

Moving Charges and Magnetism

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1. Number of turns = 100
radius = 8.0 cm
current = 0.40 A

Magnetic field of B = ?

$$|B| = \frac{\mu_0 \times 2\pi n I}{4\pi r}$$

$$= \frac{4\pi \times 10^{-7} \times 2\pi \times 100 \times 0.4}{4\pi \times 0.08}$$

$$= 3.14 \times 10^{-4} \text{ T}$$

2. Current = 35 A

20 cm from the point = 0.2 m

B = ?

$$B = \frac{\mu_0 I}{2\pi r}$$

$$= \frac{4\pi \times 10^{-7} \times 35}{2\pi \times 0.2}$$

$$= 3.5 \times 10^{-5}$$

4.3.

$I = 50 \text{ A}$

$r = 2.5 \text{ m}$

$$B = \frac{\mu_0 I}{2\pi r} = \frac{4\pi \times 10^{-7} \times 50 \times 10}{2\pi \times 2.5}$$

~~$= 4 \times 10^{-6} \text{ T}$~~ $4.0 \times 10^{-6} \text{ T}$

4.4.

$I = 90 \text{ A}$

~~$r = 1.5 \text{ m}$~~

$$B = \frac{\mu_0 I}{2\pi r} = \frac{4\pi \times 10^{-7} \times 90 \times 10}{2\pi \times 1.5}$$

$= 12 \times 10^{-6} \text{ T}$

4.5

$I = 8 \text{ A}$

$\theta = 30^\circ$

$B = 0.15 \text{ T}$

$F = BI \sin \theta$

~~$F = BI \sin \theta$~~

$\rightarrow 0.15 \times 8 \times \sin 30^\circ$

$$= \frac{4 \times 15 \times 3}{25 \times 5} = \frac{3}{5} = 0.6 \text{ N m}^{-1}$$

4.6

$$L = 3 \text{ cm} = 0.03 \text{ m}$$

$$I = 10 \text{ A}$$

$$B = 0.27 \text{ T}$$

$$F = ?$$

~~$$F = BIL$$~~

$$F = BI \sin \theta \quad (\theta = 90^\circ)$$

$$F = \frac{27}{100} \times 10 \times \frac{3}{100} \sin 90^\circ$$

$$\Rightarrow \frac{27}{100} \times 10 \times \frac{3}{100} \times 1$$

$$\Rightarrow 81 \times 10^3$$

$$= 8.1 \times 10^2 \text{ N}$$

4.7

$$I_A = 8.0 \text{ A}$$

$$I_B = 5.0 \text{ A}$$

$$r = 4.0 \text{ cm} = 0.04 \text{ m}$$

$$\text{length of section of wire A} = L = 10 \text{ cm} = 0.1 \text{ m}$$

$$\theta = 180^\circ \quad \theta = 180^\circ$$

$$B = \frac{\mu_0 2 I_1 I_2 L}{4 \pi r}$$

$$= \frac{4\pi \times 10^{-7} \times 2 \times 8 \times 5 \times 0.1}{4\pi \times 0.04}$$

$$= 2 \times 10^{-5} \text{ N}$$

4.8 length of the solenoid (L) = 80 cm = 0.8 m
 Total number of turns (N) = 5 × 400 = 2000
 Diameter of the solenoid (D) = 1.8 cm = 0.018 m
 Current carried by solenoid I = 8.0 A
 Magnitude of magnetic field

$$B = \frac{\mu_0 N I}{L}$$

$$= \frac{4\pi \times 10^{-7} \times 2000 \times 8}{0.8}$$

$$= 8\pi \times 10^{-3} \text{ T}$$

$$= \frac{8 \times 22 \times 10^{-3}}{7}$$

$$= \frac{56 \times 22 \times 10^{-3}}{7}$$

$$= \frac{176 \times 10^{-3}}{7}$$

$$= 25.14 \times 10^{-3} \text{ T}$$

$$= 25.14 \text{ mT}$$

$$= 2.514 \times 10^{-2} \text{ T}$$

4.9 $L = 10 \text{ cm} = 0.1 \text{ m}$

$I = 12 \text{ A}$

$n = 20$

$\theta = 30^\circ$

$B = 0.80 \text{ T}$

$\tau = ?$

$$\tau = n B I A \sin \theta$$

$$220 \times 0.8 \times 12 \times 0.01 \times \sin 30^\circ \quad (A = 0.1 \times 0.1 = 0.01 \text{ m}^2)$$

$$\Rightarrow 20 \times 0.8 \times 12 \times 0.01 \times \frac{1}{2}$$

$$\Rightarrow \frac{8 \times 12 \times 1}{100}$$

$$= \frac{96}{100} = 0.96 \text{ Am}$$

4.10 For M_1

$$R_1 = 10 \Omega$$

$$N_1 = 30$$

$$A_1 = 3.6 \times 10^{-3} \text{ m}^2$$

$$B_1 = 0.25 \text{ T}$$

$$K_1 = K$$

For M_2

$$R_2 = 14 \Omega$$

$$N_2 = 42$$

$$A_2 = 1.8 \times 10^{-3} \text{ m}^2$$

$$B_2 = 0.50 \text{ T}$$

$$K_2 = K$$

a) Current sensitivity of M_1

$$I_1 = \frac{N_1 B_1 A_1}{K_1}$$

Current sensitivity of M_2

$$I_2 = \frac{N_2 B_2 A_2}{K_2}$$

$$\text{Ratio} = \frac{42 \times 0.5 \times 1.8 \times 10^{-3} \times K}{30 \times 0.25 \times 3.6 \times 10^{-3} \times K} = 1.4$$

