

Linear Equation In Two Variable

Exercise 3.1

Aftab tells his daughter:- seven years ago,

1) Let the present age of Aftab be 'x'
And the present age of daughter be 'y'

Seven years ago,

Age of Aftab = $x - 7$

Age of Daughter = $y - 7$

According to the question,

~~$x = 7$~~

$\Rightarrow x - 7 = 7(y - 7)$

$\Rightarrow x - 7 = 7y - 49$

$\Rightarrow x - 7y - 7 + 49$

$\Rightarrow x - 7y + 42 = 0$ ----- (i)
 $\Rightarrow -42 + 7y$

After three years,

Age of Aftab = $x + 3$

Age of Daughter = $y + 3$

ATQ $\Rightarrow x + 3 = 3(y + 3)$

$\Rightarrow x + 3 = 3y + 9$

$\Rightarrow x - 3y + 3 - 9$

$\Rightarrow x - 3y - 6$ ----- (ii)

Equation - 1

x	-7	0	7
$y = -42 + 7x$	5	6	7

Equation table - 2

x	6	4	0
$y = 6 + 3y$	0	-1	-2

The coach of a cricket team buys 3 bats & 2 balls.
 Let the cost of bat x and the cost of ball y

ATQ

$$3x + 2y = 3900 \quad \text{--- (1)}$$

$$x + 3y = 1300 \quad \text{--- (2)}$$

$$x = \frac{3900 - 2y}{3}$$

x	300	100	700
$y = \frac{3900 - 6x}{2}$	500	600	300

For $x + 3y = 1300$
 $x = 1300 - 3y$

x	400	100	700
$y = \frac{1300 - x}{3}$	300	400	200

3) The cost of 2kg of apples and 1kg of grapes on a day was found to be Rs 150. After a month, the cost of 4kg of apples and 2kg of grapes is Rs 300. Represent the situation algebraically and geometrically.

Ans → Let the cost of 1kg of apples be 'x'
and the cost of 1kg of grapes be 'y'

ATQ

$$2x + y = 160$$

$$\Rightarrow y = 160 - 2x$$

x	50	60	70
y	60	40	20

And, $4x + 2y = 300$
 $y = \frac{300 - 4x}{2}$

x	70	80	75
y	10	-10	0

Exercise 3.2

1) 10 students of class X took part in a Mathematics quiz. If the number of girls is 4 more than the number of boys, find the smallest number of boys and girls who take part in quiz.

Ans → Let the number of girls be x
and the number of boys be y

ATA

$$\Rightarrow n + y = 10 \quad \dots \dots \dots (1)$$

$$\Rightarrow y = 10 - n$$

n	5	4	6
$y = 10 - n$	5	6	4

And, the number of girls is 4 more than the number of boys

$$\Rightarrow n = y + 4 \quad \dots \dots \dots (2)$$

$$\Rightarrow n - y = 4$$

n	4	5	6
y	0	1	2

(ii) 5 pencils and 7 pens and 7 together cost ₹50, whereas 7 pencils and 5 pens together cost ₹46. Find the cost of one pencil and that of one pen.

Ans \Rightarrow Let the cost of pencils = n
and the cost of pens = y

ATA

$$\Rightarrow 5n + 7y = 50 \quad \dots \dots \dots (1)$$

$$\Rightarrow 7y = 50 - 5n$$

$$\Rightarrow y = \frac{50 - 5n}{7}$$

n	3	10	-4
$y = \frac{50 - 5n}{7}$	5	0	10

2) (i) $5x - 4y + 8 = 0$
 $7x + 6y - 9 = 0$

$$\frac{a_1}{a_2} = \frac{5}{7} \quad \frac{b_1}{b_2} = \frac{-4}{6} = \frac{-2}{3} \quad \frac{c_1}{c_2} = \frac{-8}{-9}$$

$\frac{a_1}{a_2} \neq \frac{b_1}{b_2} = \text{Intersect}$

(ii) $9x + 3y + 12 = 0$
 $18x + 6y + 24 = 0$

$$\frac{a_1}{a_2} = \frac{9}{18} = \frac{1}{2} \quad \frac{b_1}{b_2} = \frac{3}{6} = \frac{1}{2} \quad \frac{c_1}{c_2} = \frac{12}{24} = \frac{1}{2}$$

