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Holiday Homework

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- 1) Reciprocal of zero is (d) None of the above
- 2) The multiplicative inverse of 10^{-100} is (a) 10^{100}
- 3) Zero is (a) identity for addition of rational numbers
- 4) One is (b) the identity of multiplication of rational numbers
- 5) Find the least number by which 1323 must be multiplied so that the product is a perfect cube
(a) 7
- 6) 2.7 is what percent of 18?
(b) 15%
- 7) If A & B are two sets such that $n(A) = 15$, $n(B) = 21$ & $n(A \cup B) = 36$ then $n(A \cap B)$ equal to ~~a~~ b) 0
- 8) If $5A \times A = 399$ then the value of A is
(b) 7
- 9) If 30 men can do a work in 24 days. How many men will do the same work in 12 days?
(c) 15
- 10) $a+b = b+a$ is called
(a) commutative law of addition

11) Insert three rational numbers between $\frac{2}{3}$ and $\frac{3}{4}$

$$\frac{2}{3} \text{ and } \frac{3}{4}$$

$$= \frac{2}{3}, \frac{2+3}{3+4}, \frac{3}{4}$$

$$= \frac{2}{3}, \frac{5}{7}, \frac{3}{4}$$

$$= \frac{2}{3}, \frac{2+5}{3+7}, \frac{5}{7}, \frac{5+3}{7+4}, \frac{3}{4}$$

$$= \frac{2}{3} \left(\frac{7}{10}, \frac{5}{7}, \frac{8}{11} \right) \frac{3}{4}$$

12) Simplify: $(12)^{-2} \times 4^3$

$$\left(\frac{1}{12}\right)^2 \times 4^3$$

$$= \frac{1}{144} \times 64$$

13) Question in review.

14) Write the following rational numbers in descending order: $\frac{2}{7}, -\frac{9}{8}, -\frac{3}{2}, 0, \frac{2}{5}$

$$\frac{2}{7}, -\frac{9}{8}, -\frac{3}{2}, 0, \frac{2}{5}$$

$$\text{LCM of } 7, 8, 2, 5 = 280$$

$$\frac{8}{7} = \frac{8 \times 40}{7 \times 40} = \frac{320}{280}$$

$$\frac{-9}{8} = \frac{-9 \times 35}{8 \times 35} = \frac{-315}{280}$$

$$\frac{-3}{2} = \frac{-3 \times 140}{2 \times 140} = \frac{-420}{280}$$

0

$$\frac{2}{5} = \frac{2 \times 56}{5 \times 56} = \frac{112}{280}$$

$$0, \frac{112}{280}, \frac{320}{280}, \frac{112}{280}, 0, \frac{-315}{280}, \frac{-420}{280}$$

$$= \frac{8}{7}, \frac{2}{5}, 0, \frac{-9}{8}, \frac{-3}{2}$$

15) Find the sum of additive inverse and multiplicative inverse of 7.

$$\text{additive inverse} = -7$$

$$\text{multiplicative inverse} = \frac{1}{7}$$

$$\text{Sum} = \frac{-7}{1} + \frac{1}{7}$$

$$= \frac{-49+1}{7}$$

$$= \frac{-48}{7}$$

16) The perimeter of a triangle is $8y^2 - 9y + 4$ and its two sides are $3y^2 - 5y$ and $4y^2 + 12$. Find its third side.

$$\begin{aligned}\text{Sum of two sides} &= 3y^2 - 5y + 4y^2 + 12 \\ &= 3y^2 + 4y^2 - 5y + 12 \\ &= 7y^2 - 5y + 12\end{aligned}$$

$$\begin{aligned}\text{The perimeter of triangle} &= 8y^2 - 9y + 4 \\ \text{Third side} &= (8y^2 - 9y + 4) - (7y^2 - 5y + 12) \\ &= 8y^2 - 9y + 4 - 7y^2 + 5y - 12 \\ &= 8y^2 - 7y^2 - 9y + 5y + 4 - 12 \\ &= y^2 - 4y - 8\end{aligned}$$

17) Then work done by A in one day = $\frac{1}{20}$
work done by B in one day = $\frac{1}{15}$

