

Chapter : 4 Moving charges and Magnetism

1) $N = 100$
 $r = 8 \text{ cm} = 0.08 \text{ m}$
 $I = 0.40 \text{ A}$

At Centre:
$$\frac{\mu_0 I N}{2\pi r} = \frac{4\pi \times 10^{-7} \times 0.4 \times 100}{2 \times 0.08}$$

$$= 3.14 \times 10^{-4} \text{ T}$$

2) $I = 35 \text{ A}$
 $r = 20 \text{ cm} = 0.2 \text{ m}$

$$B = \frac{\mu_0 I}{2r} = \frac{4\pi \times 10^{-7} \times 35}{2 \times 0.2} = 3.5 \times 10^{-5} \text{ T}$$

6) $l = 3 \text{ cm} = 0.03 \text{ m}$
 $I = 10 \text{ A}$
 $B = 0.27 \text{ T}$
 $\theta = 90^\circ$

$F = BIl \sin \theta$
 $= 0.27 \times 10 \times 0.03 \times \sin 90$
 $= 8.1 \times 10^{-2} \text{ N}$

7) $I_A = 8 \text{ A}$
 $I_B = 5 \text{ A}$
 $r = 4 \text{ cm} = 0.04 \text{ m}$
 $l_A = 10 \text{ cm} = 0.1 \text{ m}$

$$B = \frac{\mu_0 2 I_A I_B l_A}{4\pi r} = \frac{4\pi \times 10^{-7} \times 8 \times 5 \times 0.1}{2\pi \times 0.04}$$

$$= 2 \times 10^{-5} \text{ N}$$

8) $l = 80 \text{ cm} = 0.8 \text{ m}$
 $N = 5 \times 400 = 2000$
 $D = 1.8 \text{ cm} = 0.018 \text{ m}$
 $I = 8 \text{ A}$

$$B = \frac{\mu_0 N I}{l} = \frac{4\pi \times 10^{-7} \times 2000 \times 8}{0.8}$$

$$= 8\pi \times 10^{-3} = 2.5 \times 10^{-2} \text{ T}$$

11) $B = 6.5 \text{ G} = 6.5 \times 10^{-4} \text{ T}$

$v = 4.8 \times 10^6$

$\theta = 90^\circ$

$m_e = 9.1 \times 10^{-31} \text{ kg}$

$e = 1.6 \times 10^{-19} \text{ C}$

Magnetic force is exerted on the electron is
 $F = e v B \sin \theta$

Centrifugal force $F_c = \frac{m v^2}{r}$

$F_c = F$

$\Rightarrow \frac{m v^2}{r} = e v B \sin \theta \Rightarrow r = \frac{m v}{e B \sin \theta} = \frac{9.1 \times 10^{-31} \times 4.8 \times 10^6}{6.5 \times 10^{-4} \times 1.6 \times 10^{-19} \times \sin 90^\circ}$

$= 4.2 \times 10^{-2} \text{ m} = \underline{4.2 \text{ cm}}$

12) $B = 4.5 \times 10^{-4} \text{ T}$

$v = 4.8 \times 10^6$

$\theta = 90^\circ$

$m_e = 9.1 \times 10^{-31}$

$e = 1.6 \times 10^{-19}$

$r = 4.2 \text{ cm} = 0.042 \text{ m}$

Let frequency of the electron be f

Angular frequency $= \omega = 2\pi f$

Velocity is related to

angular frequency as $v = r\omega$

$= e v B = \frac{m v^2}{r} \Rightarrow e r = \frac{m (r\omega)}{r} = \frac{m \omega}{e}$

$\Rightarrow f = \frac{e B r}{2\pi m}$

\therefore Frequency is independent of the speed of electron.

