

4) The sides of the triangle are 18 cm, 10 cm and third side is unknown x .

So,

$$\text{Perimeter of the triangle} = 42 \text{ cm}$$

So,

$$\text{The length of the 3rd side} = 18 + 10 + x = 42 \text{ cm}$$

$$\Rightarrow x = 42 - 28 \text{ cm}$$

$$\Rightarrow x = 14 \text{ cm}$$

Hence,

$$\begin{aligned} \text{The semi Perimeter of the triangle} &= \frac{42}{2} \text{ cm} \\ &= 21 \text{ cm} \end{aligned}$$

$$\begin{aligned} \text{Area of the triangle} &= \sqrt{s(s-a)(s-b)(s-c)} \text{ cm}^2 \\ &= \sqrt{21(21-18)(21-10)(21-14)} \text{ cm}^2 \\ &= \sqrt{21 \times 3 \times 11 \times 7} \text{ cm}^2 \\ &= \sqrt{4851} \text{ cm}^2 \\ &= 21\sqrt{11} \text{ cm}^2 \end{aligned}$$

5) The sides of the triangle are in the ratio of 12:17:25 and its perimeter is 540 cm. Let the sides be $12x$, $17x$ and $25x$.

$$\text{The length of the sides} = 12x + 17x + 25x = 540 \text{ cm}$$

$$\Rightarrow 54x = 540 \text{ cm} \Rightarrow x = \frac{540}{54} \text{ cm} \Rightarrow x = 10 \text{ cm}$$

$$\text{Hence, } 12x = 12 \times 10 = 120 \text{ cm}, 17x = 17 \times 10 = 170 \text{ cm} \text{ \& } 25x = 25 \times 10 = 250 \text{ cm}$$

$$\text{Semi Perimeter of the triangle} = \frac{540}{2} \text{ cm}$$

$$= 270 \text{ cm}$$

$$\begin{aligned} \text{Area of the triangle} &= \sqrt{s(s-a)(s-b)(s-c)} \text{ cm}^2 \\ &= \sqrt{270(270-250)(270-170)(270-120)} \text{ cm}^2 \\ &= \sqrt{270 \times 20 \times 100 \times 150} \text{ cm}^2 \\ &= \sqrt{81000000} \text{ cm}^2 \\ &= 9000 \text{ cm}^2 \end{aligned}$$