

Home Assignment

- ① Ampere's circuital law states that line integral of magnetic field around any closed loop is equal to μ_0 times the electric current flowing through the cross section area enclosed by that loop.

Mathematically $\oint \mathbf{B} \cdot d\mathbf{l} = \mu_0 I$

Let the current flowing in the solenoid having number of turns per unit length n be I .

Magnitude of magnetic field inside the solenoid B while outside is zero.

Now $\oint_{\text{loop}} \mathbf{B} \cdot d\mathbf{l} = \int_{ab} \mathbf{B} \cdot d\mathbf{l} + \int_{bc} \mathbf{B} \cdot d\mathbf{l} + \int_{cd} \mathbf{B} \cdot d\mathbf{l} + \int_{da} \mathbf{B} \cdot d\mathbf{l}$

The value of first term $\int_{ab} \mathbf{B} \cdot d\mathbf{l} = BL$

The second and fourth term are zero because angle between magnetic field and the length of the loop is 90°

The third term is also zero as the value of magnetic field outside the solenoid is zero

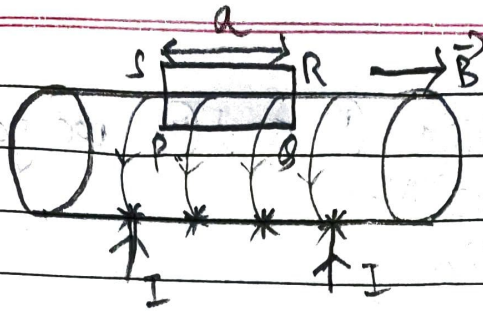
Total current flow through the loop

$I_{\text{total}} = (nL)I$

From Ampere's circuital law, we get $BL = \mu_0 (nLI)$

$\Rightarrow B = \mu_0 nI$

2a)



Current flowing through each current = I
Magnetic field is zero outside the solenoid and is present only in the horizontal axis as, while taking each term the vertical components cancel out each other.

length of the Solenoid = l

$$PS = RS = a$$

current through length $a = I_0$

According to Ampere's circuital law.

$$\oint \vec{B} \cdot d\vec{e} = \mu_0 I$$

$$\begin{aligned} \text{LHS} :- \oint \vec{B} \cdot d\vec{e} &= \int_P^Q \vec{B} \cdot d\vec{e} + \int_Q^R \vec{B} \cdot d\vec{e} + \int_R^S \vec{B} \cdot d\vec{e} + \int_S^P \vec{B} \cdot d\vec{e} \\ &= \int \vec{B} \cdot d\vec{e} \cos 0^\circ + \int \vec{B} \cdot d\vec{e} \cos 90^\circ + \int \vec{B} \cdot d\vec{e} + \int \vec{B} \cdot d\vec{e} \cos 90^\circ \\ &= \int \vec{B} \cdot d\vec{e} \Rightarrow B \int d\vec{e} \\ &= Ba \quad \text{--- (1)} \end{aligned}$$

$$\text{Now, } \oint \vec{B} \cdot d\vec{e} = Ba$$

$$\text{No. of turns per unit length} = \frac{n}{l}$$

$$\begin{aligned} \text{Total current} &= n l I \\ &= n I \end{aligned}$$

$$Ba = (n I) \mu_0 \quad \text{--- (11)}$$

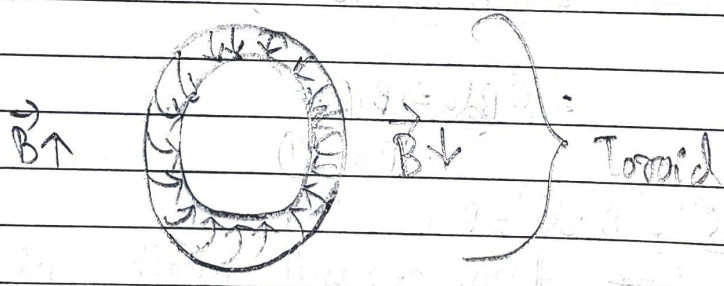
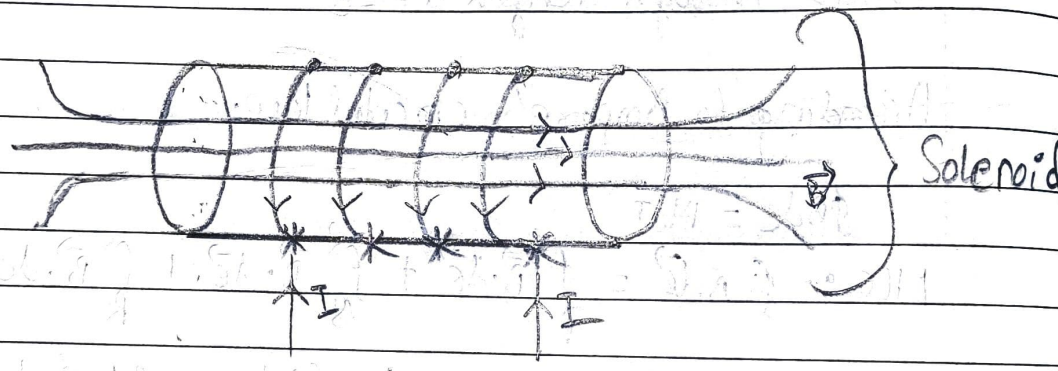
By equating (I) and (II) we got

$$B a = (n a I) \mu_0$$

$$B = n I \mu_0$$

(b) In Solenoid, the magnetic field is present inside it, where it is uniformly present at the axis but decreases towards the end and does not exist outside the solenoid.

In Toroid, the magnetic field is present in the tubular area bounded by the coil and is not present inside and outside the toroid.



(c) The magnetic field can be increased by i

- Increasing the no. of turns per unit length
- Increasing the current through it.

③ $n = 300$ $l = 0.5 \text{ m}$
 $I = 5 \text{ A}$ $r = 1 \text{ cm} = 0.01 \text{ m}$

$l \gg r$, So. it is a ideal Solenoid

$$B = \mu_0 n I$$

$$= 4\pi \times 10^{-7} \times 300 \times 5$$

$$= 4 \times 3.14 \times 1500 \times 10^{-7}$$

$$= 1.88 \times 10^{-3} \text{ T}$$

④ $l = 0.5 \text{ m}$ $n = \frac{N}{l} = \frac{500}{0.5} = 1000$
 By $n I = 500$

Flux density (B) $= 2.52 \times 10^{-3}$

As we know,

$$B = \mu_0 n I$$

$$\Rightarrow 2.52 \times 10^{-3} = 4\pi \times 10^{-7} \times 1000 \times I$$

$$\Rightarrow I = \frac{2.52 \times 10^{-3}}{4\pi \times 10^{-7} \times 1000}$$

$$= \frac{0.63 \times 10}{3.14}$$

$$= 2 \text{ A}$$