$f = \frac{e B r}{2\pi m} \Rightarrow \frac{6.5 \times 10^{-4} \times 1.6 \times 10^{-19}}{2 \times 3.14 \times 9.1 \times 10^{-31}} \approx 1.8 \text{ MHz}$

13) a) $N = 30$, $r = 8 \text{ cm} = 0.08 \text{ m}$, $I = 6 \text{ A}$, $B = \mu_0 I N$, $\theta = 60^\circ$
 $A = \pi r^2 = 3.14 \times (0.08)^2 = 0.0201$

$$\tau = n I B A \sin \theta$$

$$= 30 \times 6 \times 1 \times 0.0201 \times \sin 60^\circ$$

$$= 3.123 \text{ N m}$$

b) As τ doesn't depend on shape so it will not change.

Additional Exercise:

14) $r_1 = 16 \text{ cm} = 0.16 \text{ m}$
 $n_1 = 20$, $I_1 = 16 \text{ A}$, $r_2 = 0.1 \text{ m}$, $I_2 = 18 \text{ A}$.

$$B_{\text{centre}} = \frac{\mu_0 I_1 N_1}{2r_1} = \frac{4\pi \times 10^{-7} \times 20 \times 16}{2 \times 0.16} = 4\pi \times 10^{-4} \text{ T (towards east)}$$

$$B_2 = \frac{\mu_0 N_2 I_2}{2r_2} = \frac{4\pi \times 10^{-7} \times 25 \times 18}{2 \times 0.10} = 9\pi \times 10^{-4} \text{ T (towards west)}$$

$$B_{\text{net}} = B_2 - B_1$$

$$= 9\pi \times 10^{-4} - 4\pi \times 10^{-4}$$

$$= 5\pi \times 10^{-4} \text{ T (towards west)}$$

15) $B = 100 \text{ G} = 100 \times 10^{-4} \text{ T}$, $N = 1000 \text{ turns/m}$, $I = 15 \text{ A}$

$$B = \frac{\mu_0 N I}{l} \Rightarrow \frac{N I}{l} = \frac{B}{\mu_0} \Rightarrow \frac{N I}{l} = \frac{100 \times 10^{-4}}{4\pi \times 10^{-7}} \Rightarrow \frac{N I}{l} = 7961$$

Let the current = 10 A & $l = 0.6 \text{ m}$

So we get = $\frac{N \times 10}{0.6} = 7961 \Rightarrow N = \frac{7961 \times 0.6}{10} \Rightarrow N = 477.6$

17) $r_1 = 25 \text{ cm} = 0.25 \text{ m}$, $r_2 = 26 \text{ cm} = 0.26 \text{ m}$, $N_1 = 3500$, $I = 11 \text{ A}$

a) Outside the toroid, magnetic field is zero.

b) $B = \frac{\mu_0 N I}{l} \Rightarrow l = 2\pi (r_1 + r_2) = \pi \times 0.51$

$$B = \frac{\mu_0 N I}{l} = \frac{4\pi \times 10^{-7} \times 3500 \times 11}{\pi \times 0.51} = 3.02 \times 10^{-2} \text{ T}$$

18a) Initial velocity is either parallel or anti parallel to the magnetic field. There is no magnetic force acting on the particle when it is parallel or anti-parallel and it moves undeflected.

b) Yes, as magnetic force can change the direction of velocity but not its magnitude.

c) Magnetic field should be in a vertically downward direction.

19) $B = 0.157$, $V = 2\text{KV}$. gain in KE of an $e^- \Rightarrow E = \frac{1}{2}mv^2$
 $\Rightarrow eV = \frac{1}{2}mv^2$

$$\Rightarrow u = \sqrt{2eV/m}$$

$$= \sqrt{2 \times 1.6 \times 10^{-19} \times 2 \times 10^3 / 9.1 \times 10^{-31}}$$

$$= 2.65 \times 10^7 \text{ m/s}$$

a) $F_1 = F_2$, $F_1 = eVB$, $F_2 = mv^2/2 \Rightarrow eVB = mv^2/2 \Rightarrow r = mv/eB$
 $\Rightarrow r = mv/eB \Rightarrow r = 9.1 \times 10^{-31} \times 2.65 \times 10^7 / 1.6 \times 10^{-19} \times 0.15$
 $\Rightarrow 10^{-3} \text{ m} = 1 \text{ mm}$

b) $r = mv \sin \theta / Be$, $r = 9.1 \times 10^{-31} \times 2.65 \times 10^7 \times \sin 30^\circ / 0.15 \times 1.6 \times 10^{-19}$
 $= 50.2 \times 10^{-5} \text{ m}$, $r = 0.5 \text{ mm}$.