Then work done by A & B in one day

$$= \frac{1}{20} + \frac{1}{15} = \frac{7}{60}$$

$$\text{A \& B done in 6 days} = \frac{7}{60} \times 6 = \frac{7}{10}$$

$$\text{work left} = 1 - \frac{7}{10} = \frac{3}{10}$$

$$\text{Then B can do } \frac{3}{10} \text{ work} = \frac{3}{10} \times \frac{15}{1} = \frac{9}{2} \text{ days.}$$

18) At what rate percent annum will ₹630 produce an interest of ₹126 in 4 years.

$$P = ₹630$$

$$S.I. = ₹126$$

$$T = 4 \text{ years}$$

$$R = \frac{100 \times S.I.}{P \times T}$$

$$= \frac{100 \times 126}{630 \times 4}$$

$$= 5\%$$

ii) Let $P = ₹100$

$$\text{Amount} = 2 \times 100 = ₹200$$

$$\text{Interest} = A - P$$

$$= 200 - 100 = 100$$

$$T = 6\frac{1}{4} \text{ years} = \frac{25}{4} \text{ yrs}$$

$$R = \frac{100 \times I}{P \times T} = \frac{100 \times 100}{100 \times \frac{25}{4}} = \frac{100 \times 100}{100} \times \frac{4}{25} = 16\%$$

19) Calculate the difference between the compound interest and the simple interest on ₹7500 in two years and at 8% per annum.

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$$\text{Principal} = ₹ 7500$$

$$R = 8\%$$

$$T = 2 \text{ yrs}$$

$$\begin{aligned} \text{Simple Interest} &= \frac{P \times R \times T}{100} = \frac{7500 \times 8 \times 2}{100} \\ &= ₹ 1200 \end{aligned}$$

$$\begin{aligned} \text{Interest of the first year} &= \frac{7500 \times 8 \times 1}{100} \\ &= ₹ 600 \end{aligned}$$

$$\begin{aligned} \text{Amount} &= P + S.I. \\ &= 7500 + 600 \\ &= 8100 \end{aligned}$$

$$P \text{ of second year} = ₹ 8100$$

$$\begin{aligned} \text{Interest upon the second year} &= \frac{8100 \times 8 \times 1}{100} \\ &= ₹ 648 \end{aligned}$$

$$\begin{aligned} \text{Total C.I.} &= 600 + 648 \\ &= ₹ 1248 \end{aligned}$$

$$\text{Difference between C.I. and S.I.}$$

$$\begin{aligned} &= 1248 - 1200 \\ &= ₹ 48 \end{aligned}$$

20) If the price of sugar is increased by 25% today; By what percent should it be decreased tomorrow to bring the price back to the original?

Let the price of the sugar be 100
Then its price tomorrow will be 125

So, to bring back the price to normal it should be decreased $\frac{25-100}{125} \times 100 = 20\%$

22) John sold an article to Peter at 20% profit and Peter sold it to Mohan at 5% loss. If Mohan paid ₹ 912 for the article, find how much did John pay for it?

Mohan paid for the article = ₹ 912
∴ Peter sold the article to Mohan

For Peter :-

$$SP = ₹ 912$$

$$\text{Loss} = 5\%$$

$$CP = \frac{100}{(100 - L\%)} \times S.P$$

$$= \frac{100}{(100 - 5)} \times 912$$

$$= \frac{100 \times 912}{95}$$

$$= 20 \times 48$$

$$= 960$$

John sold the same article to Peter

For John :-

$$SP = 960$$

$$\text{Profit} = 20\%$$

$$CP = \frac{100}{(100 + P)} \times S.P$$

$$= \frac{100}{(100 + 20)} \times 960 = \frac{100}{120} \times 960$$

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Hence John paid for this article is ₹2800.

