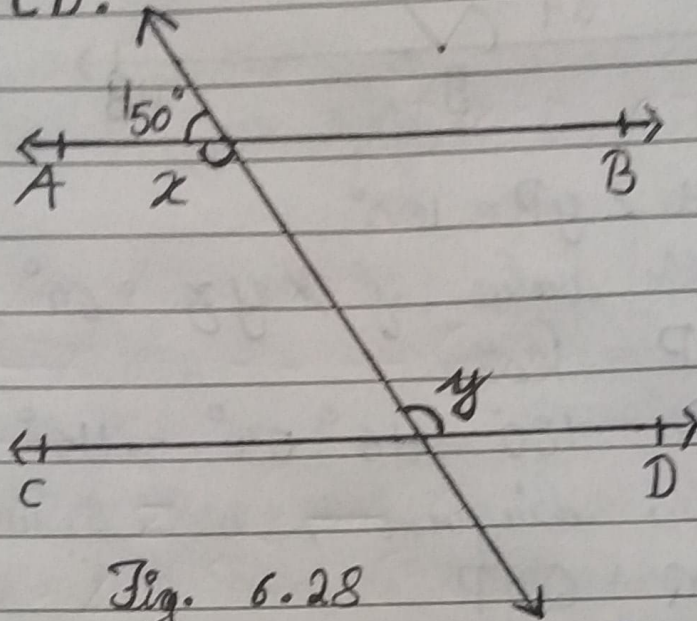


Fig. 6.28

ans) We know that a linear pair is equal to  $180^\circ$ .

$$\text{So, } x + 50^\circ = 180^\circ$$

$$x = 180^\circ - 50^\circ$$

$$x = 130^\circ$$

We also know that vertically opposite angles are.

$$\text{So, } y = 130^\circ$$

In two parallel lines, the alternate interior angles are equal. In this,

$$x = y = 130^\circ$$

This proves that alternate interior angles are equal and so,  $AB \parallel CD$ .

2) In Fig. 6.29, if  $AB \parallel CD$ ,  $CD \parallel EF$  and  $y : z = 3 : 7$ , find  $x$ .

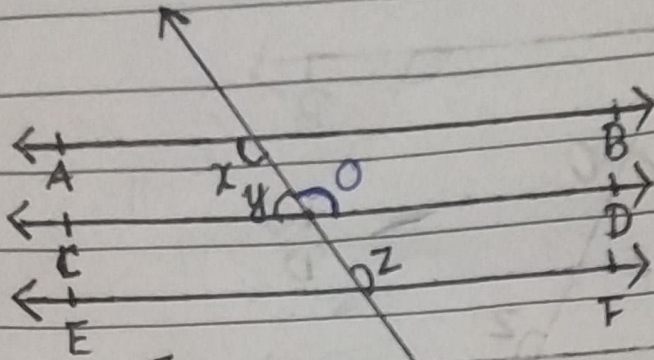


Fig. 6.29

ans) It is known that  $AB \parallel CD$ ,  $CD \parallel EF$   
As the angles on the same side of a transversal line sum up to  $180^\circ$ .

$$x + y = 180^\circ \text{ --- (i)}$$

also

$$\angle O = z \text{ (as corresponding angles)}$$

$$\text{and } y + \angle O = 180^\circ \text{ (linear pair)}$$

$$\text{So } y + z = 180^\circ$$

$$\text{Let } y \text{ be } 3a \text{ and } z \text{ be } 7a \text{ (as } y : z = 3 : 7)$$

$$\therefore 3a + 7a = 180^\circ$$

$$\rightarrow 10a = 180^\circ$$

$$\rightarrow a = \frac{180}{10} = 18^\circ$$

$$\text{Now, } y = 3 \times 18 = 54^\circ$$

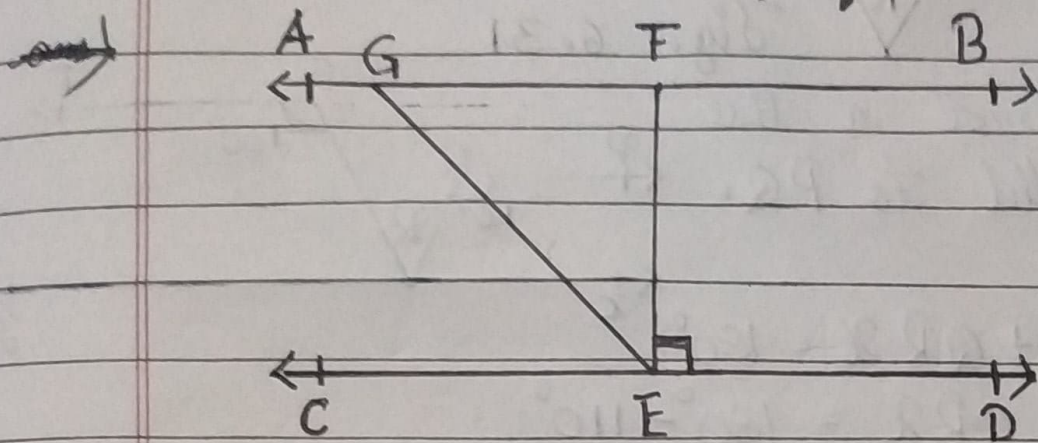
$$z = 7 \times 18 = 126^\circ$$

$$\text{Now, angle } x = x + y = 180^\circ$$

$$\Rightarrow x = 180^\circ - 54^\circ$$

$$\rightarrow x = 126^\circ$$

3) In Fig. 6.30, if  $AB \parallel CD$ ,  $EF \perp CD$  and  $\angle FED = 126^\circ$ , find  $\angle AGE$ ,  $\angle GEF$  and  $\angle FGE$



ans) Since  $AB$ ,  $CD$  and  $GE$  is a transversal.  
 It is given that  $\angle FED = 126^\circ$   
 So,  $\angle FED = \angle AGE = 126^\circ$  (Alternate interior angles)  
 Also,

$$\angle FED = \angle GEF + \angle FGE$$

As,  $EF \perp CD$ ,  $\angle FED = 90^\circ$

$$\therefore \angle GEF = 126^\circ - 90^\circ = 36^\circ$$

Again,  $\angle FGE + \angle FED = 180^\circ$  (~~linear pair~~ <sup>Transversal</sup>)

