

28.6.21

LCM

Revision Exercise

Prime factor method

20) i) 72, 80, 252

$$72 = 2 \times 2 \times 2 \times 3 \times 3 = 2^3 \times 3^2$$

$$80 = 2 \times 2 \times 2 \times 2 \times 5 = 2^4 \times 5^1$$

$$252 = 2 \times 2 \times 3 \times 3 \times 7 = 2^2 \times 3^2 \times 7^1$$

$$\text{LCM} = 2^4 \times 3^2 \times 5 \times 7$$

$$= 2 \times 2 \times 2 \times 2 \times 3 \times 3 \times 5 \times 7 = 5040$$

20) ii) 48, 66, 120

$$48 = 2 \times 2 \times 2 \times 2 \times 3 = 2^4 \times 3$$

$$66 = 2 \times 3 \times 11 = 2 \times 3 \times 11$$

$$120 = 2 \times 2 \times 2 \times 3 \times 5 = 2^3 \times 3 \times 5$$

$$\text{LCM} = 2^4 \times 3 \times 5 \times 11$$

$$= 2 \times 2 \times 2 \times 2 \times 3 \times 5 \times 11 = 2640$$

6) i) $\begin{array}{r} 28, 42 \\ 7 \end{array}$ $\begin{array}{r} 14, 21 \\ 7 \end{array}$

2, 3

$$\text{LCM} = 2 \times 7 \times 2 \times 3 = 84$$

So, the smallest number that is completely divisible by 28 and 42 is 84.

(ii)

$$\begin{array}{r} 1 \\ 28 \overline{) 42} \\ \underline{28} \quad 2 \\ 14 \overline{) 28} \\ \underline{28} \\ 00 \end{array}$$

$$\text{HCF} = 14$$

So, the largest number that can divide 28 and 42 completely is 14.

$$8) \text{ HCF} = 2 \times 3 \times 3 = 18$$

Product of the two no.

$$= \text{HCF} \times \text{LCM}$$

$$108 \times 450 = 18 \times \text{LCM}$$

$$\text{LCM} = \frac{108 \times 450}{18} = \frac{4960}{18}$$

$$\text{LCM} = \frac{108 \times 450}{18} = 49600 \div 18 = 2700$$

So, the HCF is 18 and the LCM is 2700.

$$1) (i) 108, 288, 420$$

$$2 \mid 108, 288, 420$$

$$2 \mid 54, 144, 210$$

$$3 \mid 27, 72, 105$$

$$9, 24, 35$$

$$\text{HCF} = 2 \times 2 \times 3 = 12$$

$$(ii) 36, 54, 138$$

$$2 \mid 36, 54, 138$$

$$3 \mid 18, 27, 69$$

$$6, 9, 23$$

$$\text{HCF} = 2 \times 3 = 6$$

3) (i) True. (2 and 5 are two prime numbers and their HCF is 1)

(ii) True. (8 and 9 are two co-prime numbers and their HCF is 1)

(iii) True. (5 and 7 are two prime numbers and their LCM is 35)

(iv) True. (4 and 5 are two co-prime numbers and their LCM is 20.)

Q4) Product of two numbers = 12096

HCF = 36

LCM = ?

Product of the two numbers = HCF x LCM

12096 = 36 x LCM

LCM = 12096 ÷ 36 = 336

So, the LCM is 336.

Q5) Product HCF x LCM = 1152

One no. = 48

Other no. = ?

Product of the two numbers = HCF x LCM

48 x Other no. = 1152

Other no. = 1152 ÷ 48 = 24

So, the other number is 24.

$$\begin{array}{r}
 2 \overline{) 140, 168} \\
 2 \overline{) 70, 84} \\
 7 \overline{) 35, 42} \\
 \hline
 5, 6
 \end{array}$$

LCM = 2 x 2 x 7 x 5 x 6 = 840

LCM = 840

Product of the two no. = 140 x 168 = 23520

HCF = ?

Product of the two no. = HCF x LCM

23520 = 840 x HCF

HCF = 23520 ÷ 840 = 28

So, the LCM is 840 and the HCF is 28.