

Addition of Polynomials - (Exercise - 19B)

(i) i) $(3a + 4b + 7c) + (-5a + 3b - 6c) + (4a - 2b - 4c)$
 $= 3a + 4b + 7c - 5a + 3b - 6c + 4a - 2b - 4c$
 $= 3a - 5a + 4a + 4b + 3b - 2b + 7c - 6c - 4c$
 $= 2a + 5b + (-3c)$
 $= 2a + 5b - 3c$ [Row Method]

ii) $(3a + 4b + 7c) + (-5a + 3b - 6c) + (4a - 2b - 4c)$

$$\begin{array}{r} 3a + 4b + 7c \\ -5a + 3b - 6c \\ \hline 4a - 2b - 4c \\ \hline 2a + 5b - 3c \end{array}$$

[Column Method]

EXERCISE - 19(B)

(i) i) $2x^2 + xy - y^2$, $-x^2 + 2xy + 3y^2$ and $3x^2 - 10xy + 4y^2$

$$\begin{array}{r} 2x^2 + xy - y^2 \\ +x^2 + 2xy + 3y^2 \\ \hline 3x^2 - 10xy + 4y^2 \\ \hline 4x^2 - 7xy + 6y^2 \end{array}$$

[Column Method]

ii) $x^2 - x + 1$, $-5x^2 + 2x - 2$ and $3x^2 - 3x + 1$

$$\begin{array}{r} 1x^2 - x + 1 \\ -5x^2 + 2x - 2 \\ \hline 3x^2 - 3x + 1 \\ \hline -x^2 - 2x + 0 \end{array}$$

[Column Method]

iv) $a^2 - ab + bc$, $2ab + bc - 2a^2$ and $-3bc + 3a^2 + ab$

$$\begin{array}{r} a^2 - ab + bc \\ -2a^2 + 2ab + bc \\ \hline 3a^2 + ab - 3bc \\ \hline 2a^2 - 2ab - bc \end{array}$$

[Column method]

v) $4x^2 + 7 - 3x$, $4x - x^2 + 8$ and $-10 + 5x - 2x^2$

$$\begin{array}{r} 4x^2 + 7 - 3x \\ -1x^2 + 8 + 4x \\ -2x^2 - 10 + 5x \\ \hline x^2 - 5 + 6x \end{array}$$

[Column Method]

vi) $3x + 4xy - y^2$, $xy - 4x + 2y^2$ and $3y^2 + xy + 6x$

$$\begin{array}{r} 3x + 4xy - y^2 \\ -4x + xy + 2y^2 \\ + 6x - xy + 3y^2 \\ \hline 5x + 4xy + 4y^2 \end{array}$$

[Column method]

(2) i) $-17x^2 - 2xy + 23y^2$, $-9y^2 + 15x^2 + 7xy$ and $13x^2 + 3y^2 - 4xy$

$$\begin{array}{r} -17x^2 - 2xy + 23y^2 \\ +15x^2 + 7xy - 9y^2 \\ +13x^2 - 4xy + 3y^2 \\ \hline x^2 + xy + 17y^2 \end{array}$$

[Column method]

ii) $-x^2 - 3xy + 3y^2 + 8$, $3x^2 - 5y^2 - 3 + 4xy$
and $-6xy + 2x^2 - 2 + y^2$.

$$\begin{array}{r} -x^2 - 3xy + 3y^2 + 8 \\ 3x^2 + 4xy - 5y^2 - 3 \\ \hline 2x^2 - 6xy + 1y^2 - 2 \\ \hline 4x^2 - 5xy - y^2 + 3 \end{array}$$

[Bokern Method]

iii) $a^3 - 2b^3 + a$, $b^3 - 2a^3 + b$ and $-2b + 2b^3 - 5a + 4a^3$

~~$a^3 - 2b^3 + a$~~

$$(a^3 - 2b^3 + a) + (b^3 - 2a^3 + b) + (-2b + 2b^3 - 5a + 4a^3)$$

$$\begin{aligned} &= a^3 - 2b^3 + a + b^3 - 2a^3 + b - 2b + 2b^3 - 5a + 4a^3 \\ &= (a^3 - 2a^3 + 4a^3) + (-2b^3 + b^3 + 2b^3) + (a - 5a) + (b - 2b) \\ &= 3a^3 + b^3 - 4a - b. \text{ (Ans)} \end{aligned}$$