$\frac{a_1}{a_2} = \frac{b_1}{b_2} = \frac{c_1}{c_2} = \text{Parallel}$

(iii) $6x - 3y + 10 = 0$
 $2x - y + 9 = 0$

$$\frac{a_1}{a_2} = \frac{6}{2} = 3 \quad \frac{b_1}{b_2} = \frac{-3}{-1} = 3 \quad \frac{c_1}{c_2} = \frac{10}{9}$$

$\frac{a_1}{a_2} = \frac{b_1}{b_2} \text{ parallel}$

(iii) $6x - 3y + 10 = 0$
 $2x - y + 9 = 0$

$$\frac{a_1}{a_2} = \frac{6}{2} = \frac{3}{1}$$

$$\frac{b_1}{b_2} = \frac{3}{1}$$

$$\frac{c_1}{c_2} = \frac{10}{9}$$

$$\frac{a_1}{a_2} = \frac{b_1}{b_2} \neq \frac{c_1}{c_2} \quad \text{parallel}$$

ii) $3x + 2y = 5$
 $2x - 3y = 7$

$$\frac{a_1}{a_2} = \frac{3}{2}$$

$$\frac{b_1}{b_2} = \frac{2}{-3}$$

$$\frac{c_1}{c_2} = \frac{5}{7}$$

$$\frac{a_1}{a_2} \neq \frac{b_1}{b_2} \quad \text{Intersect, Consistent}$$

iii) $2x - 3y = 8$
 $4x - 6y = 9$

$$\frac{a_1}{a_2} = \frac{2}{4} = \frac{1}{2}$$

$$\frac{b_1}{b_2} = \frac{-3}{-6} = \frac{1}{2}$$

$$\frac{c_1}{c_2} = \frac{8}{9}$$

$$\frac{a_1}{a_2} = \frac{b_1}{b_2} \neq \frac{c_1}{c_2} \quad \text{Parallel Inconsistent}$$

iii) $\frac{3}{2}x + \frac{5}{3}y = 7$

$$9x - 10y = 14$$

$$\frac{a_1}{a_2} = \frac{3}{2 \times 9} = \frac{1}{6}$$

$$\frac{b_1}{b_2} = \frac{5}{3 \times -10} = \frac{-1}{6}$$

$$\frac{c_1}{c_2} = \frac{7}{14} = \frac{1}{2}$$

Intersecting Consistent

④ $5x - 3y = 11$
 $-10x + 6y = -22$

$$\frac{a_1}{a_2} = \frac{5}{-10} = \frac{1}{-2} \quad \frac{b_1}{b_2} = \frac{-3}{6} = \frac{-1}{2} \quad \frac{c_1}{c_2} = \frac{11}{-22} = \frac{1}{-2}$$

$$\frac{a_1}{a_2} = \frac{b_1}{b_2} = \frac{c_1}{c_2} = \text{parallel, Inconsistent.}$$

⑤ $\frac{4}{3}x + 2y = 8$

$$2x + 3y = 12$$

$$\frac{a_1}{a_2} = \frac{4}{3 \times 2} = \frac{2}{3} \quad \frac{b_1}{b_2} = \frac{2}{3} \quad \frac{c_1}{c_2} = \frac{8}{12} = \frac{2}{3}$$

4) ① $xy = 5$
 $2x + 2y = 10$

$$\frac{a_1}{a_2} = \frac{1}{2} \quad \frac{b_1}{b_2} = \frac{1}{2} \quad \frac{c_1}{c_2} = \frac{5}{10} = \frac{1}{2}$$

$$\frac{a_1}{c_1} = \frac{b_1}{c_1} = \frac{c_1}{c_2} \quad \text{parallel Consistent}$$

