

Q 11) an object is placed at a distance of 10 cm from a concave mirror of focal length 20cm draw the ray diagram for the formation of image calculate the image distance state two characteristics of image formed

ANS-- position of image and complete ray diagram.

given, focal length of concave mirror, $f = -20$ cm
distance of object from the mirror, $u = -10$ cm

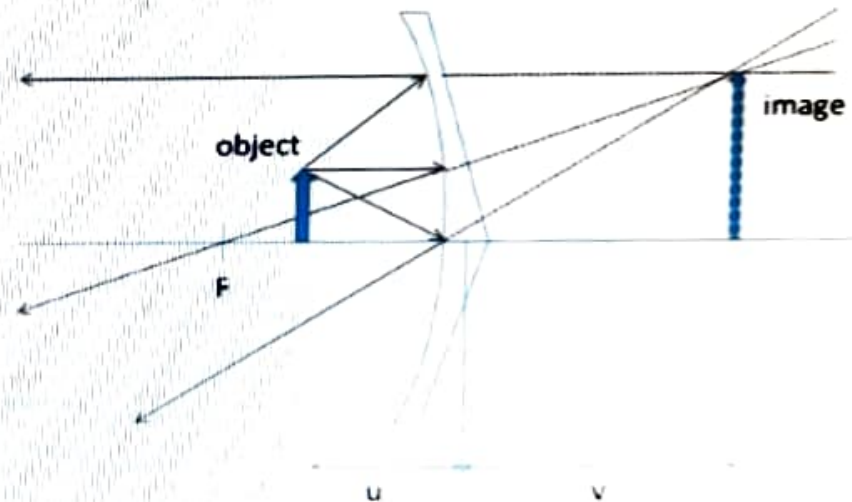
use formula, $1/v + 1/u = 1/f$

or, $1/v = 1/f - 1/u$

or, $1/v = 1/-20 - 1/-10$

or, $1/v = -1/20 + 1/10 = 1/20$

or, $v = +20$ cm



Q 12) If an object of 10 cm height is placed at a distance of 36 cm from a concave mirror of focal length 12 cm, find the position, nature and height of image.

Answer

Object distance $u = -36$ cm

Focal length of concave mirror $f = -12$ cm

Using mirror formula : $1/v + 1/u = 1/f$

Or $1/v + -1/36 = -1/12$

$\Rightarrow v = -18$ cm

Magnification

$h_o/h_i = -v/u$

Or $h_i/10 = -10 - /(-18)$

$\Rightarrow h_i = -18$ cm

Image formed is real and inverted

Q13) At what distance from a concave mirror focal length 10 cm should an object 2 cm long be placed in order to get an erect image 6 cm tall?

Ans-- Height of the object ' h_o ' = 2 cm Focal length of the mirror ' f ' = -10 cm Height of the image ' h_i ' = 6 cm We have to find the distance of the object from the mirror ' u '. Using the magnification formula, we get

$$m = \frac{h_i}{h_o} = -\frac{v}{u}$$

$$m = \frac{6}{2} = -\frac{v}{u}$$

$$m = 3 = -\frac{v}{u}$$

$$10 = \frac{1}{3u} - \frac{3}{3u} = -\frac{2}{3u}$$

$$u = -2 \times 10 / 3$$

$$u = -6.67 \text{ cm}$$

Thus, the distance of the object from the mirror ' u ' is -6.67 cm

Q 14) When an object is placed at a distance of 15 cm from a concave mirror, its image is formed at 10 cm in front of the mirror. Calculate the focal length of the mirror?

$$u = -15 \text{ cm}, v = -10 \text{ cm}$$

$$f = ?$$

We know that

$$\frac{1}{v} + \frac{1}{u} = \frac{1}{f}$$

$$\Rightarrow \frac{1}{(-10)} + \frac{1}{(-15)} = \frac{1}{f}$$

$$\Rightarrow \frac{1}{f} = -\frac{1}{10} - \frac{1}{15} = \frac{-3 - 2}{30} = -\frac{5}{30} = -\frac{1}{6}$$

$$\therefore f = -6 \text{ cm}$$

Therefore, the focal length of the concave mirror is 6

Q-16) an object 3cm high is placed at a distance of 8cm from a concave mirror which produces a virtual image of 4.5cm

