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① The radius of the circular path by the proton in the magnetic field change can be described as

$$r = \frac{1}{B} \sqrt{\frac{2mV}{q}}$$

where, magnetic field = B
potential difference = V

Therefore $r \propto \sqrt{V}$

Let r be the radius when the potential difference is V and r' be the radius when the potential difference is $2V$

$$\frac{r'}{r} = \sqrt{\frac{2V}{V}} = \sqrt{2}$$

② mass of deuteron = $2m$ (1 proton + 1 neutron)
mass of proton = m (1 proton)

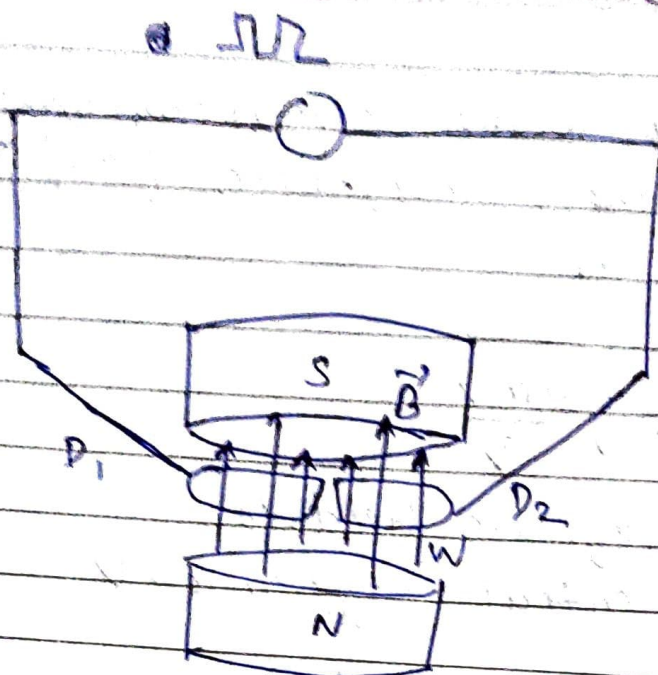
$$\therefore R(\text{proton}) = \frac{mv}{qB}$$

$$R(\text{deuteron}) = \frac{2m \times v}{2qB}$$

$$\therefore \text{Ratio} \left(\frac{\text{proton}}{\text{deuteron}} \right) = \frac{1}{2}$$

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Working:

A cyclotron accelerates a charged particle beam using a high frequency alternating voltage which is applied between two hollow 'D'-shaped sheet metal electrodes inside a vacuum chamber. An alternating voltage of several thousand volts are applied between the dees.

Cyclotron frequency is independent of the velocity of charged particle. Consider a particle of charge q revolving in the path of radius r with a velocity v . Centripetal force = Lorentz force due to magnetic field B . Therefore, frequency is independent of velocity.

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(4) (i) Let us consider: mass of proton m

Charge of proton = q

Mass of alpha particle = $4m$

Charge of alpha particle = $2q$

Cyclotron frequency

$$v = \frac{Bqr}{2\pi m} \Rightarrow v \propto \frac{q}{m}$$

For proton = Frequency, $v_p \propto \frac{q}{m}$

For alpha particle: Frequency

$$v_\alpha \propto \frac{2q}{4m}$$

$$\Rightarrow v_\alpha \propto \frac{q}{2m}$$

Thus, particle will not accelerate with same frequency.

(ii) velocity, $v = \frac{Bqr}{m} \Rightarrow v \propto \frac{q}{m}$

for proton: velocity, $v_p \propto \frac{q}{m}$

For alpha particle velocity

$$v_\alpha \propto \frac{2q}{4m} \text{ or } v_\alpha \propto \frac{q}{2m}$$

Thus, particle will not exit the dees with same velocity.