② $x - y = 8$
 $3x - 3y = 16$

$$\frac{a_1}{a_2} = \frac{1}{3}$$

$$\frac{b_1}{b_2} = \frac{1}{3}$$

$$\frac{c_1}{c_2} = \frac{1}{2}$$

$$\frac{a_1}{a_2} = \frac{b_1}{b_2}$$

parallel coincident

(iii)

$$2x + y - 6 = 0$$

$$4x - 2y - 4 = 0$$

$$\frac{a_1}{a_2} = \frac{2}{4} = \frac{1}{2}$$

$$\frac{b_1}{b_2} = \frac{1}{-2}$$

$$\frac{c_1}{c_2} = \frac{-6}{-4} = \frac{3}{2}$$

$$\frac{a_1}{a_2} \neq \frac{b_1}{b_2}$$

Intersect

(iv)

$$2x - 2y - 2 = 0$$

$$4x - 4y - 5 = 0$$

$$\frac{a_1}{a_2} = \frac{1}{2}$$

$$\frac{b_1}{b_2} = \frac{1}{2}$$

$$\frac{c_1}{c_2} = \frac{-2}{-5} = \frac{2}{5}$$

$$\frac{a_1}{a_2} = \frac{b_1}{b_2}$$

parallel

5) Half the perimeter of a rectangular garden whose length is 4m more than its width, is 36m. Find the dimension of the garden.

→

Ans Let the width of the garden is x
and the length of the garden is y .

ATQ

$$y - x = 4 \quad \text{--- (1)}$$

$$y = x + 4$$

x	0	8	12
$y = x + 4$	4	12	16

$$\Rightarrow y + x = 36 \quad \text{--- (2)}$$

$$\Rightarrow y = 36 - x$$

x	0	36	36
$y = 36 - x$	36	0	20

6) $2x + 3y - 8 = 0$

Intersecting

$$2x - 7y + 9 = 0$$

(ii) Parallel lines

$$6x + 9y + 9 = 0$$

(iii) Coincident lines

$$4x + 6y - 16$$

→ Draw the graphs of the equation $x-y+1=0$ and $3x+2y-12=0$. Determine coordinates of the vertices of the triangle formed by these lines and the x-axis. Shade the triangular region.

Ans → Given equations are → $x-y+1=0$
→ $3x+2y-12=0$

$$\begin{aligned} \Rightarrow x-y+1 &= 0 \\ \Rightarrow x-y &= -1 \\ \Rightarrow -y &= -x-1 \\ \Rightarrow y &= x+1 \end{aligned}$$

x	0	1	2
y = x+1	1	2	3

$$\begin{aligned} \Rightarrow 3x+2y-12 &= 0 \\ \Rightarrow 2y &= 12-3x \\ \Rightarrow y &= \frac{12-3x}{2} \end{aligned}$$

x	0	2	-2
y = $\frac{12-3x}{2}$	6	3	9

— X —

Exercise 3.3

$$\begin{aligned} \text{1) (i)} \quad x+y &= 14 \\ x-y &= 4 \end{aligned}$$

$$x+y=14$$

$$\Rightarrow x=14-y$$

Now substitute the value of x in second equation to get

$$x-y=4$$

$$\Rightarrow (14-y)-y=4$$

$$\Rightarrow 14-2y=4$$

$$\Rightarrow 2y=14-4$$

$$\Rightarrow y=5$$

By the value of y , we can now find the exact value of x

$$x=14-y$$

$$x=14-5$$

$$x=9$$

Hence, $x=9$ and $y=5$

$$\begin{aligned} \text{(ii)} \quad x-y &= 3 \\ \frac{x}{3} + \frac{y}{2} &= 6 \end{aligned}$$

$s - t = 3$ and
 $\frac{(s)}{3} + \frac{t}{2} = 6$ are the
 two equations

from 1st equation, we get,

$$s = 3 + t \text{ --- (1)}$$

Now substitute the value of s in second equation to get,

$$\frac{(3 + t)}{3} + \frac{t}{2} = 6$$

$$\Rightarrow \frac{(2(3 + t) + 3t)}{6} = 6$$

$$\Rightarrow \frac{(6 + 2t + 3t)}{6} = 6$$

$$\Rightarrow 6 + 5t = 36$$

$$\Rightarrow 5t = 36 - 6$$

$$\Rightarrow 5t = 30$$

$$\Rightarrow t = 30/5 = 6$$

Now, substitute the value of t in equation

$$s = 3 + 6 = 9$$

Therefore $s = 9$, $t = 6$

$$\text{(iii)} \quad \begin{aligned} 3x - y &= 3 \\ 9x - 3y &= 9 \end{aligned}$$

From 1st equation, we get

$$x = (3+y)/3$$

Now, substitute the value of x in the given second equation to get,

$$\begin{aligned} 9(3+y)/3 - 3y &= 9 \\ \Rightarrow 9 + 3y - 3y &= 9 \\ \Rightarrow 9 &= 9 \end{aligned}$$