20) $B = 0.75 \text{ T}$, $V = 15 \text{ KV} = 15 \times 10^3 \text{ V}$, $E = 9.0 \times 10^{-5} \text{ Vm}^{-1}$

$$K = \frac{1}{2}mv^2, \Rightarrow eV = \frac{1}{2}mv^2$$

$$\Rightarrow e/m = v^2/2V$$

\therefore The particular particles are not deflected by \vec{E} & \vec{B}

$$\Rightarrow eE = evB$$

$$\Rightarrow v = E/B$$

$$\frac{1}{2}m \left(\frac{E}{B}\right)^2 = eV \Rightarrow e/m = \frac{E^2}{2VB^2} \Rightarrow \frac{(9.0 \times 10^5)^2}{2 \times 15000 \times (0.75)^2}$$

$$\Rightarrow 4.8 \times 10^7 \text{ C/kg}$$

\therefore The answer is not unique as only ratio of charge to mass is determined the beam contains electrons.

24) $B = 3000 \text{ G} = 0.3 \text{ T}$, $A = 10 \times 5 = 50 \times 10^{-4} \text{ m}^2$, $I = 12 \text{ A}$.

a) $\vec{\tau} = I \vec{A} \times \vec{B}$

$\vec{A} = 50 \times 10^{-4} \hat{i}$ (y-z plane)

$\vec{B} = 0.3 \hat{k}$ (along z axis)

$\vec{\tau} = 12 \times (50 \times 10^{-4}) \hat{i} \times 0.3 \hat{k}$

$= -1.8 \times 10^{-2} \hat{j} \text{ Nm}$

(towards -ve y-direction)

b) Pt is same as a) in the -ve y direction $I_{\text{net}} = 0$

c) $\vec{A} = -50 \times 10^{-4} \hat{j}$ (x-z plane)

$\vec{B} = 0.3 \hat{k}$

$\vec{\tau} = 12 \times (-50 \times 10^{-4}) \hat{j} \times 0.3 \hat{k}$

$= -1.8 \times 10^{-2} \hat{j} \text{ Nm}$

\therefore Net force is zero.

d) $\vec{\tau} = 12 \times 50 \times 10^{-4} \times 0.3$

$= 1.8 \times 10^{-2} \text{ Nm}$

\therefore Net force is zero.

e) $\vec{A} = 50 \times 10^{-4} \hat{k}$

$\vec{B} = 0.3 \hat{k}$

$\vec{\tau} = 12 \times (50 \times 10^{-4}) \hat{k} \times 0.3 \hat{k}$

$\therefore F_{\text{net}} = 0$

f) $\vec{A} = -50 \times 10^{-4} \hat{k}$

$\vec{B} = 0.3 \hat{k}$

$\vec{\tau} = 12 (-50 \times 10^{-4}) \hat{k} \times 0.3 \hat{k}$

$\therefore F = 0$

\therefore Case (e) & (f)

27) $G = 12 \Omega$

$I = 3 \text{ mA}$

$R = \left(\frac{V}{I_g}\right) - G \Rightarrow \left(\frac{18}{3 \times 10^{-3}}\right) - 12 \Rightarrow 6000 - 12 = 5988 \Omega$

28) $G = 15 \Omega$, $I_g = 4 \text{ mA} = 4 \times 10^{-3} \text{ A}$.

Ammeter range = 0 to 6A

$$S = I_g G / I - I_g$$
$$= \frac{4 \times 10^{-3} \times 15}{6 - 0.004}$$
$$= 10 \times 10^{-3} \text{ A}$$

$$S = 10 \text{ mA}$$

\therefore 10 mA resistor must be connected in parallel

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