i) Focal length of mirror

ii) What is the position of image

iii) Draw a ray diagram to show the formation of image

height of object = 3cm = H object

the object distance = - 8cm (object distance is always negative)

if the concave mirror produces an image of 4.5cm that means that

→ height of image = 4.5cm = H image

magnification = $m = h_i/h_o = -v/u$

$$= 4.5/3 = -(v)/-8\text{cm}$$

$$= 4.5 \times 8 / 3 = v$$

$$= 36/3 = v$$

$$= v = +12\text{cm}$$

this is the case where the object is placed between focus and pole of concave mirror. the image formed here is behind the mirror and is enlarged....

Height of the object (h) = 3 cm

Distance of object from concave mirror (u) = -8 cm

Height of the virtual image formed (h') = 4.5

Let's find 'v' first =

$$-v/u = h'/h$$

$$v = -u \times h'/h$$

$$v = -(-8) \times 4.5 / 3$$

$$v = 12 \text{ cm (i) Focal length of mirror = ?}$$

$$1/f = 1/v + 1/u$$

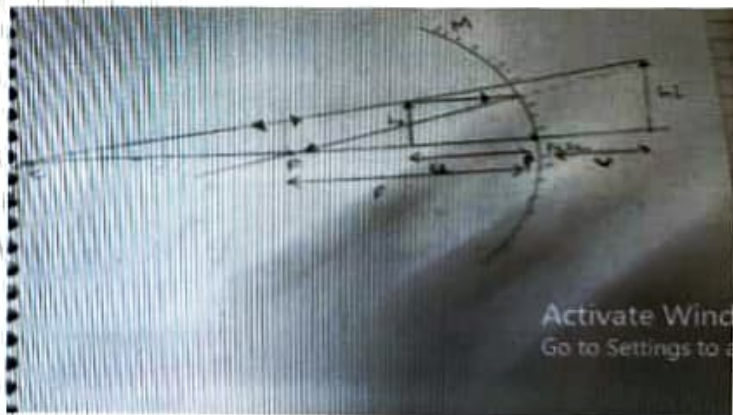
$$1/f = 1/12 + 1/-8$$

$$1/f = -1/24$$

$$1 \times 24 = -f$$

$$24 = -f$$

$$f = -24 \text{ cm}$$



Q 17) An object of size 7.0 cm is placed at 27 cm in front of a concave mirror. At what distance from the mirror should a screen be placed, so that a sharp focussed image can be obtained? Find the size and the nature of the image.

ANS--Size of the object $[o] = +7\text{cm}$

$$F = -18\text{cm}$$

$$U = -27\text{cm}$$

$$V = ?$$

$$1/f = 1/v + 1/u$$

$$1/-18\text{cm} = 1/v - 1/27$$

$$1/v = -1/54 \quad v = -54\text{cm}$$

Since V is -ve screen should be placed at 54cm in front of the mirror.

Size of the image : $m = I/O = -v/u \quad I/7 = -[54/27] \quad I = -14\text{cm}$

Nature of the image : image is real , inverted and magnified.

18) An object 3 cm high is placed at a distance of 10 cm in front of a converging mirror of focal length 20 cm. Find the position, nature and size of the image formed.

Answer

Given: $h_1=3\text{cm}$, $u=-10\text{cm}$, $f=-20\text{cm}$

We know that

$$1/v + 1/u = 1/f$$

$$\Rightarrow 1/v = 1/f - 1/u$$

$$= \frac{1}{-20} - \frac{1}{-10}$$

$$= -\frac{1}{20} + \frac{1}{10} = \frac{-1 + 2}{20} = \frac{1}{20}$$

$$\therefore v = 20\text{cm}$$

The image is formed at a distance of 20cm behind the mirror,

And

$$m = -\frac{v}{u} = \frac{h_2}{h_1}$$

$$\Rightarrow \frac{-20}{-10} = \frac{h_2}{3}$$

$$\Rightarrow h_2 = 6\text{cm}$$

Image is 6 cm in size, virtual and erect.