Therefore, y has infinite values and since $x = (3+y)/3$, so x also has infinite values.

$$\text{(iv)} \quad \begin{aligned} 0.2x + 0.3y &= 1.3 \\ 0.4x + 0.5y &= 2.3 \end{aligned}$$

From 1st equation, we get,

$$x = (1.3 - 0.3y)/0.2 \quad \text{--- (1)}$$

Now, substitute the value of x in the given second equation to get,

$$\begin{aligned} \Rightarrow 0.4(1.3 - 0.3y)/0.2 + 0.5y &= 2.3 \\ \Rightarrow 2(1.3 - 0.3y) + 0.5y &= 2.3 \\ \Rightarrow 2.6 - 0.6y + 0.5y &= 2.3 \\ \Rightarrow 2.6 - 0.1y &= 2.3 \\ \Rightarrow 0.1y &= 0.3 \\ \Rightarrow y &= 3 \end{aligned}$$

Now substitute the value of y in equation (1) we get,

$$\begin{aligned} x &= (1.3 - 0.3(3)) / 2 \\ &= 1.3 - 0.9 / 0.2 \\ &= 0.4 / 0.2 \\ &= 2 \end{aligned}$$

Therefore $x=2$ and $y=3$

$$\begin{aligned} \textcircled{1} \quad \sqrt{2}x + \sqrt{3} &= 0 \\ \sqrt{3}x - \sqrt{8}y &= 0 \end{aligned}$$

From 1st equation we get,

$$x = (-\sqrt{3}/\sqrt{2})y \quad \text{--- --- --- } \textcircled{1}$$

Putting the value of x in the given second equation to get

$$\begin{aligned} \sqrt{3}(-\sqrt{3}/\sqrt{2})y - \sqrt{8}y &= 0 \\ \Rightarrow (-3\sqrt{2}y) - \sqrt{8}y &= 0 \\ y &= 0 \end{aligned}$$

Now, substitute the value of y in equation (1)

$$x = 0$$

Therefore $x=0$ and $y=0$.

$$(vi) \quad \frac{3x}{2} - \frac{5y}{3} = -2$$

$$\frac{x}{3} + \frac{y}{2} = \frac{13}{6}$$

From 1st equation we get,

$$\left(\frac{3}{2}\right)x = -2 + \left(\frac{5y}{3}\right)$$

$$\Rightarrow x = \frac{2(-6 + 5y)}{9}$$

$$= \frac{(-12 + 10y)}{9} \quad \dots \dots \dots (i)$$

Putting the value of x in the given second equation to get

$$\begin{aligned} \left(\frac{-12 + 10y}{9}\right) \frac{1}{3} + \frac{y}{2} &= \frac{13}{6} \\ \Rightarrow \frac{y}{2} &= \frac{13}{6} - \frac{(-12 + 10y)}{27} + \frac{y}{2} \\ &= \frac{13}{6} \end{aligned}$$

$$y = 3$$

Now substitute the values of y in equation

$$\Rightarrow \frac{3x}{2} - \frac{5(3)}{3} = -2$$

$$\Rightarrow \left(\frac{3x}{2}\right) - 5 = -2$$

$$\Rightarrow x = 2$$

Therefore, $x = 2$ and $y = 3$

2) Solve $2x + 3y = 11$ and $2x - 4y = -24$ and hence find the value of 'm' for which $y = mx + 3$.

Ans \rightarrow $2x + 3y = 11$ ----- (i)
 $2x - 4y = -24$ ----- (ii)

From equation (ii) we get,

$$x = (11 - 3y) / 2$$
 ----- (iii)

Substituting the value of x in equation (ii)

$$\Rightarrow 2 \cdot (11 - 3y) / 2 - 4y = -24$$

$$\Rightarrow 11 - 3y - 4y = -24$$

$$\Rightarrow -7y = -35$$

$$\Rightarrow y = 5$$
 ----- (iv)

Putting the value of y in equation (iii) we get,

$$\begin{aligned} x &= (11 - 3 \times 5) / 2 \\ &= -4 / 2 \\ &= -2 \end{aligned}$$

Hence, $x = (-2)$, $y = 5$

Also, $y = mx + 3$

$$5 = -2m + 3$$

$$-2m = 2$$

$$m = -1$$

Therefore the value of m is (-1) .

