

Exercise 5 D'

Q1

1) $1x5$ divisible by 3?

Ans $\Rightarrow 1+x+5$ multiple of 3

$$6+x = 0, 3, 6 \text{ or } 9$$

~~$x =$~~

$$\Rightarrow 6+x = 0$$

$$x = 0 - 6 = -6$$

$$\Rightarrow 6+x = 3$$

$$x = 3 - 6 = -3$$

$$\Rightarrow 6+x = 6$$

$$x = 6 - 6 = 0$$

$$\Rightarrow 6+x = 9$$

$$x = 9 - 6 = 3$$

$$\therefore x = -6, -3, 0, 3, 6, 9$$

Since x is a digit.

$$x = 0, 3, 6, 9$$

Q2) $31x5$ divisible by 3?

$3+1+x+5$ is a multiple of 3

$$9+x = 0, 3, 6 \text{ or } 9$$

$$\Rightarrow 9+x = 0$$

$$x = 0 - 9 = -9$$

$$\Rightarrow 9+x = 3$$

$$x = 3 - 9 = -6$$

$$\Rightarrow 9+x = 6$$

$$x = 6 - 9 = -3$$

$$\Rightarrow 9+x = 9$$

$$x = 9 - 9 = 0$$

$$\therefore x = -9, -6, -3, 0, 3, 6, 9$$

Since x is a digit

$$x = 0, 3, 6 \text{ or } 9$$

3rd $28x6$ is multiple of 3
 $2+8+x+6$ is a multiple of 3
 $= 16+x = 0, 3, 6, 9, 12, 15, 18, 21$

$\Rightarrow 16+x = 0$

$x = 0-16 = (-16)$

$\Rightarrow 16+x = 3$

$x = 3-16 = (-13)$

$\Rightarrow 16+x = 6$

$x = 6-16 = (-10)$

$\Rightarrow 16+x = 9$

$x = 9-16 = (-7)$

$\Rightarrow 16+x = 12$

$x = 12-16 = (-4)$

$\Rightarrow 16+x = 15$

$x = 15-16 = (-1)$

$\Rightarrow 16+x = 18$

$x = 18-16 = 2$

$\Rightarrow 16+x = 21$

$x = 21-16 = 5$

$\therefore x = 13, -10, -7, -4$

Since x is a digit

$\therefore x = 2, 6, 9$

4th $24x$ divisible by 6

Ans $\Rightarrow 24x$ is divisible by 6, if it is divisible by 2 and 3 both

$24x$ is divisible by 3

$2+4+x$ is a multiple of 3

$6+x = 0, 3, 6, 9, 12$

$\Rightarrow 6+x = 0$

$x = -6$

$\Rightarrow 6+x = 3$

$x = -3$

$$\Rightarrow 6+x=6$$
$$x=6-6=0$$

$$\Rightarrow 6+x=9$$
$$x=9-6=3$$

$$\Rightarrow 6+x=12$$
$$x=12-6=6$$

$$\therefore x = -6, -3, 0, 3, 6 \dots \dots \dots (i)$$

Since x is digit

$$\therefore x = 0, 3, 6, 9, 12$$

~~2~~ $24x$ is divisible by 2
 $2+4+x$ is a multiple of 2

$$6+x = 0, 2, 4, 6, 8, 10$$

$$6+x=0$$

$$x=-6$$

$$6+x=2$$

$$x=-4$$

$$6+x=4$$

$$x=-2$$

$$6+x=6$$

$$x=6-6=0$$

$$6+x=8$$

$$x=8-6=2$$

$$6+x=10$$

$$x=10-6=4$$

$$\therefore x = -6, -4, -2, 0, 2, 4$$

Since x is a digit

$$\therefore x = 0, 2, 4, 6, 8$$

$$\therefore x = 0, 6 \text{ which is divisible by 6.}$$

54. $3x26$ a multiple of 6

Ans $\Rightarrow 3x26$ is a multiple of 2 and 3 both.

