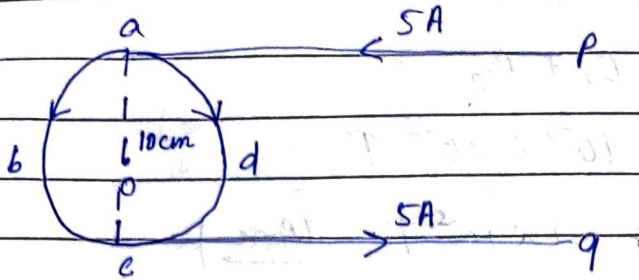


Home assignment

02.07.21

Moving charges and Magnetism

①



$$i = 5 \text{ A}$$

$$\text{diameter} = 10 \text{ cm}$$

Current in the part abc is equal to adc

$$abc = adc = 2.5 \text{ A}$$

$$\text{radius} = oa = oc = ob = od = 5 \text{ cm}$$

Magnetic field induction through at O due to current through circular coil will be zero because the magnetic field induction at O due to current through segment abc of the coil is equal and opposite to that due to current through segment adc.

Magnetic field induction at O due to current through pa.

$$\Rightarrow B_1 = \frac{\mu_0}{4\pi} \frac{I}{r} (\sin 90^\circ + \sin 0^\circ)$$

$$= \frac{\mu_0}{4\pi} \frac{I}{r} = 10^{-7} \times \frac{5}{5 \times 10^{-2}} = 10^{-5} \text{ T outwards normally to the paper.}$$

Magnetic field induction at O due to current through qc.

$$\Rightarrow B_2 = \frac{\mu_0}{4\pi} \frac{I}{r} (\sin 90^\circ + \sin 0^\circ)$$

$$= \frac{\mu_0}{4\pi} \frac{I}{r} = 10^{-7} \times \frac{5}{5 \times 10^{-2}} = 10^{-5} \text{ T.}$$

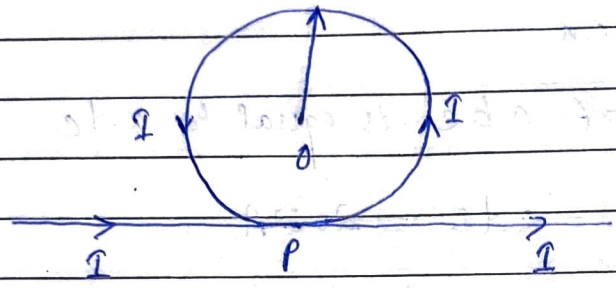
Total magnetic field induction

$$B = B_1 + B_2$$

$$B = 10^{-5} + 10^{-5} \text{ T}$$

$$B = 2 \times 10^{-5} \text{ T} \quad (\text{Ans})$$

(2)



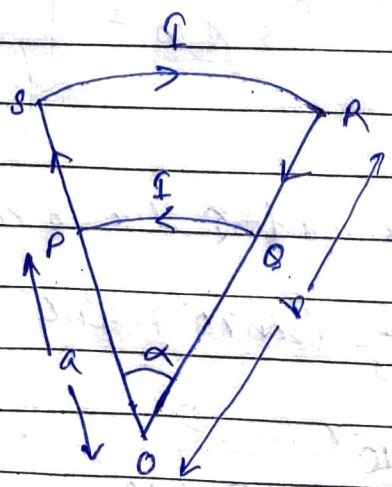
$$B_1 = \frac{\mu_0 I}{2r}$$

$$B_2 = \frac{\mu_0 I}{2\pi r}$$

$$B_1 + B_2 = \frac{\mu_0 I}{2r} + \frac{\mu_0 I}{2\pi r}$$

$$= \frac{\mu_0 I}{2r} \left(1 + \frac{1}{\pi} \right) \quad (\text{Ans})$$

(3)



$$\vec{B}_{SR} = \frac{\mu_0 i}{2b} \left[\frac{\alpha}{2\pi} \right] (-\hat{k})$$

$$\vec{B}_{PS} = \frac{\mu_0 i}{2a} \left[\frac{\alpha}{2\pi} \right] (-\hat{k})$$