3) The difference between two numbers is 26 and one number is three times the other. Find them.
(i) Let the two numbers be x and y

ATQ

$$y = 3x \text{ ----- (1)}$$
$$y - 3x = 26 \text{ ----- (2)}$$

Substituting the value of (1) and (2) we get,
 $3x - x = 26$
 $x = 13 \text{ ----- (3)}$

(ii) The larger of two supplementary angles exceeds the smaller by 18 degrees. Find them

Ans) Let the larger angle be x° and the smaller angle be y°

We know that the sum of two supplementary pair of angles is always 180°

ATQ

$$x + y = 180^\circ \text{ ----- (1)}$$
$$x - y = 18^\circ \text{ ----- (2)}$$

From (1), we get $x = 180^\circ - y \text{ ----- (3)}$

Substituting (3) in (2), we get

$$180^\circ - y - y = 18^\circ$$
$$162^\circ = 2y$$
$$y = 81 \text{ ----- (4)}$$

Using the value of y in (3) we get,

$$x = 180^\circ - 81^\circ = 99^\circ$$

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(iii) The coach of a cricket team buys 7 bats and 6 balls for ₹3800. Later, she buys 3 bats and 5 balls for ₹1750. And the cost of each bat and each ball.

Ans: Let the cost of a bat be x and the cost of a ball be y .

ATQ

$$7x + 6y = 3800 \quad \text{--- (i)}$$

$$3x + 5y = 1750 \quad \text{--- (ii)}$$

From (i) we get,

$$y = \frac{3800 - 7x}{6} \quad \text{--- (iii)}$$

Substituting (iii) in (ii) we get,

$$3x + 5 \left(\frac{3800 - 7x}{6} \right) = 1750$$

$$\Rightarrow 3x + \frac{19000 - 35x}{6} = 1750$$

$$\Rightarrow 3x - \frac{35x}{6} = 1750 - \frac{19000}{6}$$

$$\Rightarrow \frac{(18x - 35x)}{6} = \frac{(10500 - 19000)}{6}$$

$$\Rightarrow \frac{-17x}{6} = \frac{-8500}{6}$$

$$\Rightarrow -17x = -8500$$

$$x = 500 \quad \text{--- (iv)}$$

Substituting the value of x in (iii) we get

$$y = \frac{3800 - 7 \times 500}{6}$$

$$= \frac{3000}{6} = 500$$

(iv) The taxi charges in a city consist of a fixed charge together with the charge for the distance covered. For a distance of 10 km, the charge paid is Rs 105 and for a journey of 15 km, the charge paid is 155. How much does a person have to pay for travelling a distance of 25 km.

Ans \rightarrow Let the fixed charge be Rs x
Per Capital charge be Rs y

ATQ

$$x + 10y = 105 \quad \text{--- (1)}$$

$$x + 15y = 155 \quad \text{--- (2)}$$

$$\text{From (1) we get } x = 105 - 10y \quad \text{--- (3)}$$

Substituting the value of x in (2) we get,

$$105 - 10y + 15y = 155$$

$$5y = 50$$

$$y = 50/5$$

$$y = 10 \quad \text{--- (4)}$$

Putting the value of y in (3) we get,

$$x = 105 - 10 \times 10$$

$$= 5.$$

(v) A fraction becomes $9/11$, if 2 is added to both the numerator and the denominator. If 3 is added to both the numerator and denominator, it becomes $5/6$. Find the fraction.

Ans Let the fraction be n/y

ATQ

$$\frac{n+y}{y+2} = \frac{9}{11}$$

$$\Rightarrow 11n - 9y = -4 \text{ ----- (1)}$$

$$\frac{(n+3)}{(y+3)} = \frac{5}{6}$$

$$6n + 18 = 5y + 15$$

$$\Rightarrow 6n - 5y = -3 \text{ ----- (2)}$$

From (1) we get $n =$

$$\frac{(-4 + 9y)}{11} \text{ ----- (3)}$$

Substituting the value of n in (2) we get,

$$\frac{6(-4 + 9y)}{11} - 5y = 3$$

$$\Rightarrow -24 + 54y - 55y = -33$$

$$\Rightarrow -y = -9$$

$$\Rightarrow y = 9 \text{ ----- (4)}$$

Substituting the value of y in (3) we get

$$n = \frac{(-4 + 9 \times 9)}{11} = 7$$

Hence the fraction is $7/9$.