[Row Method]

Subtraction in Polynomial - (Exercise-19B)

~~$4a + 2b - 3c$, $6a - 5b + 8c$, $-2a + 3b + 2c$~~

④ i) Subtract:

$5a - 3b + 2c$ from $a - 4b - 2c$

$(a - 4b - 2c) - (5a - 3b + 2c)$

$= a - 4b - 2c - 5a + 3b - 2c$

$= a - 5a - 4b + 3b - 2c - 2c$

~~$= a - 5a - 4b + 3b - 2c - 2c$~~

[Row Method]

$= -4a - b - 4c$ (Ans)

i) $5a - 3b + 2c$ from $a - 4b - 2c$

~~Row Method~~

$a - 4b - 2c$

$(-)$ $5a - 3b + 2c$

$= + - -$

$-4a - b - 4c$

[Column method]

Exercise - 19(B)

③ i) $3a - (a + 2b)$

$= 3a - a - 2b$

$= 2a - 2b$ (Ans)

ii) $(5x - 3y) - (x + y)$

$= 5x - 3y - x - y$

$= 5x - x - 3y - y$

$= 4x - 4y$ (Ans)

iii) $(8a + 15b) - (3b - 7a)$

$= 8a + 15b - 3b + 7a$

$= 8a + 7a + 15b - 3b$

$= 15a + 12b$ (Ans)

$$\begin{aligned}
 \text{iv)} & (8x + 7y) - (4y - 3x) \\
 & = 8x + 7y - 4y + 3x \\
 & = 8x + 3x + 7y - 4y \\
 & = 11x + 3y \text{ (Ans)}
 \end{aligned}$$

$$\begin{aligned}
 \text{v)} & 7 - (4a - 5) \\
 & = 7 - 4a + 5 \\
 & = 7 + 5 - 4a \\
 & = 12 - 4a \text{ (Ans)}
 \end{aligned}$$

$$\begin{aligned}
 \text{vi)} & (6y - 13) - (4 - 7y) \\
 & = 6y - 13 - 4 + 7y \\
 & = 6y + 7y - 13 - 4 \\
 & = 13y - 17 \text{ (Ans)}
 \end{aligned}$$

④ Subtract :-

i) $4x - 6y + 3z$ from $12x + 7y - 21z$

$$\begin{aligned}
 & (12x + 7y - 21z) - (4x - 6y + 3z) \\
 & = 12x + 7y - 21z - 4x + 6y - 3z \\
 & = 12x - 4x + 7y + 6y - 21z - 3z \\
 & = 8x + 13y - 24z
 \end{aligned}$$

ii) $5 - a - 4b + 4c$ from $5a - 7b + 2c$

$$\begin{aligned}
 & (5a - 7b + 2c) - (5 - a - 4b + 4c) \\
 & = 5a - 7b + 2c - 5 + a + 4b - 4c \\
 & = 5a + a - 7b + 4b + 2c - 4c - 5 \\
 & = 6a - 3b - 2c - 5
 \end{aligned}$$

i) $-8x - 12y + 17z$ from $x - y - z$.

$$\begin{aligned} & (x - y - z) - (-8x - 12y + 17z) \\ &= x - y - z + 8x + 12y - 17z \\ &= 1x + 8x - y + 12y - z - 17z \\ &= 9x + 11y - 18z \end{aligned}$$

5ii) Take $-ab + bc - ca$ from $bc - ca + ab$

$$\begin{aligned} & (bc - ca + ab) - (-ab + bc - ca) \\ &= bc - ca + ab + ab - bc + ca \\ &= bc - bc - ca + ca + ab + ab \\ &= 2ab \end{aligned}$$

