

3) (i) In $\triangle ABM$ and $\triangle PQN$

we have

$$BM = QN$$

$$\left[BC = \frac{1}{2} QR \right]$$

$$\Rightarrow \frac{1}{2} BC = \frac{1}{2} QR$$

$$AB = PQ$$

$$AM = PN$$

$$\therefore \triangle ABM \cong \triangle PQN \text{ [SSS congruence]}$$

$$\Rightarrow \angle ABM = \angle PQN$$

(ii) Now, in $\triangle ABC$ and $\triangle PQR$, we have

$$AB = PQ$$

$$\angle ABC = \angle PQR$$

$$BC = QR$$

$$\therefore \triangle ABC \cong \triangle PQR \text{ [SAS congruence]}$$

4.) BE and CF are altitudes of a $\triangle ABC$

$$\therefore \angle BEC = \angle CFB = 90^\circ$$

Now, in right triangles $\triangle BEC$ and $\triangle CFB$, we have
Hyp, $BC =$ Hyp, BC [Common]
Side $BE =$ Side CF [Given]

$$\therefore \triangle BEC \cong \triangle CFB \text{ [By RHS Congruence]}$$

$$\therefore \angle BCE = \angle CBF \text{ (CPCT)}$$

Now, in $\triangle ABC$, $\angle B = \angle C$

$$\therefore AB = AC$$

Hence $\triangle ABC$ is an isosceles triangle.

5.) Draw $AP \perp BC$

In $\triangle ABP$ and $\triangle ACP$, we have

$$AB = AC \quad [\text{Given}]$$

$$\angle APB = \angle APC \quad [\text{Each} = 90^\circ]$$

$$AP = AP \quad [\text{Common}]$$

$$\triangle ABP \cong \triangle ACP \quad [\text{By RHS congruence}]$$

$$\text{Also } \angle B = \angle C \quad [\text{CPCT}]$$