

## Revision Exercise (Chapter 8)

1. Find the JCF of:

i) 108, 288 and 420

Ans: Using division method we get  
HCF of 108 and 288

$$\begin{array}{r}
 108 \quad | \quad 288 \quad | \quad 2 \\
 -\quad 216 \\
 \hline
 72 \quad | \quad 108 \quad | \quad 1 \\
 -\quad 72 \\
 \hline
 36 \quad | \quad 72 \quad | \quad 12 \\
 -\quad 72 \\
 \hline
 0
 \end{array}$$

Here the last divisor is 36

$\therefore$  HCF of 108 and 288 is 36

HCF of 108, 288 and 420 = HCF of 36 and 420

$$\begin{array}{r}
 36 \overline{)420} \\
 -36 \\
 \hline
 60 \\
 -36 \\
 \hline
 24 \overline{)36} \\
 -24 \\
 \hline
 12 \quad 24 \quad 2 \\
 -24 \\
 \hline
 0
 \end{array}$$

Here the last divisor is 12

So, the HCF of 36 and 480 is 12

The HCF of 108, 288 and 420 is 12.

ii) 36, 54 and 138

Ans- By using division method we get,  
HCF of 36 and 54

$$\begin{array}{r} 36 \mid 54 \mid 1 \\ -36 \\ \hline 18 \mid 36 \mid 2 \\ -36 \\ \hline 0 \end{array}$$

Here the last divisor is 18.

∴ The HCF of 36 and 54 is 18.

HCF of 36, 54 and 138 = HCF of 18 and 138

$$\begin{array}{r} 18 \mid 138 \mid 7 \\ -126 \\ \hline 12 \mid 18 \mid 1 \\ -12 \\ \hline 6 \mid 12 \mid 2 \\ -12 \\ \hline 0 \end{array}$$

Here the last divisor is 6

So, the HCF of 18 and 138 is 6

∴ The HCF of 36, 54 and 138 is 6

2. Find the LCM of:

i) 72, 80 and 252

Ans- By using Common division method the LCM of 72, 80 and 252 is

2	72, 80, 252
2	36, 40, 126
2	18, 20, 63
2	9, 10, 63
3	9, 5, 63
3	3, 5, 21
	1, 5, 7

$$\text{LCM of } 72, 80 \text{ and } 252 = 2 \times 2 \times 2 \times 2 \times 3 \times 3 \times 5 \times 7 \\ = 5040$$

ii) 48, 66 and 120

Ans- By using Common division method the LCM of 48, 66 and 120 is

2	48, 66, 120
2	24, 33, 60
2	12, 33, 30
3	6, 33, 15
	2, 11, 5

$$\text{LCM of } 48, 66, 120 \text{ is } = 2 \times 2 \times 2 \times 2 \times 3 \times 5 \times 11 \\ = 2640$$

3. State true or false (Give an example in support of your answer in each case):

i) HCF of two prime numbers is 1

Ans- The Statement is True.

Example: The two prime numbers are 2 and 3.

HCF of 2 and 3 =

By using division method we get

$$\begin{array}{r} 2 \mid 3 \mid 1 \\ \underline{-2} \quad \quad \quad \\ 1 \mid 2 \mid 2 \\ \underline{-2} \quad \quad \quad \\ 0 \end{array}$$

Here the last divisor is 1.

So, the HCF of 2 and 3 is 1.

So, The prime numbers have no common factor except 1.

$\therefore$  The above statement is True.

ii) HCF of two co-prime numbers is 1

Ans) The Statement is True

Example: Two co-prime numbers are 4 and 9

HCF of 4 and 9 =

Using Division method we get

$$\begin{array}{r} 4 \mid 9 \mid 2 \\ \underline{-8} \quad \quad \quad \\ 1 \mid 4 \mid 4 \\ \underline{-4} \quad \quad \quad \\ 0 \end{array}$$

Here the last divisor is 1

So, the HCF of 4 and 9 is 1

$\therefore$  The above statement is True.

iii) LCM of two prime numbers is equal to their product.

Ans- The statement is True.

Example: The two prime numbers are - 5 and 11

Using Common division Method LCM of 5 and 11 is

$$\begin{array}{r} 5 | 5, 11 \\ 11 | 1, 11 \\ \hline 1, 1 \end{array}$$

$$LCM = 5 \times 11 = 55$$

$$\text{The product of 5 and } 11 = 5 \times 11$$

$$= 55$$

So, the two prime numbers is equal to their product.

