

H.W

Magnetism and Matter

$$3.) \quad B = 0.25 \text{ T}$$

$$T = 4.5 \times 10^{-2} \text{ J}$$

$$\phi = 30^\circ$$

$$T = mB \sin \phi$$

$$m = \frac{T}{B \sin \phi} = \frac{4.5 \times 10^{-2}}{0.25 \times \sin 30^\circ} = 0.36 \text{ J/T}$$

$$4.) \quad m = 0.32 \text{ J/T}$$

$$B = 0.15 \text{ T}$$

a) magnetic field is  $0^\circ$ 

$$P.E \text{ of the system} = -mB \cos \phi$$

$$= -0.32 \times 0.15 \cos 0^\circ$$

$$= -4.8 \times 10^{-2} \text{ J}$$

b)  $\phi = 180^\circ$

$$P.E = -mB \cos \phi$$

$$= -0.32 \times 0.15 \cos 180^\circ$$

$$= 4.8 \times 10^{-2} \text{ J}$$

$$5.) \quad n = 800, \quad A = 2.5 \times 10^{-4} \text{ m}^2, \quad I = 3.0 \text{ A}$$

$$M = nIA$$

$$= 800 \times 3 \times 2.5 \times 10^{-4}$$

$$= 0.6 \text{ J/T}$$

$$7) a) m = 1.5 \text{ J/r}, B = 0.22 \text{ T}$$

$$i) \phi_1 = 0^\circ$$

$$\phi_2 = 90^\circ$$

$$W = -mB(\cos\phi_2 - \cos\phi_1)$$

$$= -1.5 \times 0.22 (\cos 90^\circ - \cos 0^\circ)$$

$$= 0.33 (0 - 1)$$

$$= 0.33 \text{ J}$$

$$ii) \phi_1 = 0^\circ$$

$$\phi_2 = 180^\circ$$

$$W = -mB(\cos\phi_2 - \cos\phi_1)$$

$$= 1.5 \times 0.22 (\cos 180^\circ - \cos 0^\circ)$$

$$= -0.33 (-1 - 1)$$

$$= +0.66 \text{ J}$$

$$b) i) \phi = \phi_2 = 90^\circ$$

$$T = mB \sin\phi = mB \sin 90^\circ$$

$$= 1.5 \times 0.22 \sin 90^\circ$$

$$= 0.33 \text{ J}$$

For case (i.),

$$\phi = \phi_2 = 180^\circ$$

$$T = MB \sin \phi = MB \sin 180^\circ = 0.5$$

8)  $n = 2000, A = 1.6 \times 10^{-4} \text{ m}^2, I = 4.0 \text{ A}$

a)  $M = nAI$   
 $= 2000 \times 4 \times 1.6 \times 10^{-4}$   
 $= 1.28 \text{ A m}^2$

b)  $B = 7.5 \times 10^{-2} \text{ T}, \phi = 30^\circ$

$$T = MB \sin \phi$$

$$= 1.28 \times 7.5 \times 10^{-2} \sin 30^\circ$$

$$= 0.048 \text{ J}$$

$\therefore$  Since the magnetic field is uniform, the force on the solenoid is zero. The torque on the solenoid is  $0.048 \text{ J}$

9.)  $N = 16, r = 10 \text{ cm} = 0.1 \text{ m}, A = \pi r^2 = \pi \times (0.1)^2$   
 $I = 0.75 \text{ A}, B = 50 \times 10^{-2} \text{ T}, \omega = 2.0 \text{ s}^{-1}$

$$M = NIA = NI \pi r^2 = 16 \times 0.75 \times \pi \times (0.1)^2$$

$$= 0.377 \text{ J/T}$$

$$\omega = \frac{1}{2\pi} \sqrt{\frac{MB}{I}} \Rightarrow I = \frac{MB}{4\pi^2 \omega^2} = \frac{0.377 \times 5 \times 10^{-2}}{4\pi^2 \times (2)^2}$$

$\therefore$  Axis of rotation  
 $= 1.19 \times 10^{-9} \text{ kg m}^2$

$$= 1.2 \times 10^{-9} \text{ kg m}^2$$

11)  $\phi = 12^\circ$ ,  $\delta = 60^\circ$ ,  $B_H = 0.16 \text{ G}$

$$B_H = B \cos \delta = \frac{0.16}{\cos 60^\circ} = 0.32 \text{ G}$$

Earth's magnetic field lies in the vertical plane,  $12^\circ$  west of the geographic meridian, making an angle of  $60^\circ$  with the horizontal direction. Its magnitude is  $0.32 \text{ G}$ .

13)  $H = 0.36 \text{ G}$

$$B_1 = \frac{\mu_0 2M}{4\pi d^3} = H \quad \text{--- (i)}$$

$\mu_0$  - permeability of free space

$M$  = magnetic moment

$$B_2 = \frac{\mu_0 M}{4\pi d^3} = \frac{H}{2} \quad \text{[using eq (i)]}$$

$$\begin{aligned} \text{Total } \Rightarrow B &= B_1 + B_2 = H + \frac{H}{2} \\ &= 0.36 + 0.18 \\ &= 0.54 \text{ G} \end{aligned}$$

18.)

Current in the wire = 2.5 A  
The earth's magnetic field at a location  $B = 0.33 \text{ G}$   
 $= 0.33 \times 10^{-4} \text{ T}$   
Angle of dip is zero,  $\delta = 0$

$$B_H = B \cos \delta = 0.33 \times 10^{-4} \cos 0 \\ = 0.33 \times 10^{-4} \text{ T}$$

$$B_C = \left( \frac{\mu_0}{2\pi} \right) \times \left( \frac{I}{r} \right) \\ = \left( \frac{4\pi \times 10^{-7}}{2\pi} \right) \times \left( \frac{2.5}{r} \right) \\ = \left( 5 \times 10^{-7} / r \right)$$

$$B_H = B_C \\ 0.33 \times 10^{-4} = 5 \times 10^{-7} / r$$

$$r = \frac{5 \times 10^{-7} \times 10^{-4}}{0.33}$$

$$= 0.015 \text{ m}$$

$$= 1.5 \text{ cm}$$