19) A concave mirror has a focal length of 4 cm and an object 2 cm tall is placed 9 cm away from it. Find the nature, position and size of the image formed

• **ANS— $h_1 = 2\text{cm}$, $u = -9\text{cm}$, $f = -4\text{cm}$**

• **We know that**

$$\frac{1}{v} + \frac{1}{u} = \frac{1}{f}$$

$$\frac{1}{v} = \frac{1}{f} - \frac{1}{u} = \frac{1}{-4} - \frac{1}{-9}$$

$$= -\frac{1}{4} + \frac{1}{9} = \frac{-9 + 4}{36} = -\frac{5}{36}$$

$$\therefore v = -7.2\text{ cm}$$

• **The image is formed at a distance 7.2 cm in front of the mirror**

$$\text{• Again, } m = -\frac{v}{u} = -\frac{-7.2}{-9} = -0.8$$

$$\text{• } m = \frac{h_2}{h_1} = -0.8 = \frac{h_2}{2} \Rightarrow h_2 = -1.6\text{ cm}$$

• **So, image is 1.6 cm in size, real and inverted.**

Q-20) When an object is placed 20 cm from a concave mirror, a real image magnified three times is formed. Find: (a) the focal length of the mirror. (b) Where must the object be placed to give a virtual images three times the height of the object?

ANS-

Distance of the object ' u ' = -20 cm Magnification ' m ' = -3 (a) We have to find the focal length of the mirror. Using the magnification formula, we get $v = -60$ cm

$$1/f = 1/v + 1/u$$

$$1/f = 1/(-60) + 1/(-20)$$

$$1/f = -1/60 - 3/60 = -4/60$$

$$1/f = -1/15$$

$$f = -15 \text{ cm}$$

Thus, the focal length of the concave mirror is 15 cm. (b) Now, if the image is virtual and 3 times magnified, then we have to find the position of the object. Given, Focal length of the concave mirror

$$= -15 \text{ cm}$$

$$3 = -v/u \quad v = -3u$$

Therefore, the distance of the image ' v '

$$\text{is } -3u$$

Again, using the mirror formula, we get $1/f = 1/v + 1/u$

$$1/f = 1/(-3u) + 1/(-20)$$

$$1/f = -1/60 - 3/60 = -4/60$$

$$1/f = -1/15 \quad m = -v/u \quad 3 = -v/u$$

$$v = -3u$$

$$1/f = 1/v + 1/u$$

$$1/f = 1/(-3u) + 1/(-20) = -4/60$$

Q21) A dentist's mirror has a radius of curvature of 3 cm. How far must it be placed from a small dental cavity to give a virtual image of the cavity that is magnified five times?

ANS-The dentist's mirror is a concave mirror. Radius of curvature 'R' = -3 cm Therefore, the focal length of the mirror $f = \frac{R}{2} = \frac{-3}{2} = -1.5$ cm Given that magnification 'm' = 5 Therefore, using the magnification formula, we get $m = -\frac{v}{u}$

$$v = -5u$$

Now, using the mirror formula, we get

$$\frac{1}{f} = \frac{1}{v} + \frac{1}{u}$$

$$u = -1.2 \text{ cm}$$

The dentist should place the object at a distance of 1.2 cm from the mirror.

focal length of the mirror

Concept: Linear Magnification (M) Due to Spherical

$$\frac{1}{-1.5} = \frac{1}{-5u} + \frac{1}{u} \quad \frac{1}{-1.5} = \frac{1}{-5u} + \frac{1}{u} \quad \frac{1}{-1.5} = \frac{1}{-5u} + \frac{5}{5u} = \frac{4}{5u} \quad u = \frac{(-1.5) \times 4}{5} = -1.2 \text{ cm}$$

$$f = \frac{R}{2} = \frac{3}{2} = 1.5 \text{ cm}$$

Q-22) A large concave mirror has a radius of curvature of 1.5 m. A person stands 10 m in front of the mirror. Where is the person's image?