Putting the value of  $\angle FED = 126^\circ$ , we get,  
 $\angle FGE = 54^\circ$

So,

$$\angle AGE = 126^\circ$$

$$\angle GEF = 36^\circ$$

$$\angle FGE = 54^\circ$$

4) In Fig. 6.31, if  $PQ \parallel ST$ ,  $\angle PQR = 110^\circ$  and  $\angle RST = 130^\circ$ , find  $\angle QRS$ .  
[Hint: Draw a line parallel to  $ST$  through point  $R$ .]

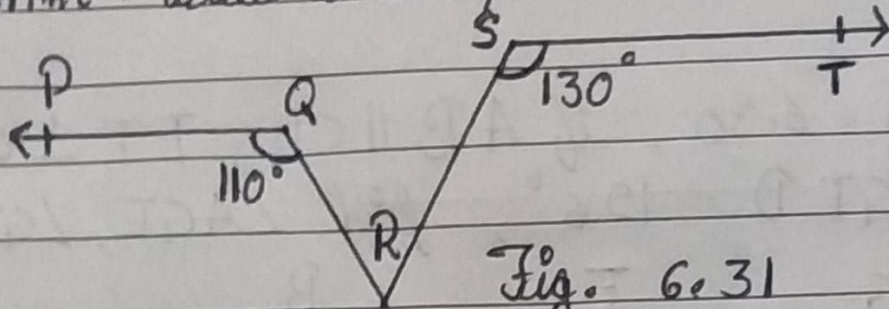
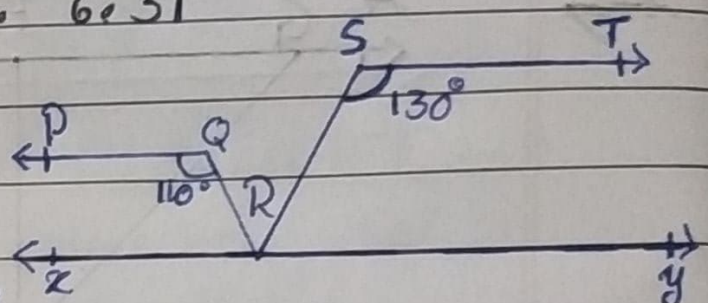


Fig. 6.31

ans) First construct a line  $XY$  parallel to  $PQ$ .



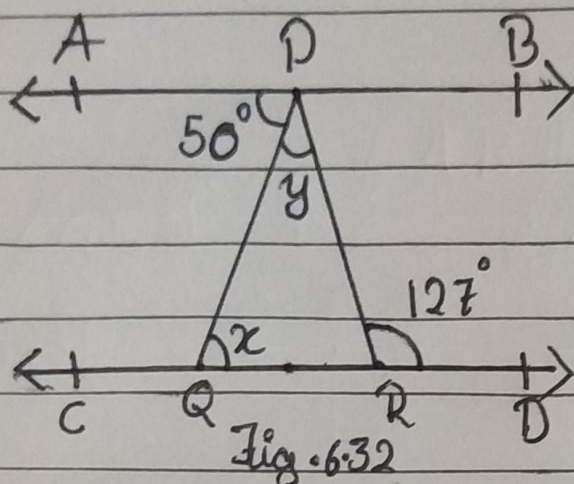
So,  $\angle PQR + \angle QRX = 180^\circ$   
 $\rightarrow \angle QRX = 180^\circ - 110^\circ$   
 $\therefore \angle QRX = 70^\circ$

Similarly,  
 $\angle RST + \angle SRY = 180^\circ$   
 $\rightarrow \angle SRY = 180^\circ - 130^\circ$   
 $\Rightarrow \angle SRY = 50^\circ$

Now, for the linear pairs on the  $XY$   
 $\angle QRX + \angle QRS + \angle SRY = 180^\circ$

Putting their respective values, we get  
 $\angle QRS = 180^\circ - 70^\circ - 50^\circ$   
 $= 60^\circ$

5) In Fig. 6.32, if  $AB \parallel CD$ ,  $\angle APQ = 50^\circ$  and  $\angle PRD = 127^\circ$ , find  $x$  and  $y$ .



ans) From the diagram,  
 $\angle APQ = \angle PQR$  (Alternate interior angles)  
 Now, putting the value of  $\angle APQ = 50^\circ$  and  $\angle PQR = x$   
 we get,

$$x = 50^\circ$$

also,

$\angle APR = \angle PRD$  (Alternate interior angles)

$$\angle APR = 127^\circ$$

We know that  $\angle APR = \angle APQ + \angle QPR$

Now, putting values, we get

$$127^\circ = 50^\circ + y$$

$$y = 77^\circ$$

$\therefore$  the value of  $x$  is  $50^\circ$  and  $y$  is  $77^\circ$ .