$\Rightarrow 3x26$ is a multiple of 2 as it has even number 6 at its unit place.

$\Rightarrow 3x26$ is a multiple of 3

$\Rightarrow 3+x+2+6$ is a multiple of 3

~~$\Rightarrow 11+x$ is a multiple of 3~~

$\Rightarrow 11+x = 0, 3, 6, 9, 12, 15, 18, 21$

$\Rightarrow 11+x = 0$

$$x = -11$$

$\Rightarrow 11+x = 3$

$$x = -8$$

$\Rightarrow 11+x = 6$

$$x = 6 - 11 = -5$$

$\Rightarrow 11+x = 9$

$$x = -2$$

$\Rightarrow 11+x = 12$

$$x = 1$$

$\Rightarrow 11+x = 15$

$$x = 4$$

$\Rightarrow 11+x = 18$

$$x = 7$$

$\Rightarrow 11+x = 21$

$$x = 10$$

$\therefore x = -11, -8, -5, -2, 1, 4, 7, 10$

Since x is a digit

$\therefore x = 1, 4, 7$

64) $42x8$ is divisible by 4

Ans) Then the number $x8$ must be divisible by 4
 $x8 = 10x + 8$

$x8 = 8, 18, 28, 38, 48, 58, 68, 78, 88, 98$

$x8$ only 8, 28, 48, 68, 88 are divisible by 4.
 So the value of x are 0, 2, 4, 6, 8

7) $9142x$ is a multiple of 4.

Ans) Then the number $2x$ must be a multiple of 4
 $2x = \text{multiples of } 4$

$2x = 20, 24, 28$

$\therefore x = 0, 4 \text{ or } 8$

8) $7x34$ divisible by 9.

Ans) $7+x+3+4$ is a multiple of 9

$14+x = 0, 9, 18, 27$

$14+x=0$

$x = -14$

$14+x=9$

$x = -5$

$14+x=18$

$x = 4$

$14+x=27$

$x = 13$

$\therefore x = -14, -5, 4, 13$

\therefore Since x is a digit

$\therefore x = 4$

9) $5x555$ a multiple of 9?

Ans) $5+x+5+5+5$ is a multiple of 9.

$20+x = 0, 9, 18, 27, 36$

$20+x=0$

$x = -20$

$20+x=9$

$x = 9-20 = (-11)$

$$20 + x = 18$$

$$x = -2$$

$$20 + x = 27$$

$$x = 7$$

$$20 + x = 36$$

$$x = 16$$

$$\therefore x = -2, -11, -2, 7, 16$$

Since x is a digit

$$\therefore x = 7 \text{ or } 16$$

10) $3x2$ divisible by 11

Sum of the digit in even place = x

Sum of the digit in odd place = $3 + 2 = 5$

Difference in the sum of digits in even place and sum of digits in odd place

$$= x - 5$$

$2x3x2$ is a multiple of 11

$\Rightarrow x - 5$ must be multiple of 11

$$\Rightarrow x - 5 = 0, 11, 22$$

$$\Rightarrow x - 5 = 0$$

$$x = 5$$

$$\neq x - 5 = 11$$

$$x = 16$$

$$\neq x - 5 = 22$$

$$x = 17$$

$$\therefore x = 5, 16, 17$$

$$\therefore x = 5$$

11) $5x2$ a multiple of 11

Sum of digit in even place = x

Sum of digit in odd place = $5 + 2 = 7$

Difference in the sum of the digits in even place and sum of digit in odd place

$$= x - 7$$

$5x2$ is a multiple of 11

$x-7$ is a multiple of 11

$x-7 = 0, 11, 22, 33, 44, \dots$

$$x-7 = 0$$

$$x = 7$$

$$x-7 = 11$$

$$x = 18$$

$$x-7 = 22$$

$$x = 19$$

$$x-7 = 33$$

$$x = 40$$

$$x-7 = 44$$

$$x = 51$$

$\therefore x = 7, 18, 19, 40, 51, \dots$

$\therefore x = 7$

- x - x - x - x -