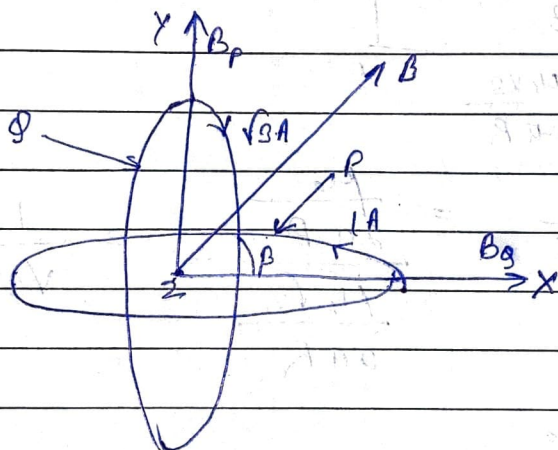
B_{net}

Due to SP and RQ will be 0.

$$\vec{B}_{net} = \frac{\mu_0 i \alpha}{4\pi} \left[\frac{1}{a} - \frac{1}{b} \right]$$

$$\vec{B}_{net} = \frac{\mu_0 i \alpha}{4\pi ab} (b-a) \quad (\underline{\underline{Ans}})$$

(4)



Magnetic field at the centre of the coil are perpendicular to each other.

B_{net} is the resultant of two fields caused due to coil P and Q.

$$B_p = \frac{\mu_0 I}{2aR} = \frac{\mu_0}{2aR}$$

$$B_q = \frac{\mu_0 I}{2aR} = \frac{\mu_0 \sqrt{3}}{2aR}$$

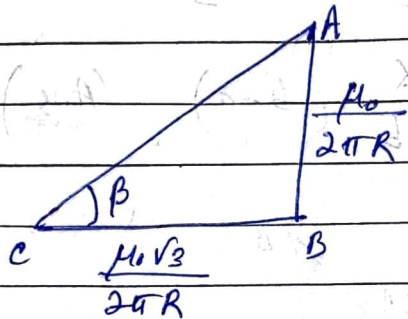
Net magnetic field $B = \sqrt{B_p^2 + B_q^2}$

$$= \sqrt{\left(\frac{\mu_0}{2aR}\right)^2 + \left(\frac{\mu_0 \sqrt{3}}{2aR}\right)^2}$$

$$= \frac{\mu_0}{2aR} \sqrt{4}$$

$$= \frac{\mu_0}{aR}$$

For Direction of magnetic field

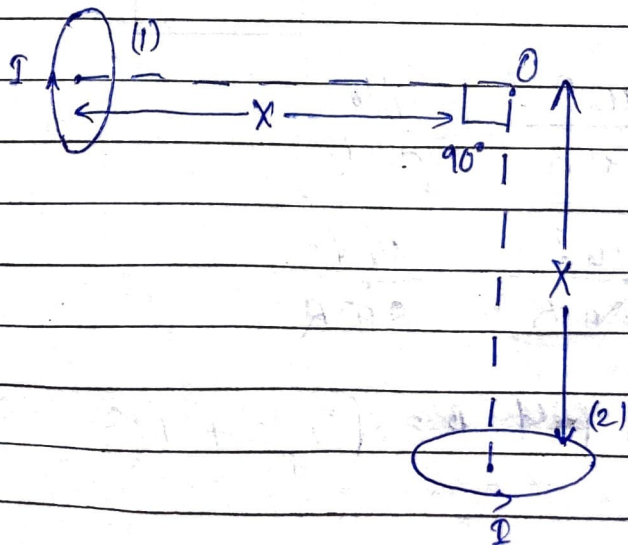


$$\beta = \frac{AB}{BC} = \frac{\frac{\mu_0}{2aR}}{\frac{\mu_0 \sqrt{3}}{2aR}} = \frac{1}{\sqrt{3}} = 30^\circ$$

$$\beta = 30^\circ$$

The direction of magnetic field is 30° with the X direction.

(D)



magnetic field due to circular loop = $\frac{\mu_0}{4\pi} \frac{2\pi R^2 I}{(x^2 + R^2)^{3/2}}$

$$|\vec{B}| = \frac{\mu_0 R^2 I}{2(x^2 + R^2)^{3/2}}$$

$$|\vec{B}_{\text{net}}| = \sqrt{2} |\vec{B}| = \frac{\sqrt{2} \mu_0 R^2 I}{2(x^2 + R^2)^{3/2}}$$

So $|\vec{B}_{\text{net}}|$ & its direction is $\frac{\mu_0 R^2 I}{\sqrt{2}(x^2 + R^2)^{3/2}}$

is along vector $\frac{\hat{i} - \hat{j}}{\sqrt{2}}$ (here)