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Date _____
Page _____

Home Assignment

1)

$v =$ potential difference

Angle between motion $\theta = 90^\circ$

$$\frac{mv^2}{r} = qvB$$

$$R_1 = \frac{mv}{qB}$$

$$R_2 = \left(\frac{m}{qB}\right)^{1/2} v^2$$

$$R_2 = \left(\frac{m}{qB}\right)^{1/2} v\sqrt{2}$$

$$\frac{R_1}{R_2} = \frac{1}{\sqrt{2}}$$

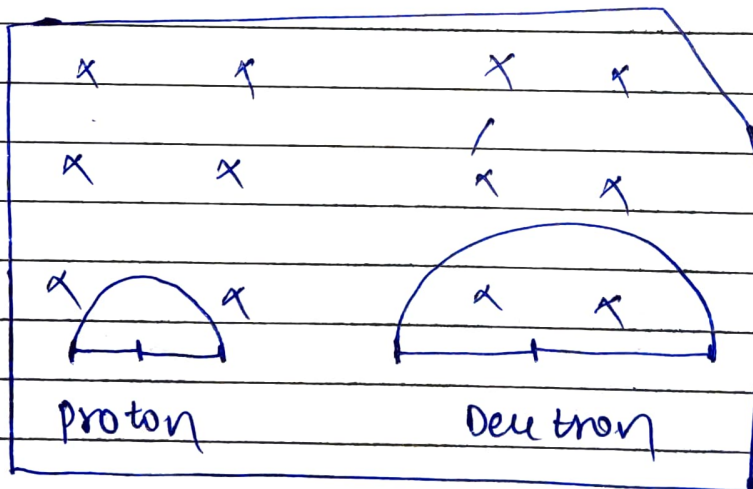
$$\frac{1}{2} mv^2 = qv$$

$$\frac{1}{2} mv^2 = q(2v)$$

$$\frac{v_1}{\sqrt{2}} = \frac{1}{\sqrt{2}}$$

$$v_2 = v\sqrt{2}$$

2)



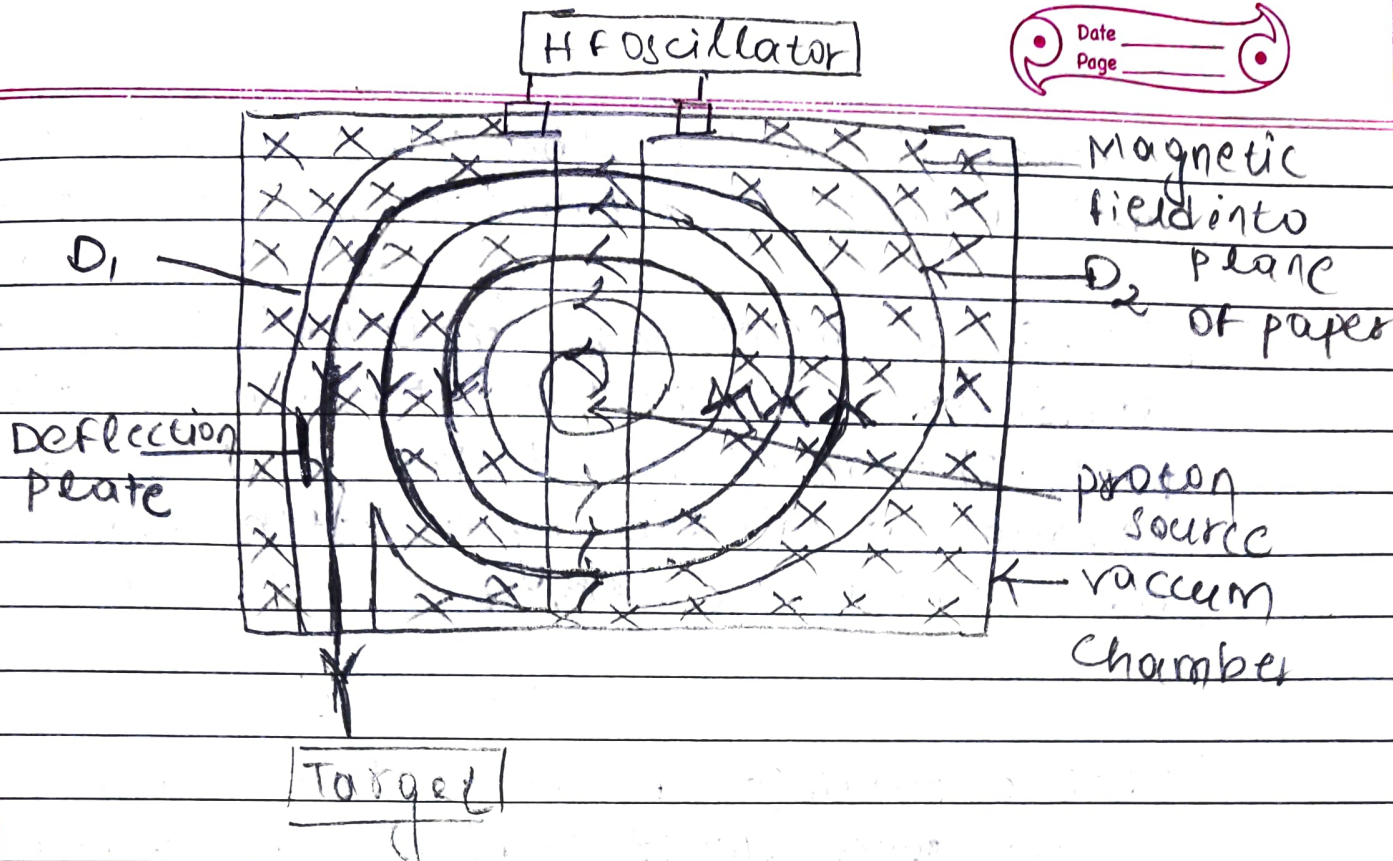
Mass of deuteron = $2m$ (1 proton + 1 neutron)
Mass of proton = m (1 proton)

