

5.) $PR > PQ$
 $\angle PQR > \angle PRQ$ (i)

[Angle opposite to longer side is greater]

$\angle QPS > \angle RPS$ [PS bisects $\angle QRR$] (ii)

In $\triangle PQR$, $\angle PQS + \angle QPS + \angle PSQ = 180$

$\Rightarrow \angle PSQ = 180 - \angle PQS + \angle QRS$ (iii)

Similarly in $\triangle PSR = 180 - \angle PRS + \angle QRS$

$\Rightarrow \angle PRS = 180 - \angle QRS + \angle QRS$ from (ii) and (iii)

From (i) we know that $\angle PQS < \angle PRS$

So from (iii) and (iv) $\angle PQS < \angle PRS$

$\Rightarrow \angle PSR > \angle PSQ$

6.) We have a line ℓ and O is a point not on ℓ

$OP \perp \ell$

We have a line ℓ and a point O not on ℓ .
 $OP \perp \ell$ and $OP \perp CS$

In $\triangle OPQ$, $\angle P = 40^\circ$

$\therefore \angle Q$ is an acute angle
 $\angle Q < 90^\circ$

$\therefore \angle Q < \angle P$

Hence, $OP < OQ$

Similarly, we can prove that OP is shorter than OR , OS etc.