

6.7.21

CH-4 Home Assignment

1) Ampere's circuital law states that the line integral of magnetic field \vec{B} around any closed path in vacuum is μ_0 times the total current through the closed path.

Let n be the no. of turns per unit length.

Total no. of ~~the~~ turns = nh

Enclosed current is $I_e = I(nh)$

From Ampere's circuital law

$$BI = \mu_0 I_e$$

$$Bh = \mu_0 I(nh)$$

$$B = \mu_0 n I$$

$$2) a) \oint \vec{B} \cdot d\vec{l} = \mu_0 I$$

$$\oint_{pqrs} \vec{B} \cdot d\vec{l} = \int_{pq} \vec{B} \cdot d\vec{l} + \int_{qr} \vec{B} \cdot d\vec{l} + \int_{rs} \vec{B} \cdot d\vec{l} + \int_{sp} \vec{B} \cdot d\vec{l}$$

$$\int_{qr} \vec{B} \cdot d\vec{l} = \int_{sp} \vec{B} \cdot d\vec{l} = \int B dl \cos 90 = 0$$

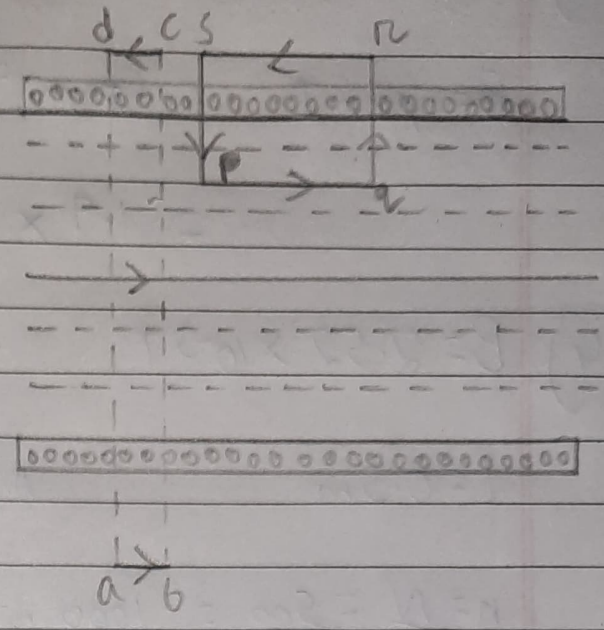
$$\int_{rs} \vec{B} \cdot d\vec{l} = 0$$

$$\oint_{pqrs} \vec{B} \cdot d\vec{l} = \int_{pq} \vec{B} \cdot d\vec{l} = BL$$

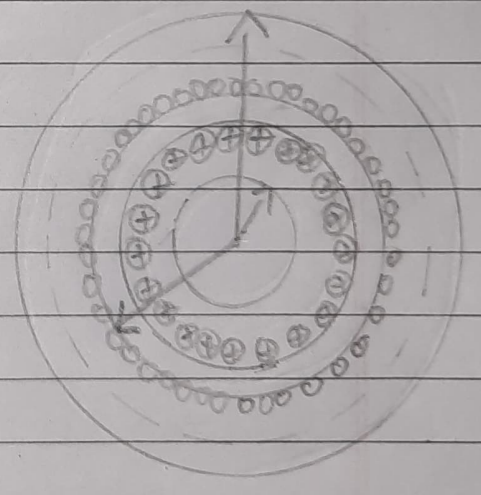
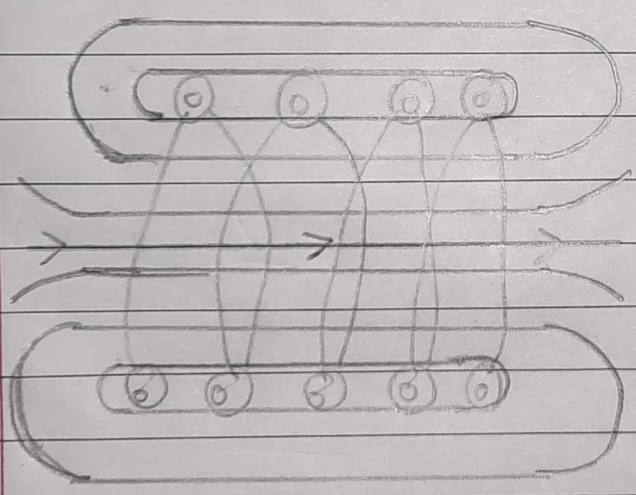
$$\oint \vec{B} \cdot d\vec{l} = \mu_0 I$$

$$BL = \mu_0 (n \ell I)$$

$$B = \mu_0 n I$$



b) Magnetic lines do not exist outside the body of a toroid. Toroid is a closed & solenoid is open on both side. Magnetic field is uniform inside a toroid whereas, for a solenoid, it is different at 2 ends & centre.



c) The magnetic field is made strong by

- i) Passing large current &
- ii) Using laminated coil of soft iron.

$$3) \quad n = 300 \quad i = 5 \text{ A} \quad l = 0.5 \text{ m} \quad r = 10^{-2} \text{ m}$$

$$B = \mu_0 n i = 4\pi \times 10^{-7} \times 300 \times 5$$

$$= 1.9 \times 10^{-3} \text{ T}$$

$$4) \quad B = 2.52 \times 10^{-3} \text{ T}$$

$$l = 0.5 \text{ m} \quad N = 500$$

$$n = \frac{N}{l} = \frac{500}{0.5} = 1000 \text{ m}^{-1}$$

$$B = \mu_0 n i$$

$$\Rightarrow i = \frac{B}{\mu_0 n} = \frac{2.52 \times 10^{-3}}{4\pi \times 10^{-7} \times 1000} = 2.0 \text{ A}$$