

EXERCISE

5.37 Magnetic field strength,  $B = 0.25 \text{ T}$

Torque on the bar magnet,  $T = 4.5 \times 10^{-2} \text{ J}$

Angle b/w the bar magnet and the external magnetic field,  $\theta = 30^\circ$

Torque is related to magnetic moment ( $M$ ) as:

$$T = MB \sin \theta$$

$$\therefore M = \frac{T}{B \sin \theta}$$

$$= \frac{4.5 \times 10^{-2}}{0.25 \times \sin 30^\circ}$$

$$= \frac{4.5 \times 10^{-2}}{0.25 \times 0.5} = 0.36 \text{ J T}^{-1}$$

$$= 0.36 \text{ J T}^{-1}$$

Ans

5.4) Moment of the bar magnet,  $M = 0.32 \text{ J T}^{-1}$

External magnetic field,  $B = 0.15 \text{ T}$

(a) The bar magnet is aligned along the magnetic field. The system is considered as being in stable equilibrium. Hence, the angle  $\theta$ , b/w the bar magnet and the magnetic field is  $0^\circ$ .

$$\text{Potential energy of the system} = -MB \cos \theta$$

$$= -0.32 \times 0.15 \cos 0^\circ$$

$$= -4.8 \times 10^{-2} \text{ J}$$

Ans

(b) The bar magnet is obtained oriented  $180^\circ$  to the magnetic field. Hence, it is in unstable equilibrium,  $\theta = 180^\circ$

$$\text{Potential energy} = -MB \cos \theta$$

$$= -0.32 \times 0.15 \cos 180^\circ$$

$$= 4.8 \times 10^{-2} \text{ J}$$

Ans



5.5) No. of turns in the solenoid,  $n = 800$   
Area of cross-section,  $A = 2.5 \times 10^{-4} \text{ m}^2$   
Current in the solenoid,  $I = 3.0 \text{ A}$

A current carrying solenoid behaves as a bar magnet, because a magnetic field develops along its axis, i.e. along its length.

The magnetic moment associated with the given current-carrying solenoid is calculated as:

$$\begin{aligned} M &= nIA \\ &= 800 \times 3 \times 2.5 \times 10^{-4} \\ &= 0.6 \text{ JT}^{-1} \end{aligned} \quad \underline{\text{Ans}}$$

5.8) No. of turns on the solenoid,  $n = 2000$   
Area of cross-section of the solenoid,  $A = 1.6 \times 10^{-4} \text{ m}^2$   
Current in the solenoid,  $I = 4 \text{ A}$

(a) The magnetic moment along the axis of the solenoid is calculated as:

$$\begin{aligned} M &= nAI \\ &= 2000 \times 1.6 \times 10^{-4} \times 4 \\ &= 1.28 \text{ Am}^2 \end{aligned} \quad \underline{\text{Ans}}$$

(b) Magnetic field,  $B = 7.5 \times 10^{-2} \text{ T}$   
Angle b/w the magnetic field and the axis of the solenoid  
 $\theta = 30^\circ$

$$\begin{aligned} \text{Torque, } \tau &= MB \sin \theta \\ &= 1.28 \times 7.5 \times 10^{-2} \sin 30^\circ \\ &= 4.8 \times 10^{-2} \text{ Nm} \end{aligned} \quad \underline{\text{Ans}}$$

5.9) No. of turns in the circular coil,  $N = 16$

Radius of the coil,  $r = 10 \text{ cm} = 0.1 \text{ m}$

Cross-section of the coil,  $A = \pi r^2 = \pi \times (0.1)^2 \text{ m}^2$

Current in the coil,  $I = 0.75 \text{ A}$

Magnetic field strength,  $B = 5.0 \times 10^{-2} \text{ T}$

Frequency of oscillation of the coil,  $\nu = 2.0 \text{ s}^{-1}$

∴ Magnetic moment,  $M = NIA = N I \pi r^2$

$$= 16 \times 0.75 \times \pi \times (0.1)^2$$

$$= 0.377 \text{ J T}^{-1}$$

Frequency is given by the relation:

$$\nu = \frac{1}{2\pi} \sqrt{\frac{MB}{I}}, \text{ where } I = \text{moment of inertia of the coil}$$

$$\therefore I = \frac{MB}{4\pi^2 \nu^2}$$

$$= \frac{0.377 \times 5 \times 10^{-2}}{4\pi^2 \times (2)^2} = 1.19 \times 10^{-4} \text{ kg m}^2$$

Ans

5.11) Angle of declination,  $\theta = 12^\circ$

Angle of dip,  $\delta = 60^\circ$

Horizontal component of earth's magnetic field,

$$B_H = 0.16 \text{ G}$$

Earth's magnetic field at the given location =  $B$

We can relate  $B$  and  $B_H$  as:

$$B_H = B \cos \delta$$

$$\therefore B = \frac{B_H}{\cos \delta} = \frac{0.16}{\cos 60^\circ} = 0.32 \text{ G}$$

Ans



5.13) Earth's magnetic field at the given place,  $H = 0.36 \text{ G}$   
The magnetic field at a distance  $d$ , on the axis of the magnet is given as:

$$B_1 = \frac{\mu_0}{4\pi} \frac{2M}{d^3} = H \quad \text{--- (1)}$$

where,

$\mu_0$  = Permeability of free space

$M$  = magnetic moment

The magnetic field at the same distance  $d$ , on the equatorial line of the magnet is given as:

$$B_2 = \frac{\mu_0 M}{4\pi d^3} = \frac{H}{2} \quad \text{[Using eq. (1)]}$$

$$\begin{aligned} \text{Total magnetic field, } B &= B_1 + B_2 \\ &= H + \frac{H}{2} \end{aligned}$$

$$= 0.36 + 0.18 = 0.54 \text{ G} \quad \underline{\text{Ans}}$$

5.18) Current in the wire,  $I = 2.5 \text{ A}$

Angle of dip at the given location on earth,  $\delta = 0^\circ$   
Earth's magnetic field,  $H = 0.33 \text{ G} = 0.33 \times 10^{-4} \text{ T}$

The horizontal component of earth's magnetic field is given as:

$$H_H = H \cos \delta$$

$$= 0.33 \times 10^{-4} \times \cos 0^\circ = 0.33 \times 10^{-4} \text{ T}$$

The magnetic field at the neutral point at a distance

R from the cable is given by the relation:

$$H_H = \frac{M_0 I}{2\pi R}$$

where,  $M_0 =$  Permeability of free space  
 $= 4\pi \times 10^{-7} \text{ Tm/A}$

$$\therefore R = \frac{M_0 I}{2\pi H_H}$$

$$= \frac{4\pi \times 10^{-7} \times 2.5}{2\pi \times 0.33 \times 10^{-4}} = 15.15 \times 10^{-3} \text{ m} = 1.51 \text{ cm}$$

Ans