

Magnetism

3)  $\theta = 30^\circ$   
 $B = 0.25 \text{ T}$   
 $\tau = 4.5 \times 10^{-2} \text{ J}$   
 $A \tau = m B \sin \theta$

$$m = \frac{\tau}{B \sin \theta} = \frac{4.5 \times 10^{-2}}{0.25 \times \sin 30} = 0.36 \text{ J T}^{-1}$$

4)  $m = 0.32 \text{ J T}^{-1}$   
 $B = 0.15 \text{ T}$

(i) The bar will be in stable equilibrium when its magnetic moment  $\vec{m}$  is parallel to  $\vec{B}$ . Its potential energy is then minimum and is given by

$$U_{\min} = -mB \cos 0^\circ = -0.32 \times 0.15 \times 1$$

$$= -4.8 \times 10^{-2} \text{ J}$$

(ii) The bar will be in unstable equilibrium when its magnetic moment  $\vec{m}$  is antiparallel to  $\vec{B}$ . Its potential ~~moment~~ energy is then maximum and is given by

$$U_{\max} = -mB \cos 180^\circ = -0.32 \times 0.15 \times (-1)$$

$$= +4.8 \times 10^{-2} \text{ J}$$

5)  $N = 800$   
 $A = 2.5 \times 10^{-4} \text{ m}^2$   
 $I = 3 \text{ A}$   
 $m = NIA = 800 \times 3 \times 2.5 \times 10^{-4}$   
 $= 0.60 \text{ J T}^{-1}$

The magnetic field of a solenoid has the same pattern as that of a bar magnet. It acts along

the axis of the solenoid. Its direction is determined by the sense of flow of current.

8)

$$N = 2000$$

$$A = 1.6 \times 10^{-4} \text{ m}^2$$

$$I = 4.0 \text{ A}$$

(a) Magnetic moment of solenoid of turn  $N$ , area of cross section  $A$  and carrying current  $I$  is

$$m = NIA$$

$$= 2000 \times 4.0 \times 1.6 \times 10^{-4} \text{ Am}^2$$

$$= 1.28 \text{ Am}^2$$

The magnetic moment act along the axis of the solenoid in a direction related to the sense of current via the right hand ~~screw~~ screw rule.

(b) Net force experienced by the magnetic dipole in the uniform magnetic field = 0

The magnitude of the torque  $\tau$  exerted by the magnetic field  $\vec{B}$  on the solenoid is given by

$$\tau = mB \sin \theta = 1.28 \times 7.5 \times 10^{-2} \times \sin 30^\circ$$

$$= 0.048 \text{ Nm}$$

This torque tend to align the axis of the solenoid along the field  $\vec{B}$ .

9)

$$N = 16$$

$$r = 10 \text{ cm} = 0.10 \text{ m}$$

$$I = 0.75 \text{ A}$$

$$B = 5.0 \times 10^{-2} \text{ T}$$

$$v = 2.0 \text{ s}^{-1}$$

Magnetic moment of the coil is

$$M = NIA = Nl \cdot \pi r^2$$

Frequency of oscillation,  $\nu = \frac{1}{2\pi} \sqrt{\frac{MB}{I}}$

Moment of inertia is

$$I = \frac{MB}{4\pi^2 \nu^2} = \frac{Nl \pi r^2 \cdot B}{4\pi^2 \nu^2}$$

$$= \frac{16 \times 0.75 \times (0.1)^2 \times 5 \times 10^{-2}}{4 \times 3.14 \times 4}$$

$$= 1.2 \times 10^{-4} \text{ kg m}^2$$

11)  $B_H = 0.16 \text{ G}$   
 $\delta = 60^\circ$

$$B = \frac{B_H}{\cos \delta} = \frac{0.16}{\cos 60^\circ} = \frac{0.16}{0.5} = 0.32 \text{ G}$$

Thus the earth's magnetic field has a magnitude of 0.32 G and lies in a vertical plane  $12^\circ$  west of the geographic meridian making an angle of  $60^\circ$  with the horizontal direction.

13)  $B_{axis} = \frac{\mu_0}{4\pi} \cdot \frac{2m}{r^3} = B_H$

Magnetic field of the magnet on its normal bisector at the same distance will be

$$B_{eqva} = \frac{\mu_0}{4\pi} \cdot \frac{m}{r^3} = \frac{B_H}{2} = \frac{0.36}{2} = 0.18 \text{ G}$$

∴ Total magnetic field at the required point on the normal bisector is

$$B_{\text{cable}} + B_H = 0.18 + 0.36 \\ = 0.54 \text{ G}$$

18) Suppose the neutral point lies at a distance  $r$  from the cable. Then at the neutral point.

$$\frac{\mu_0 I}{2\pi r} = B_H$$

$$\text{or } r = \frac{\mu_0 I}{2\pi B_H} = \frac{4\pi \times 10^{-7} \times 2.5}{2\pi \times 0.33 \times 10^{-4}}$$

$$= 1.5 \times 10^{-2} \text{ m}$$

$$= 1.5 \text{ cm}$$

As the direction of the magnetic field of the cable is opposite to that of  $\vec{B}_H$  at point above the cable, so the line of neutral point lies parallel to and above the cable at a distance of 1.5 cm from it.