

# Magnetism And Matter



3)  $\theta = 30^\circ$      $B = 0.25 \text{ T}$      $\tau = 4.5 \times 10^{-2} \text{ J}$      $M = ?$

$$\tau = MB \sin \theta \Rightarrow M = \frac{\tau}{B \sin \theta}$$

$$\Rightarrow M = \frac{4.5 \times 10^{-2}}{0.25 \times \sin 30} = 0.36 \text{ JT}^{-1}$$

4)  $M = 0.32 \text{ JT}^{-1}$      $B = 0.15 \text{ T}$

a) For stable equilibrium, the angle bet<sup>n</sup> magnetic moment  $\vec{m}$  & magnetic field  $\vec{B}$ ,  $\theta = 0^\circ$   
Potential energy,  $U = -MB \cos \theta$   
 $= -0.32 \times 0.15 \times 1 = -4.8 \times 10^{-2} \text{ J}$

b) For the unstable equilibrium, the angle bet<sup>n</sup>  $\vec{m}$  &  $\vec{B}$ ,  $\theta = 180^\circ$  & potential energy will be maximum, i.e.  $U = -MB \cos 180 = -0.32 \times 0.15 \times (-1)$   
 $= 4.8 \times 10^{-2} \text{ J}$

5)  $N = 800$      $A = 2.5 \times 10^{-4} \text{ m}^2$      $I = 3 \text{ A}$

$$M = NIA = 800 \times 3 \times 2.5 \times 10^{-4} = 0.6 \text{ J/T}$$

By using maxwell's right hand <sup>grip</sup> thumb rule, the magnetic field is along the axis of solenoid.

8)  $N = 2000$      $A = 1.6 \times 10^{-4} \text{ m}^2$      $I = 4 \text{ A}$

a) Magnetic moment associated with Solenoid,  
 $M = NIA = 2000 \times 4 \times 1.6 \times 10^{-4}$   
 $= 1.28 \text{ J/T}$

6) Net force on solenoid is 0.

$$\tau = MB \sin \theta = 1.28 \times 1.5 \times 10^{-2} \times \sin 30$$

$$= 0.048 \text{ Nm}$$

This torque tends to align the axis of the solenoid along the field  $\vec{B}$ .

8)  $N = 16$        $r = 10 \text{ cm} = 0.1 \text{ m}$        $I = 0.75 \text{ A}$   
 $B = 5 \times 10^{-2} \text{ T}$        $f = 2.0 \text{ s}^{-1}$

Magnetic moment of coil,  $M = nIA = 16 \times 0.75 \times \pi (0.1)^2$   
 $= 0.377 \text{ J/T}$

frequency of oscillation,  $f = \frac{1}{2\pi} \sqrt{\frac{mB}{I}}$

Moment of Inertia,  $I = \frac{mB}{4\pi^2 f^2} = \frac{0.377 \times 5 \times 10^{-2}}{4 \times 3.14 \times 3.14 \times 2 \times 2}$   
 $= 1.2 \times 10^{-4} \text{ kg m}^2$

11) angle of declination,  $\theta = 12^\circ$  west

$\delta = 60^\circ$        $B_H = 0.16 \text{ G}$

$\therefore B = \frac{B_H}{\cos \delta} = \frac{0.16}{\cos 60} = \frac{0.16 \times 2}{1} = 0.32 \text{ G}$

The earth's magnetic field lies in a vertical plane  $12^\circ$  west of geographical meridian at an angle  $60^\circ$  above the horizontal.

13) As the null points lies on the axis of the magnets, therefore



$$B_{axial} = \frac{\mu_0}{4\pi} \cdot \frac{2m}{r^3} = B_H$$

Magnetic field of the magnet on its normal bisector at the same distance will be

$$B_{equa} = \frac{\mu_0}{4\pi} \frac{m}{r^3} = \frac{B_H}{2} = 0.36 \div 2 = 0.18 \text{ G}$$

Total magnetic field at the required point on the normal bisector is

$$B_{equa} + B_H = 0.18 + 0.36 = 0.54 \text{ G}$$

18) Suppose the neutral point lies at a distance  $r$  from the cable. Then at the neutral point,

$$\frac{\mu_0 I}{2\pi r} = B_H$$

$$\text{or } r = \frac{\mu_0 I}{2\pi B_H} = \frac{4\pi \times 10^{-7} \times 2.5}{2\pi \times 0.33 \times 10^{-4}} = 1.5 \times 10^{-2} \text{ m} = 1.5 \text{ cm}$$

As the direction of the magnetic field of the cable is opp to that of  $B_H$  at point above the cable, so the line of neutral point lies parallel to and above the cable at a distance of 1.5cm from it.