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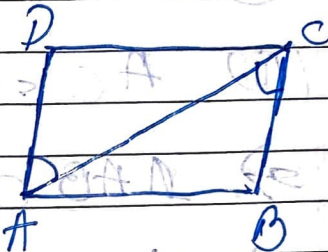
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1) In  $\triangle ABC$  and  $\triangle ADC$

(i)  $\angle BAC = \angle DCA$

(ii)  $AC = AC$  [common]

(iii)  $\angle BCA = \angle DAC$



$\Rightarrow \triangle ABC \cong \triangle ADC$

2) Proof

In  $\triangle ABC$  and  $\triangle BAD$

$AB = AB$

$BC = AD$

[Opposite sides of a parallelogram are equal]

$\therefore AC = BD$  [Diagonal]

$\therefore \triangle ABC \cong \triangle BAD$  [SSS]

$\angle ABC = \angle BAD$

Since,  $ABCD$  is a parallelogram  
 $\angle ABC + \angle BAD = 180^\circ$

$\angle ABC + \angle ABC = 180^\circ$

$2\angle ABC = 180^\circ$

$\angle ABC = \angle BAD = 90^\circ$

3.  $\triangle ABC$  and  $\triangle CDA$

(i)  $AB = CD$  [given]

(ii)  $BC = AD$  [given]

(iii)  $AC = AC$  (common)

$\Rightarrow \triangle ABC \cong \triangle CDA$  [SSS]

$\Rightarrow \angle BAC = \angle ACD$  [by CPCT]

but these two are a.i.a

$\Rightarrow CD \parallel AB$

$\angle BCA = \angle CAD$  [by CPCT]

but these 2 are a.i.a

$\Rightarrow AD \parallel BC$

[mirror]  $AB = CD$   
[222]  $BC = AD$   
 $\triangle ABC = \triangle CDA$   
 $AC = CA$

Since  $\triangle ABC$  is a parallelogram  
 $\angle ABC + \angle BAD = 180^\circ$

$\angle ABC + \angle ABC = 180^\circ$

$2\angle ABC = 180^\circ$

$\angle ABC = 90^\circ$