

5.) Ans In isosceles  $\triangle ABC$ , we have

$$AB = AC$$

$$\angle ABC = \angle ACB$$

[Angle opposite to equal sides are equal]

Now in isosceles  $\triangle DCB$ , we have  $BD = CD$

$$\angle DBC = \angle DCB$$

Adding (i) and (ii)

$$\angle ABC + \angle DBC = \angle ACB + \angle DCB$$

$$\Rightarrow \angle ABD = \angle ACD$$

$$AB = AC$$

$$\angle ACB = \angle ABC$$

[Angles opposite to equal sides are equal]

Adding (i) and (ii)

$$\angle ACB + \angle ACD = \angle ABC + \angle ADC$$

$$\Rightarrow \angle BCD = \angle ABC + \angle ADC$$

Now, in  $\triangle BCD$ , we have

$$\angle BCD + \angle DBC + \angle BDC = 180^\circ$$

$$\therefore \angle BCD + \angle BCD = 180^\circ$$

$$2\angle BCD = 180^\circ$$

$$\angle BCD = 90^\circ$$

Hence,  $\angle BCD = 90^\circ$  or a right angle.

7.) In  $\triangle ABC$ , we have

$$\angle A = 90^\circ \quad \text{? Given.}$$

$$\text{and } AB = AC$$

We know that angle opposite to equal sides of an isosceles triangle are equal.

$$\text{So, } \angle B = \angle C$$

Since,  $\angle A = 90^\circ$ , therefore sum of remaining two angles =  $90^\circ$ .

Hence,  $\angle B = \angle C = 45^\circ$ .

8.  $\triangle ABC$  is an equilateral

So,  $AB = BC = AC$

Now,  $AB = AC$

$\Rightarrow \angle ACB = \angle ABC$

Again,  $BC = AC$

$\Rightarrow \angle BAC = \angle ABC$

Now in  $\triangle ABC$

$\angle ABC + \angle ACB + \angle BAC = 180^\circ$

$\Rightarrow \angle ABC + \angle ABC + \angle ABC = 180^\circ$

$\Rightarrow \angle ABC = 180^\circ / 3$

$\Rightarrow \angle ABC = 60^\circ$

Also, from (i) and (ii)

$\angle ACB = 60^\circ$  and  $\angle BAC = 60^\circ$

Hence, each angle of an equilateral triangle is  $60^\circ$ .