Voltage sensitivity of M_1 is

$$V_1 = \frac{N_1 B_1 A_1}{K_1 R_1}$$

Voltage sensitivity of M_2

$$V_2 = \frac{N_2 B_2 A_2}{K_2 R_2}$$

$$\text{Ratio} = \frac{42 \times 0.5 \times 1.8 \times 10^{-3} \times 10 \times K}{30 \times 0.25 \times 3.6 \times 10^{-3} \times 14 \times K}$$

$$= 1$$

4.11 $B = 6.5 \times 10^4 \text{ T}$

$v = 4.8 \times 10^6 \text{ m/s}$

radius = ?

~~Centrifugal force~~

$$R = \frac{mv}{qB} = \frac{9.1 \times 10^{-31} \times 4.8 \times 10^6}{1.5 \times 10^{-19} \times 6.5 \times 10^{-4}}$$

$$= \frac{91 \times 10^{-30} \times 4.8 \times 10^4}{1.5 \times 10^{-19} \times 6.5 \times 10^{-4}}$$

$$= \frac{91 \times 10^8 \times 48 \times 10^4}{1.5 \times 6.5}$$

$$= \frac{91 \times 48 \times 10^4}{15 \times 65 \times 10^2} = 4.48 \times 10^2$$

$$4.12 \quad f = \frac{qB}{2\pi m}$$

$$= \frac{1.5 \times 10^{-19} \times 8.5 \times 10^{-4}}{2\pi \times 9.1 \times 10^{-31}}$$

$$4.13 \quad N = 30$$

$$r = 8 \text{ cm} = 0.08 \text{ m} \quad \text{Area} = \pi r^2 = 0.02 \text{ m}^2$$

$$I = 6 \text{ A}$$

$$B = 1.0 \text{ T}$$

$$\theta = 60^\circ$$

$$\tau = NBIA \sin \theta$$

$$= 30 \times 6 \times 1 \times 0.02 \times \sin 60^\circ$$

$$= 3.1 \text{ Nm}$$

b) No θ as it depends upon area of the coil hence the answer would not change

4.14

coil X

$$r_1 = 16 \text{ cm} = 0.16 \text{ m}$$

$$n_1 = 20$$

$$I_1 = 16 \text{ A}$$

X = anticlockwise

coil Y

$$r_2 = 10 \text{ cm} = 0.1 \text{ m}$$

$$n_2 = 25$$

$$I_2 = 18 \text{ A}$$

Y = clockwise

$$B = \frac{\mu_0 n I}{2r}$$

B coil X

$$B_1 = \frac{4\pi \times 10^{-7} \times 20 \times 16}{2 \times 0.16}$$

$$= 4\pi \times 10^{-4} \text{ T}$$

(Towards east)

Coil Y

$$B_2 = \frac{\mu_0 n_2 I_2}{2r_2}$$

$$B_2 = \frac{4\pi \times 10^{-7} \times 25 \times 18}{2 \times 0.10}$$

$$= 9\pi \times 10^{-4} \text{ T}$$

(Towards west)

Hence Net magnetic field =

$$B = B_2 - B_1$$

$$= 9\pi \times 10^{-4} - 4\pi \times 10^{-4}$$

$$= 5\pi \times 10^{-4} \text{ T}$$

$$= 1.57 \times 10^{-3} \text{ T}$$

4.15) $B = 100 \text{ G} = 100 \times 10^{-9} \text{ T}$

$$n = 1000 \text{ turns}$$

$$I = 15 \text{ A}$$

$$B = \mu_0 n I$$

$$\therefore n I = \frac{B}{\mu_0} = \frac{100 \times 10^{-9}}{4\pi \times 10^{-7}} = 8000 \text{ A/m}$$

16a) \bullet at center $\rightarrow \frac{\mu_0 I}{2R} < \frac{\mu_0 I \cdot R^2}{2(R^2 + r^2)^{3/2}}$

- b) Radius = r
 num of turns = N
 both equal current distance = r
 at mid point: $B_1 + B_2$

$$B = 0.72 \frac{\mu_0 \cdot I \cdot N}{r}$$

- 4.17) Inner radius $r = 25 \text{ cm} = 0.25 \text{ m}$
 Outer radius $R = 26 \text{ cm} = 0.26 \text{ m}$
 $N = 3500$
 $I = 11 \text{ A}$

a) Magnetic field outside the toroid is zero.