ANS--The radius of curvature of the mirror ' R ' = -1.5m Focal length of the mirror ,

$$f = 1 / R = 1 / 1.5 = 0.75\text{m}$$

Distance of the object ' u ' = -10 m We have to find the distance of the image ' v '. Using the mirror formula

$$1 / f = 1 / v + 1 / u$$

$$1 / 0.75 = 1 / v + 1 / -10$$

$$1 / v = 3 / 30 - 40 / 30$$

$$1 / v = -37 / 30$$

$$\text{or } v = (-30) / 37$$

$$\text{or } v = 0.81 \text{ m}$$

Thus, the person's image will be formed at a distance of 0.81 m from the mirror

23) An object of 5.0 cm size is placed at a distance of 20.0 cm from a converging mirror of focal length 15.0 cm. At what distance from the mirror should a screen be placed to get the sharp image? Also calculate the size of the image.

ANS-- Concave mirror is a converging mirror. Distance of the object from the mirror ' u ' = -20 cm Height of the object ' h_o ' = 5 cm Focal length of the mirror ' f ' = -15 cm We have to find the distance of the image ' v ' and the height of the image ' h_i '

Using the mirror formula, we get

$$1/f = 1/v + 1/u$$

$$1/-15 = 1/v + 1/-20 =$$

$$1/v - 1/20$$

$$1/v = 1/20 - 1/15$$

$$m = -v/u = h_i/h_o$$

$$\text{or } h_i/5 = -3 \text{ or cm}$$

Therefore, the height of the image will be

$$\text{or } 1/v = 3 - 4/60 = 1/60$$

$$\text{or } v = -60 \text{ m} = -v/u = h_i/h_o$$

$$h_i = -3 \times 5 = -15$$

26) How far should an object be placed from the pole of converging mirror of focal length 20 cm to form a real image of the size exactly $\frac{1}{4}$ th the size of the object?

Answer

For converging mirror we know that magnification $m = -v/u$ and real images formed by concave mirror are inverted so, $-\frac{1}{4} = v/-u \Rightarrow v = u/4$

Using these in the mirror formula :

$$v/1 + u/1 = f/1$$

$$-4/u + -1/u = -1/20$$

$$u/5 = 1/20$$

This gives $u = 5 \times 20 = 100 \text{ cm}$

24) A concave mirror produces 3 times enlarged virtual image of an object placed at 10 cm in front of mirror. Calculate the radius of curvature of mirror.

Ans-- $m = +3$

Object Distance = $u = -10\text{cm}$ (sign conventions)

$V = ?$

Formula to be used: $m = -V/u$

$V = -m \times u$

$= -3 \times -10$

$= 30\text{ cms}$

Now to find focal length, Let us use mirror formula:

$1/f = 1/v + 1/u$

$1/f = 1/30 - 1/10$

$= 1 - 3/30$

$= -2/30$

$= -1/15$

$f = -15\text{cms.}$

The object is placed between P and F and we get virtual, enlarged and erect image.

Radius of curvature = $2f$

$= 2 \times -15$

$= -30\text{cms.}$

25) a bright object 50mm stands on the axis of concave mirror of focal length 100mm and at a distance of 300mm from the concave mirror how big will be the image?

ans- Height of the object (h) = 50 mm

Focal length of the mirror (f) = -100 mm

Object distance (u) = -300 mm

$$1/v + 1/u = 1/f$$

$$1/v = 1/f - 1/u$$

$$1/v = 1/(-100) - 1/(-300)$$

$$1/v = -1/100 + 1/300$$

$$1/v = (-3 + 1)/300$$

$$1/v = -2/300$$

$$v = 300/-2$$

$$v = -150 \text{ mm}$$

Therefore, the image will be formed 150 mm away from the pole.

magnification, $m = h'/h = v/u$

$$= v/u$$

$$= -150/-300$$

$$= 1/2$$

$$m = 1/2$$

$$\text{height of image} = m \times \text{height of object}$$

Q 28) when an object placed (a) 20cm, (b) 4cm, in front of concave mirror of focal length 12cm. Find the nature and position of the image formed in each case.

ANS- a) $u = -20 \text{ cm}$, $f = -12 \text{ cm}$

$$1/v + 1/u = 1/f$$

$$1/v + 1/-20 = 1/-12$$

$$1/v = -1/12 + 1/20 = (-20 + 12)/240 = -8/240$$

$$v = -30 \text{ cm}$$

The image is formed at a distance of 30 cm in front of the mirror.

The image is real and inverted.