$$R(\text{proton}) = \frac{mv}{qB}$$

$$R(\text{deutron}) = \frac{2m \times v}{qB}$$

$$\text{Ratio } \frac{\text{proton}}{\text{deutron}} = \frac{1}{2}$$

3)



→ working principle of cyclotron.

i) Suppose a positive ion, say a proton, enters gap between the two dees and find dee D_1 to be negative. It gets accelerated toward ~~the~~ dee D_1 . As it enters the dee D_1 , it ~~do~~ does experience any electric field due to shielding effect of the metallic dee.

ii) The perpendicular magnetic field throws it into a circular path. At the instant the proton comes out of dee D_1 , it finds dee D_1 ~~positive~~ positive and dee D_2 negative. It gets accelerated toward dee D_2 .

iii) Thus if the frequency of the applied voltage is kept exactly the same as the frequency of revolution of the proton, then every time the proton reaches the gap between the two dees, the electric field

is reversed and proton receives a push and finally it acquires very high energy.

iv) This is called the cyclotron's resonance condition - The proton follows a spiral path - The accelerated proton is ejected through a window by a deflecting voltage and hits the target.

→ Let a particle of charge q and mass m enter ~~to enter~~ a region of magnetic field \vec{B} with a velocity \vec{v} , normal to the field \vec{B} . The particle follows a circular path, the necessary centripetal force being provided by the magnetic field.

∴ Magnetic force on charge q = centripetal force on charge q
 or $qvB \sin 90^\circ = \frac{mv^2}{r}$ or $r = \frac{mv}{qB}$

period of revolution of the charge particle is given by

$$T = \frac{2\pi r}{v} = \frac{2\pi}{v} \cdot \frac{mv}{qB} = \frac{2\pi m}{qB}$$

The frequency of revolution of the particle will be $f_c = \frac{1}{T} = \frac{qB}{2\pi m}$

Hence, this frequency is independent of both the velocity of the particle and the radius of the orbit and is called cyclotron frequency.

4) i) As cyclotron frequency depends on both charge and mass of ion to be accelerated it is obvious that an α particle and a proton cannot be accelerated ~~at~~ at the same cyclotron frequency.

ii) As,
$$r = \frac{mv}{qB}$$

Hence, at the slit of ~~the~~ the dees of a cyclotron
$$v = \frac{qBR}{m}$$

As $\left(\frac{q}{m}\right)_{\text{proton}} > \left(\frac{q}{m}\right)_{\alpha\text{-particle}}$, the proton

will have higher velocity ~~than~~ than alpha particle.

5) A particle will trace circular path in clockwise direction as its deviation will be in the ~~the~~ direction $(\vec{v} \times \vec{B})$ i.e. perpendicular to the velocity of particle. Neutron will pass without any deviation as magnetic field does not exert neutral particle. Electron will trace circular path in anticlockwise direction as its deviation will be in the direction opposite to $(\vec{v} \times \vec{B})$ with a smaller radius due to large charge/mass ratio as $r = mv/qB$