

Home Assignment

- 1.) Ampere's Circuital law:
The line integral of magnetic field of induction \vec{B} around any closed path in free space is equal to absolute permeability of free space μ_0 times the total current flowing through area bounded by the path.

$$\text{Mathematically, } \oint \vec{B} \cdot d\vec{l} = \mu_0 I$$

Calculation of magnetic field inside a long straight solenoid:

According to Ampere's Circuital law,

$$\oint \vec{B} \cdot d\vec{l} = \mu_0 \times \text{total current through the loop abcd}$$

$$\oint \vec{B} \cdot d\vec{l} = \int_a^b \vec{B} \cdot d\vec{l} + \int_c^d \vec{B} \cdot d\vec{l} + \int_d^a \vec{B} \cdot d\vec{l}$$

$$\text{But } \int_b^c \vec{B} \cdot d\vec{l} = \int_b^c B dl \cos 90^\circ = 0$$

$$\int_c^d \vec{B} \cdot d\vec{l} = 0 \text{ as } B = 0 \text{ for points outside the solenoid.}$$

$$\therefore \oint \vec{B} \cdot d\vec{l} = \int_a^b \vec{B} \cdot d\vec{l}$$

$$= \int_a^b B dl \cos 0^\circ = B \int_a^b dl = Bl$$

Where,

$$l = \text{length}, \quad n = \frac{N}{l} \text{ (No. of turns per unit length)}$$

$$N = nl \text{ (Total no. of turns in length)}$$

Total current flowing = nI

$$\text{Now, } \oint \vec{B} \cdot d\vec{l} = \mu_0 I_{\text{enc}} = \mu_0 n l I$$

$$\Rightarrow B l = \mu_0 n l I$$

$$\Rightarrow B = \mu_0 n I$$

2.) a) Same as 1) 200 turns.

b)

- \Rightarrow In a toroid, magnetic lines do not exist outside the body.
- \Rightarrow Toroid is closed whereas the solenoid is open on both sides.
- \Rightarrow Magnetic field is uniform inside a toroid, whereas for solenoid, it is different at the two ends and the center.

c) The magnetic field lines inside a given solenoid is made strong by:

- \Rightarrow Increasing the current.
- \Rightarrow using a soft ~~iron~~ iron.
- \Rightarrow Increasing the no. of coils in the solenoid.

Q3 $n = 300 \text{ turns/m}$ $I = 5 \text{ A}$, $l = 0.5 \text{ m}$

$$B = \mu_0 n I$$

$$= 4\pi \times 10^{-7} \times 300 \times 5$$

$$= 18840 \times 10^{-6}$$

$$= 1.884 \times 10^{-2} \text{ T}$$

Q.9

$$l = 0.5 \text{ m}$$

$$N = 500$$

$$\text{Flux density} = 2.25 \times 10^{-3} \text{ T}$$

find the current in the solenoid.

$$\text{Given, } \mu_0 = 4\pi \times 10^{-7} \text{ Hm}^{-1}$$

$$B = \mu_0 n \cdot I$$

$$B = \frac{\mu_0 N I}{l}$$

$$2.25 \times 10^{-3} = \frac{4\pi \times 10^{-7} \times 500 \times I}{0.5}$$

$$I = \frac{0.5 \times 2.25 \times 10^{-3}}{4\pi \times 10^{-7} \times 500}$$

$$\therefore I = 1.79 \approx 1.8 \text{ A}$$