Exercise 3.4

1. Solve the following pairs of linear equations by the elimination method and the substitution method:

(i) $x + y = 5$ and $2x - 3y = 4$

By method of Elimination

$$\begin{aligned} x + y &= 5 && \text{--- (i)} \\ 2x - 3y &= 4 && \text{--- (ii)} \end{aligned}$$

When the equation (i) is multiplied by 2 we get,

$$\begin{aligned} 5y &= 6 && 2x + 2y = 10 && \text{--- (iii)} \\ y &= 6/5 && \text{---} && \text{---} \end{aligned}$$

$$x = 19/5, y = 6/5$$

(ii) $3x + 4y = 10$ and $2x - 2y = 2$

By the method of Elimination

$$\begin{aligned} 3x + 4y &= 10 && \text{--- (i)} \\ 2x - 2y &= 2 && \text{--- (ii)} \end{aligned}$$

When the equation (i) and (ii) is multiplied by 2; we get

$$4x - 4y = 4 && \text{--- (iii)}$$

Hence $x = 2$ and $y = 1$

(ii) Five years ago Nuri was thrice as old as Sonu. Ten years later, Nuri will be twice as old as Sonu. How old are Nuri and Sonu?

Ans: Let us assume present age of Nuri is n and present age of Sonu = y

ATQ

$$n - 5 = 3(y - 5) \quad \text{--- (i)}$$
$$\Rightarrow n - 3y = -10$$

Now, $n + 10 = 2(y + 10)$ --- (ii)

$$\Rightarrow n - 2y = 10$$

Age of Nuri is 50 years
Age of Sonu is 20 years.

Exercise 3.5

1) (i) $n - 3y - 3 = 0$
3) $-9y - 2 = 0$

Parallel

(ii) $2n + y = 5$
 $3n + 2y = 8$

Intersect

(iii)

$$\begin{aligned} 3x - 2y &= 20 \\ 6x - 7y &= 40 \end{aligned}$$

Infinite Numbers.

(iv)

$$\begin{aligned} x - 3y - 7 &= 0 \\ 3x - 3y - 15 &= 0 \end{aligned}$$

Intersecting

2) (i)

$$2x + 3y = 7$$

$$(a-b)x + (a+b)y = 3a+b=2$$

(i)

$$(a+b)y + (a-b)y - (3a+b-2) = 0$$

$$a_1/a_2 = 2(a-b) \quad b_1/b_2 = 3(a+b)$$

thus at $a=5 \quad b=1$

(a)

3) Solve the following pair of linear equations

$$8x + 5y = 9 \quad \text{--- (i)}$$

$$3x + 2y = 4 \quad \text{--- (ii)}$$

$$x = (4 - 2y) / 3 \quad \text{--- (iii)}$$

$$8(4 - 2y) / 3 + 5y = 9$$

$$y = -5$$

$$y = 5$$

$x = -2$ and $y = 5$.

4) (i) Let x be the fixed charge
and y be charge of food per day.

$$x + 20y = 1000 \quad \text{--- (i)}$$
$$x + 26y = 1180 \quad \text{--- (ii)}$$

Subtracting (i) from (ii) get,

$$6y = 180$$
$$y = 30$$

Using this value in equation

$$x = 1180 - 26 \times 30$$
$$x = \text{Rs } 400$$

Therefore, fixed charges is Rs 400 and Charge per day is Rs 30.

