

Home Assignment 2/07/21

① $r = 0.05 \text{ m}$

The magnetic ~~field~~ field induction at O due to current through circular coil abcd will be zero. Because magnetic field induction at O due to current through segment abc of the coil is equal and opposite to that due to B induction due to current through long straight conductor.

$$B_1 = \frac{\mu_0 I}{4\pi r} (\sin 90^\circ + \sin 0^\circ) = \frac{1}{2} \frac{\mu_0 I}{2\pi r} =$$

~~to~~ I_0

$$10^{-7} \times \frac{5}{5 \times 10^{-2}}$$

Total magnetic field induction at O

$$= 10^{-5} \text{ T}$$

$$B = B_1 + B_2 = 10^{-5} + 10^{-5} = \boxed{2 \times 10^{-5}} \text{ Normally outward to the plane of paper}$$

② Field due to straight conductor

$$B_1 = \frac{\mu_0 I}{2\pi r}, \text{ up the plane of the paper}$$

Field due to circular loop at point O

$$B_2 = \frac{\mu_0 I}{2r}, \text{ up the plane of paper}$$

$$\text{Total } B_1 + B_2 = \frac{\mu_0 I}{2\pi r} + \frac{\mu_0 I}{2r} = \boxed{\frac{\mu_0 I}{2r} \left(1 + \frac{1}{\pi}\right)}$$

$$(3) \quad B_1 = \frac{\mu_0 I}{4\pi a} \quad \text{(outward)} \quad B_2 = \frac{\mu_0 I}{4\pi b} \quad \text{(inward)}$$

$B_3 = 0 \quad B_4 = 0$ } O is along a straight wire

$$B_{net} = B_1 - B_2 = \frac{\mu_0 I \alpha}{4\pi} \left[\frac{1}{a} - \frac{1}{b} \right]$$

$$B = \frac{\mu_0 I \alpha (b-a)}{4\pi a b}$$

(4)

$$B_p = \frac{\mu_0 I}{2\pi R} = \frac{\mu_0}{2\pi R}$$

$$B_2 = \frac{\mu_0 I}{2\pi R} = \frac{\mu_0 \sqrt{3}}{2\pi R}$$

$$B = \sqrt{B_p^2 + B_2^2} = \sqrt{\left(\frac{\mu_0}{2\pi R}\right)^2 + \left(\frac{\mu_0 \sqrt{3}}{2\pi R}\right)^2}$$

$$= \frac{\mu_0}{2\pi R} \sqrt{4} = \frac{\mu_0}{\pi R} \quad \tan B = \frac{AB}{B} = \frac{\mu_0}{\mu_0 \sqrt{3}} = \frac{1}{\sqrt{3}}$$

$$B = 30^\circ \quad \underline{\underline{\text{Ans}}}$$

The direction of net magnetic field is 30° with the x direction.

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B due to circular loop = $\frac{\mu_0 2\pi R^2 I}{4\pi (r^2 + R^2)^{3/2}}$

$$\vec{B} = \frac{\mu_0 R^2 I}{2(r^2 + R^2)^{3/2}}$$

$$|\vec{B}_{net}| = \sqrt{2} |\vec{B}| = \frac{\sqrt{2} \mu_0 R^2 I}{2(r^2 + R^2)^{3/2}}$$

direction is along $\frac{-\hat{i} - \hat{j}}{\sqrt{2}}$