23) Prem paid for the scooter = ₹14,490
Rahim sold the same scooter to Prem

(i) For Rahim:-

$$SP = ₹14,490$$

$$P = 5\%$$

$$CP = \frac{100}{(100+P\%)} \times SP$$

$$= \frac{100}{(100+5\%)} \times 14,490$$

$$= \frac{100 \times 14,490}{105}$$

$$= ₹13,800$$

Rajesh sold the same scooter to Rahim

For Rajesh:-

$$SP = ₹13,800$$

$$P = 8\%$$

$$CP = \frac{100}{(100-P\%)} \times SP$$

$$= \frac{100}{(100-8\%)} \times 13,800$$

$$= \frac{100 \times 13,800}{92}$$

$$= ₹150$$

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Hence Rajesh paid for the scooters ₹150

24) Insert six rational numbers between $\frac{5}{6}$ and $\frac{8}{9}$

$$\frac{5}{6} \text{ and } \frac{8}{9}$$

$$= \frac{5}{6}, \frac{5+8}{6+9}, \frac{8}{9}$$

$$= \frac{5}{6}, \frac{13}{15}, \frac{8}{9}$$

$$= \frac{5}{6}, \frac{5+13}{6+15}, \frac{13}{15}, \frac{13+8}{15+9}, \frac{8}{9}$$

$$\frac{5}{6}, \frac{18}{21}, \frac{13}{15}, \frac{21}{24}, \frac{8}{9}$$

$$\frac{5}{6}, \frac{5+18}{6+21}, \frac{18}{21}, \frac{18+13}{21+15}, \frac{13}{15}, \frac{13+21}{15+24}, \frac{21}{24}, \frac{21+8}{24+9}, \frac{8}{9}$$

$$= \frac{5}{6}, \frac{23}{27}, \frac{18}{21}, \frac{31}{36}, \frac{13}{15}, \frac{34}{39}, \frac{21}{24}, \frac{29}{33}, \frac{8}{9}$$

25) If $\sqrt{784} = 28$ find the value of :-

i) $\sqrt{7.84} + \sqrt{78400}$

ii) $\sqrt{0.0784} + \sqrt{0.000784}$

ans) i) $28 + 280$
 $= 282.8$

ii) $0.28 + 0.028$
 $= 0.308$

26) iii) $B = \{y : 2y + 1 < 3 \text{ and } y \in \mathbb{N}\}$

$$= 2y + 1 = 3$$

$$= 2y = 3 - 1$$

$$= 2y = 2$$

$$= y = \frac{2}{2}$$

$$= y = 1$$

Yes, this set is called the singleton set.

27) If John sells his bicycle for ₹ 637, he will suffer a loss of 9%. For how much should it be sold, if he desires a profit of 5%?

$$\text{SP of the bicycle} = ₹ 637$$

$$\text{Loss} = 9\%$$

$$\text{CP} = \frac{100}{(100 - 9\%)} \times \text{SP}$$

$$= \frac{100}{100 - 9} \times 637$$

$$= \frac{100 \times 637}{91}$$

$$= 700$$

Desires a profit of 5%.

$$\text{CP} = 700$$

$$\text{SP} = \frac{100}{(100 + P\%)} \times \text{CP}$$

$$\frac{100}{100-5\%} \times 700$$

$$= \frac{100 \times 700}{95}$$

$$= \frac{100 \times 700}{95}$$

$$= 735$$

28) 3 men 6 boys
1 man = 2 boys

3 men or 6 boys can finish a work in 20 days

4 men and 12 boys = 4 + 6 men = 10m

3 men can finish a work in 20 days

10 men can finish the work in $\frac{20 \times 3}{10}$

= 6 days.

29) 5 persons maintained for 20 days with ₹ 2480

$$\text{Then 1 person} = \frac{2480}{20 \times 5} = \frac{2480}{100}$$

So the maintenance of 8 persons = 24.80
 $\times 8 = 198.40$
 day.

Qo the number of days ₹ 6944 can be maintained @ per person will be

$$\frac{6944}{198.40} = 35 \text{ days.}$$

$$\begin{aligned} 30) \quad x^2 - 9x - 10 &= 0 \\ x^2 - 10x + x - 10 &= 0 \\ x(x-10) + 1(x-10) &= 0 \\ (x-10)(x+1) &= 0 \end{aligned}$$

$$\begin{array}{l} x-10=0 \quad \text{or} \quad x+1=0 \\ x=10 \quad \quad \quad x=-1 \end{array}$$