(ii) Let the fraction be $\frac{x}{y}$

So as per the question given

$$\frac{(x-1)}{y} = \frac{1}{3} \Rightarrow 3x - y = 3 \quad \text{--- (i)}$$
$$x(y+8) = \frac{1}{4} \Rightarrow 4x - y = 8 \quad \text{--- (ii)}$$

$$y = 12,$$

Therefore the fraction is $\frac{5}{12}$

(ii)

Let the number of right answers is x
and number of wrong be y

$$\rightarrow 3x - y = 40 \text{ ----- (1)}$$
$$4x - 2y = 50$$

$$\rightarrow 2x - y = 25 \text{ ----- (2)}$$

Subtracting equations (2) from equation (1)

$$x = 15 \text{ ----- (3)}$$

Putting this in equation (2)

$$30 - y = 25$$
$$y = 5$$

Exercise 3.6

(i) $\frac{1}{2x} + \frac{1}{3y} = 2$

$$\frac{1}{3x} + \frac{1}{2y} = \frac{13}{6}$$

$$m/(-26 - (-36)) = n/(-24 - (-39)) = \frac{1}{9-4}$$

$$m/10 = n/15 = 1/5$$

$$m/10 = 1/5 \text{ and } n/15$$

$$m = 2 \text{ and } n = 3$$

(ii) $\frac{2}{\sqrt{x}} + \frac{3}{\sqrt{y}} = 2$

$\frac{4}{\sqrt{x}} - \frac{9}{\sqrt{y}} = (-1)$

Ans $\rightarrow 2m + 3n = 2$ ----- (i)

$4m - 9n = -1$ ----- (ii)

Multiplication equation

$6m + 9n = 6$ ----- (iii)

$2 \times 1/2 + 3n = 2$

$3n = 1$

$n = 1/3$

$x = 4, y = 9$

Hence $x = 4$ and $y = 9$

(iii) $\frac{4}{x} + 3y = 14$

$\frac{3}{x} - 4y = 23$

Ans $\rightarrow 4x + 3y - 14 = 0$ ----- (i)

$\rightarrow 3x - 4y - 23 = 0$ ----- (ii)

By cross multiplication,

$$m/(-69-56) = y/(-42 - (-92)) = 1/(-16-9)$$

$$m/125 = -1/25 \text{ and } y/50 = -1/25$$

$$m = 5 \text{ and } b = (-2)$$

$$m = 1/n = 5$$

$$\text{So } n = 1/5, \quad y = 2$$

2/1

Ritu can row downstream 20 km in 2 hrs, and upstream 4 km in 2 hrs. Find her speed of rowing in still water and the speed of the current.

Ans Speed of Ritu in still water = x km/hr.

Speed of stream = y km/hr.

ATQ,

$$2(x+y) = 20$$

$$x+y = 10 \quad \text{--- (1)}$$

$$\text{And } 2(x-y) = 4$$

Adding both the eq 1 and 2

$$2x = 12$$

$$x = 6$$

$$y = 4$$

Ritu rowing still water = 6

(ii) 2 women and 5 men can together finish an embroidery work in 4 days, while 3 women and 6 men together can finish in 3 days. Find the time taken by 1 woman alone to finish work, and also that taken by 1 man alone.

Ans → Number of days = y
 work done = y

$$4 \left(\frac{2}{x} + \frac{5}{y} \right) = 1$$

$$\left(\frac{2}{x} + \frac{5}{y} \right) = \frac{1}{4}$$

And $3 \left(\frac{3}{x} + \frac{6}{y} \right) = 1$

$$\left(\frac{3}{x} + \frac{6}{y} \right) = \frac{1}{3}$$

Now by cross multiplication,

$$m/20-18 = n/(9-8) = 1/(180-144)$$

$$m = 1/18$$

$$m = 1/x = 1/18$$

$$x = 18$$

$$y = 36$$

Number of days 18.

Number of days to finish 36.

(iii) Rishi travels 300 km to her home partly by train and partly by bus. She takes 4 hours if she travels 60 km by train & remaining by bus. Find the speed of the train & bus separately.

Ans
Speed of train = x km/h

Speed of bus = y km/h

ATQ

$$60/x + 240/y = 4 \quad \text{--- (i)}$$

$$100/x + 200/y = 25/6 \quad \text{--- (ii)}$$

$$\Rightarrow 60x + 240y = 4 \quad \text{--- (iii)}$$

$$\Rightarrow 600x + 1200y = 25 \quad \text{--- (iv)}$$

Multiply eq. 3 by 10 to get

$$60x + 2400y = 40$$

$$x = 1/60$$

$$x = \frac{1}{n} = \frac{1}{60}$$

$$x = 60$$

And $y = 1/n$

$$y = 80$$

Therefore, speed of train = 60 km/h &
speed of bus = 80 km/h.