∴ The above statement is True.

iv) LCM of two co-prime numbers is equal to their product.

Ans- The statement is True.

Example: The two co-prime numbers are 4 and 9

Using Common division method LCM of 4 and 9 is

$$\begin{array}{r} 2 | 4, 9 \\ 3 | 2, 9 \\ \hline 2, 3 \end{array}$$

$$LCM = 2 \times 2 \times 3 \times 3 = 36$$

$$\text{The product of 4 and } 9 \text{ is } = 4 \times 9$$

$$= 36$$

So, The LCM of two co-prime numbers is equal to their product.

∴ The above statement is True.

4. The product of two numbers is 12096 and their HCF is 36.  
Find their LCM.

Ans- Product of two numbers = 12096

HCF of the two numbers = 36

Relationship between HCF and LCM is

Product of two numbers = Product of their HCF and LCM

Product of two numbers = 12096

So as the relation,

$$\text{HCF} \times \text{LCM} = 12096$$

~~$$36 \times \text{LCM} = 12096$$~~

$$\text{LCM} = 12096 / 36$$

$$= 336$$

∴ The LCM of the two numbers is 336.

5. The product of the HCF and LCM of two numbers is 1152. If one number is 48, find the other one.

Ans- Product of the HCF and LCM = 1152

One number = 48

Relationship between HCF and LCM =

Product of HCF and LCM = Product of the two numbers

Product of the HCF and LCM = 1152

So as per the relation,

Product of the two numbers = 1152

$$48 \times \text{Other number} = 1152$$

$$\text{Other number} = 1152 / 48$$

$$= 24$$

∴ The other number is 24.

6.i) Find the smallest number that is completely divisible by 28 and 42.

Ans We know that the least number which is divisible by 28 and 42 is their LCM.

LCM of 28 and 42 =

$$\begin{array}{r} 2 | 28, 42 \\ 7 | 14, 21 \\ \quad 2, 3 \end{array}$$

$$\text{LCM of } 28 \text{ and } 42 = 2 \times 2 \times 3 \times 7 = 84$$

∴ The smallest number that is completely divisible by 28 and 42 is 84.

ii) Find the largest number than can divide 28 and 42 completely.

Ans- We know that the largest number which can divide 28 and 42 completely will be their HCF.

HCF of 28 and 42 =

$$\begin{array}{r} 28 | 42 | 1 \\ \hline 28 | 28 | 2 \\ \hline 14 | 28 | 2 \\ \hline 14 | 14 | 0 \end{array}$$

Hence the last divisor is 14

∴ The HCF of 28 and 42 is 14

∴ The ~~smallest~~ largest number that can divide 28 and 42 completely is 14.

7. Find the LCM of 140 and 168. Use the LCM obtained to find the HCF of given numbers.

Ans- Numbers are 140 and 168

LCM of 140 and 168 =

$$\begin{array}{r} 2 | 140, 168 \\ 2 | 70, 84 \\ 7 | 35, 42 \\ \hline & 5, 6 \end{array}$$

$$\text{LCM of } 140, 168 = 2 \times 2 \times 7 \times 5 \times 6 = 840$$

HCF = 1<sup>st</sup> number  $\times$  2<sup>nd</sup> number

$$\begin{aligned} \text{L.C.M} \\ = \frac{140 \times 168}{840} &= \frac{23,520}{840} \\ &= 28 \end{aligned}$$

$\therefore$  The LCM of 140 and 168 is 840 and The HCF of 140 and 168 is 28.

8. Find the HCF of 108 and 450 and use the HCF obtained to find the LCM of the given numbers.

Ans- Numbers are given = 108 and 450

HCF of 108 and 450

$$\begin{array}{r} 108 | 450 | 4 \\ \hline 432 \\ 18 | 108 | 6 \\ \hline 108 \\ 0 \end{array}$$

$\therefore$  The last divisor is 18

$\therefore$  HCF of 108 and 450 is 18.

$$\text{LCM} = \frac{1^{\text{st}} \text{ number} \times 2^{\text{nd}} \text{ number}}{\text{H.C.F}} = \frac{108 \times 450}{18} = 2700$$

$\therefore$  The HCF of 108 and 450 is 18 & LCM of 108 and 450 is 2700.