

Exercise 4.2

1) Find the roots of the following quadratic equations by factorisation:

(i) $x^2 - 3x - 10 = 0$

$$\Rightarrow x^2 - 5x + 2x - 10$$

$$\Rightarrow x(x-5) + 2(x-5)$$

$$\Rightarrow (x-5)(x+2)$$

The roots of this equation $x^2 - 3x - 10 = 0$ are the various values of x for which $(x-5)(x+2) = 0$

Therefore $x-5=0$ or $x+2=0$
 $\Rightarrow x=5$ or $x=-2$

(ii) $2x^2 + x - 6 = 0$

Taking LHS,

$$\Rightarrow 2x^2 + 4x - 3x - 6$$

$$\Rightarrow 2x(x+2) - 3(x+2)$$

$$\Rightarrow (x+2)(2x-3)$$

The roots of this equation, $2x^2 + x - 6 = 0$, are the values of x for which $(x+2)(2x-3) = 0$

Therefore, $x+2=0$ or $2x-3=0$

$$\Rightarrow x = -2 \quad \text{or} \quad x = \frac{3}{2}$$

$$(iii) \sqrt{2}u^2 - 7u + 5\sqrt{2} = 0$$

Taking LHS,

$$\Rightarrow \sqrt{2}u^2 + 5u + 2u + 5\sqrt{2}$$

$$\Rightarrow u(\sqrt{2}u + 5) + \sqrt{2}(\sqrt{2}u + 5) = (\sqrt{2}u + 5)(u + \sqrt{2})$$

The roots of this equation $\sqrt{2}u^2 + 7u + 5\sqrt{2} = 0$ are the values of u for which $(u + \sqrt{2})(u + 5) = 0$

$$\text{Therefore } \sqrt{2}u + 5 = 0 \text{ or } u + \sqrt{2} = 0$$

$$\Rightarrow u = -5/\sqrt{2} \text{ or } u = -\sqrt{2}$$

$$(iv) \frac{2u^2 - u + 1}{8} = 0$$

Taking LHS,

$$\Rightarrow \frac{1}{8}(16u^2 - 8u + 4)$$

$$= \frac{1}{8}(16u^2 - 4u - 4u + 4)$$

$$= \frac{1}{8}(4u(4u - 1) - 1(4u - 1))$$

$$= \frac{1}{8}(4u - 1)^2$$

The roots of this equation, $\frac{2u^2 - u + 1}{8} = 0$ are the values of u for which $(4u - 1)^2 = 0$

$$\text{Therefore } (4u - 1) = 0 \text{ or } (4u - 1) = 0$$

$$\Rightarrow u = 1/4 \text{ or } u = 1/4.$$

$$(v) 100u^2 - 20u + 1 = 0$$

Taking LHS,

$$= 100u^2 - 10u - 10u + 1$$

$$= 10u(10u - 1) - 1(10u - 1)$$

$$= (10u - 1)^2$$

$$\Rightarrow 10u - 1 = 0 \text{ or } u = 1/10$$

3) Find two numbers whose sum is 27 and product is 182.

Ans: First Number be x
Second Number be $27-x$

Therefore the product of two numbers

$$\begin{aligned}x(27-x) &= 182 \\ \Rightarrow x^2 - 27x - 182 &= 0 \\ \Rightarrow x^2 - 13x - 14x + 182 &= 0 \\ \Rightarrow x(x-13) - 14(x-13) &= 0 \\ \Rightarrow (x-13)(x-14) &= 0 \\ x &= 13 \quad \text{and} \quad x = 14\end{aligned}$$

First number 13
Second Number = $27-13$
 $= 14$

And if first number 14
Second number = $27-14$
 $= 13$

Hence the numbers are 13 and 14.

4) Find two consecutive positive integers whose sum of squares is 365.

Ans: Let, the two consecutive positive integers be x and $x+1$.

$$\begin{aligned}
 n^2 + (n+1)^2 &= 365 \\
 \Rightarrow n^2 + n^2 + 1 + 2n &= 365 \\
 \Rightarrow 2n^2 + 2n - 364 &= 0 \\
 \Rightarrow n^2 + n - 182 &= 0 \\
 \Rightarrow n^2 + 14n - 13n - 182 &= 0 \\
 \Rightarrow n(n+14) - 13(n+14) &= 0 \\
 \Rightarrow (n+14)(n-13) &= 0
 \end{aligned}$$

Thus the integers are positive

$$\therefore n+1 = 13+1 = 14$$

5) The altitude of a right triangle is 7 cm less than its base. If the hypotenuse is 13 cm, find the other two sides.

Ans: The base of the right triangle be n cm

Given the altitude of right triangle = $(n-7)$ cm

From Pythagoras theorem, we know

$$\text{Base}^2 + \text{Altitude}^2 = \text{Hypotenuse}^2$$

$$\Rightarrow n^2 + (n-7)^2 = 13^2$$

$$\Rightarrow n^2 + n^2 + 49 - 14n = 169$$

$$\Rightarrow 2n^2 - 14n - 120 = 0$$

$$\Rightarrow n^2 - 7n - 60 = 0$$

$$\Rightarrow n^2 - 12n + 5n - 60 = 0$$

$$\Rightarrow n(n-12) + 5(n+12) = 0$$

$$\Rightarrow (n-12)(n+5) = 0$$

$$n = 12 \quad \text{or} \quad n = -5$$

6) A cottage industry produces a certain number of pottery articles in a day. It was observed that each article cost more than twice the number of articles produced in a day. If the total cost of day = 90. Find the number of articles produced and the cost of each article.

Ans → Let us say the number of articles produced be x .

Therefore, cost of production of each article = RS $(2x+3)$.

Given total cost of production is RS 90.

$$\therefore x(2x+3) = 90$$

$$\Rightarrow 2x^2 + 3x - 90 = 0$$

$$\Rightarrow 2x^2 + 15x - 12x - 90 = 0$$

$$\Rightarrow x(2x+15) - 6(2x+15) = 0$$

$$\Rightarrow (2x+15)(x-6) = 0$$

Thus either $2x+15 = 0$ or $x-6 = 0$

$$\Rightarrow x = -15/2 \text{ or } x = 6$$

$$\text{Cost of each article} = 2 \times 6 + 3 = ₹ 15.$$