b) $B = \frac{\mu_0 N I}{l}$

where l is length of toroid

$$l = 2\pi \left[\frac{r_1 + r_2}{2} \right]$$

$$= \pi (0.25 + 0.26)$$

$$= 0.51\pi$$

$$\therefore B = \frac{4\pi \times 10^{-7} \times 3500 \times 11}{0.51\pi} = 3.0 \times 10^{-2} \text{ T}$$

c) Magnetic field in empty space surrounding by toroid is zero

~~4.19~~

4.19 a) Charge particle moves in straight line path

b) Final speed = Initial speed

c) If electric field is equal and opposite to magnetic field then charge particle moves unaffected

4.20 $B = 0.75 \text{ T}$

$V = 15 \text{ kV} = 15 \times 10^3 \text{ V}$

$E = 9 \times 10^5 \text{ Vm}$

Mass of electron = m

charge of electron = $-e$

velocity " " = v

Kinetic energy of electron = eV

$$eV = \frac{1}{2}mv^2$$

$$\therefore \frac{e}{m} = \frac{v^2}{2V} \quad \text{--- (1)}$$

$eE = e v B$ (Particle remains unaffected)

$v = \frac{E}{B}$ - (2)

Putting (2) in (1) we get

$\frac{e}{m} = \frac{1}{2} \left(\frac{E}{B} \right)^2 = \frac{E^2}{2 v B^2}$

$= \frac{(9.0 \times 10^5)^2}{2 \times 15000 \times (0.75)^2} = 4.8 \times 10^4 \text{ C/Kg}$

4.21 a) $l = 0.45 \text{ m}$

$m = 60 \text{ g} = 60 \times 10^{-3} \text{ kg}$

$g = 9.8 \text{ m/s}^2$

$I = 5 \text{ A}$

~~BIL~~ $BIL = mg$

$B = \frac{mg}{IL}$

$= \frac{60 \times 10^{-3} \times 9.8}{5 \times 0.45} = 0.26 \text{ T}$

4.22) $I = 300 \text{ A}$
 $r = 1.5 \text{ cm} = 0.015 \text{ m}$
 $L = 70 \text{ cm} = 0.7 \text{ m}$

$$F = \frac{\mu_0 I^2 L}{2\pi r}$$

$$F = \frac{4\pi \times 10^{-7} \times (300)^2 \times 0.7}{2\pi \times 0.015} = 1.2 \text{ N/m}$$

~~4.23~~

4.24 $B = 3000 \text{ G} = 3000 \times 10^{-4} \text{ T} = 0.3 \text{ T}$
 $I = 12 \text{ A}$
 $b = 5 \text{ cm}$
 $L = 10 \text{ cm}$
 $A = L \times b = 50 \text{ cm}^2 = 50 \times 10^{-4} \text{ m}^2$

a) $\tau = 12 \times (50 \times 10^{-4}) \hat{i} \times 0.3 \hat{k}$
 $= -1.8 \times 10^{-2} \hat{j} \text{ Nm}$

b) ~~The answer is~~

⊙

4.25

$$n = 20$$

$$r = 10 \text{ cm} = 0.1 \text{ m}$$

$$B = 0.10 \text{ T}$$

$$I = 5.0 \text{ A}$$

a) The total torque on the coil is zero

b) Total force on the coil is zero

d)

c) cross sectional Area $A = 10^{-9} \text{ m}^2$

Number of free electron per cubic meter

$$N = 10^{29} / \text{m}^3$$

Charge of electron $e = 1.6 \times 10^{-19} \text{ C}$

$$F = BeV_d \text{ (} V_d \text{ is drift velocity)}$$

$$V_d = \frac{I}{NeA}$$

$$\therefore F = \frac{BeI}{NeA}$$

$$= \frac{0.10 \times 5.0}{10^{29} \times 10^{-5}} = 5.0 \times 10^{-23} \text{ N}$$

4.26

$$G = 12 \Omega$$

$$I_g = 3 \text{ mA} = 3 \times 10^{-2} \text{ A}$$

$$V = 18 \text{ V}$$

$$R = \frac{V}{I_g} - G = \frac{18}{3 \times 10^{-2}} - 12 = 6000 - 12 = 5988 \Omega$$

4.28

Resistance of galvanometer $G = 15 \Omega$

$$I_g = 4 \text{ mA} = 4 \times 10^{-3} \text{ A}$$

Range of ammeter is ∞ which needs to be converted to ~~10 A~~ 6 A

$$\therefore I = 6 \text{ A}$$

$$S = \frac{I_g G}{I - I_g}$$

$$= \frac{4 \times 10^{-3} \times 15}{6 - 4 \times 10^{-3}}$$

$$\Rightarrow \frac{60 \times 10^{-2}}{6 - 0.004} = \frac{0.06}{5.996} = 0.01 \Omega$$

$$= 10 \text{ m}\Omega$$