$5x + 6y - 3z$ from $3x + 5y - 4z$

ii) Take $-ab + bc - ca$ from $bc - ca$

$$\begin{aligned} & (3x + 5y - 4z) - (5x + 6y - 3z) \\ &= 3x + 5y - 4z - 5x - 6y + 3z \\ &= 3x - 5x + 5y - 6y - 4z + 3z \\ &= -2x - y - z \end{aligned}$$

iii) Take $-\frac{3}{2}p + q - r$ from $\frac{1}{2}p - \frac{1}{3}q - \frac{3}{2}r$

$$\begin{aligned} & \left(\frac{1}{2}p - \frac{1}{3}q - \frac{3}{2}r \right) - \left(-\frac{3}{2}p + q - r \right) \\ &= \frac{1}{2}p - \frac{1}{3}q - \frac{3}{2}r + \frac{3}{2}p - q + r \\ &= \frac{1}{2}p + \frac{3}{2}p - \frac{1}{3}q - q - \frac{3}{2}r + r \\ &= \frac{4}{2}p - \left(\frac{1}{3}q + \frac{3}{3}q \right) - \left(\frac{3}{2}r - \frac{2}{2}r \right) \\ &= \frac{4}{2}p - \frac{4}{3}q - \frac{1}{2}r \end{aligned}$$

$$= 2p - \frac{4}{3}q - \frac{1}{2}r$$

iv) Take $1 - a + a^2$ from $a^2 + a + 1$

$$\begin{aligned} & (a^2 + a + 1) - (1 - a + a^2) \\ &= a^2 + a + 1 - 1 + a - a^2 \\ &= a^2 - a^2 + a + a + 1 - 1 \\ &= 2a \end{aligned}$$

④ iv) $2ab + cd - ac - 2bd$ from $ab - 2cd + 2ac + bd$

$$\begin{aligned} & (ab - 2cd + 2ac + bd) - (2ab + cd - ac - 2bd) \\ &= ab - 2cd + 2ac + bd - 2ab - cd + ac + 2bd \\ &= 1ab - 2ab - 2cd - 1cd + 2ac + 1ac + 1bd + 2bd \\ &= -ab - 3cd + 3ac + 3bd \end{aligned}$$

⑥ From the sum of $x + y - 2z$ and $2x - y + z$ subtract $x + y + z$.

Solution: $[(x + y - 2z) + (2x - y + z)] - (x + y + z)$

$$\begin{aligned} &= [x + y - 2z + 2x - y + z] - (x + y + z) \\ &= [3x + y - y - 2z + z] - (x + y + z) \\ &= [3x - z] - (x + y + z) \\ &= 3x - z - x - y - z \\ &= 3x - x - y - z - z \\ &= 2x - y - 2z \quad (\text{Ans}) \end{aligned}$$

⑦ From the sum of $3a - 2b + 4c$ and $3b - 2c$ subtract $a - b - c$.

Sol:
$$\begin{aligned} & \{(3a - 2b + 4c) + (3b - 2c)\} - (a - b - c) \\ &= (3a - 2b + 4c + 3b - 2c) - (a - b - c) \\ &= (3a - 2b + 3b + 4c - 2c) - (a - b - c) \\ &= (3a + b + 2c) - (a - b - c) \\ &= 3a + b + 2c - a + b + c \\ &= 3a - a + b + b + 2c + c \\ &= 2a + 2b + 3c \text{ (Ans)} \end{aligned}$$

⑧ Subtract $x - 2y - z$ from the sum of $3x - y + z$ and $x + y - 3z$.

Sol:
$$\begin{aligned} & \{(3x - y + z) + (x + y - 3z)\} - (x - 2y - z) \\ &= \{3x - y + z + x + y - 3z\} - (x - 2y - z) \\ &= (3x + x - y + y + z - 3z) - (x - 2y - z) \\ &= (4x - 2z) - (x - 2y - z) \\ &= 4x - 2z - x + 2y + z \\ &= 4x - x + 2y - 2z + z \\ &= 3x + 2y - z \text{ (Ans)} \end{aligned}$$

⑨ Subtract the sum of $x + y$ and $x - z$ from the sum of $x - 2z$ and $x + y + z$.

Sol:
$$\begin{aligned} & \{(x - 2z) + (x + y + z)\} - \{(x + y) + (x - z)\} \\ &= \{x - 2z + x + y + z\} - \{x + y + x - z\} \\ &= (x + x + y - 2z + z) - (x + x + y - z) \\ &= (2x + y - z) - (2x + y - z) \\ &= 2x + y - z - 2x - y + z \\ &= 2x - 2x + y - y - z + z \\ &= 0 \end{aligned}$$