(b) $u = -4 \text{ cm}$, $f = -12 \text{ cm}$

$$1/v + 1/u = 1/f$$

$$1/v + 1/-4 = 1/-12$$

$$1/v = -1/12 + 1/4 = (-1 + 3)/12 = 2/12$$

$$v = 6 \text{ cm}$$

The image is formed at a distance of 6 cm behind the mirror.

The image is virtual and erect.

Q 27) When an object is placed at a distance of 50cm from a concave spherical mirror, the magnification produced is, $1/2$. Where should the object be placed to get a magnification of, $-1/5$?

ans - $m = -1/2$ (means the image is real)

$u = -50$ cm.

We know,

From magnification formula

$$m = -v/u$$

$$\Rightarrow -1/2 = -v / -50$$

$$\Rightarrow v = -50/2 \text{ cm}$$

$$\Rightarrow v = -25 \text{ cm}$$

Also,

According to the mirror formula,

$$\Rightarrow 1/f = 1/v - (-1/u)$$

$$\Rightarrow 1/f = -1/25 - 1/50$$

$$\Rightarrow 1/f = (-2-1)/50$$

$$\Rightarrow 1/f = -3/50 \Rightarrow f = -50/3 \text{ cm}$$

So, the focal length of mirror is 60 cm.

Now, we are given that $m = -1/5$

$$m = -v/u$$

$$\Rightarrow -1/5 = -v/u \Rightarrow v = u/5$$

According to mirror formula,

$$1/f = 1/u + 1/v$$

$$\Rightarrow -3/50 = 1/u + 5/u$$

$$\Rightarrow -3/50 = 6/u$$

Therefore, $u = 300/3 = 100$ cm

Q 30) A man holds a spherical shaving mirror of radius of curvature 60 cm, and focal length 30 cm, at a distance of 15 cm, from his nose. Find the position of image, and calculate the magnification.

ANS--Radius of curvature, $R = -60\text{cm}$ (concave mirror)

$F = -30\text{cm}$, $u = -15\text{cm}$

We have

$$1/v + 1/u = 1/f$$

$$1/v + 1/-15 = 1/-30$$

$$1/v = 1/15 + 1/-30$$

$$1/v = 1/30$$

$$V = 30 \text{ cm}$$

$$m = - (v/u)$$

$$m = - (30/-15)$$

$$m = 2$$

so, the image is formed 30 cm behind the mirror and the magnification is +2

Q 29) A concave mirror produces a real image 1 cm tall of an object 2.5 mm tall placed 5 cm from the mirror. Find the position of the image and the focal length of the mirror.

ANS-- $h_2 = 1\text{ cm} = 10\text{ mm}$ (real image), $h_1 = 2.5\text{ mm}$, $u = -5\text{ cm} = -50\text{ mm}$

$$m = -h_2/h_1$$

$$m = -(10/2.5)$$

$$m = -4$$

and we know that

$$m = -(v/u)$$

and we know that

$$m = -(v/u)$$

$$-4 = -(v/(-50))$$

$$v = -200\text{ mm}$$

$$v = -20\text{ cm}$$

The image is formed 20 cm in front of the mirror.

And,

$$1/v + 1/u = 1/f$$

$$1/-20 + 1/-5 = 1/f$$

$$1/f = -25/100$$

$$f = -4\text{ cm}$$

25) a bright object 50mm stands on the axis of concave mirror of focal length 100mm and at a distance of 300mm from the concave mirror how big will be the image?

ans—Height of the object (h) = 50 mm

Focal length of the mirror (f) = -100 mm

Object distance (u) = -300 mm

$$1/v + 1/u = 1/f$$

$$1/v = 1/f - 1/u$$

$$1/v = 1/(-100) - 1/(-300)$$

$$1/v = -1/100 + 1/300$$

$$1/v = (-3 + 1)/300$$

$$1/v = -2/300$$

$$v = 300/-2$$

$$v = -150 \text{ mm}$$

Therefore, the image will be formed 150 mm away from the pole.

magnification (m) = $h'/h = -v/u$

$$h' = -(v)(h)/u$$

$$h' = -(-150)(50) / (-300)$$

$$h' = -7500/300$$

$$h' = -25 \text{ mm}$$

Therefore the height of the image will be 25 mm