

Q1. (i) P(2, 3) and Q(4, 1).

$$x_1 = 2, y_1 = 3, x_2 = 4 \text{ and } y_2 = 1$$

$$\therefore \text{Dist. } PQ = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} \\ = \sqrt{(4 - 2)^2 + (1 - 3)^2}$$

$$= \sqrt{(2)^2 + (-2)^2} = \sqrt{4 + 4}$$

$$= \sqrt{8} = 2\sqrt{2} \text{ units.}$$

(ii) P(-5, 7) and Q(-1, 3).

$$x_1 = -5$$

$$y_1 = 7$$

$$x_2 = -1$$

$$y_2 = 3$$

$$\therefore \text{Dist. } PQ = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$= \sqrt{(-1 + 5)^2 + (3 - 7)^2}$$

$$= \sqrt{(4)^2 + (-4)^2} = \sqrt{16 + 16}$$

$$= \sqrt{32} = 4\sqrt{2} \text{ units.}$$

(iii) P(a, b).

Q(-a, -b).

$$x_1 = a$$

$$y_1 = b$$

$$x_2 = -a$$

$$y_2 = -b$$

$$\therefore \text{Dist. } PQ = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$= \sqrt{(-a - a)^2 + (-b - b)^2}$$

$$= \sqrt{(-2a)^2 + (-2b)^2}$$

$$= \sqrt{2\sqrt{a^2 + b^2}} \text{ units.}$$

Q2. A(0, 0).

B(36, 15).

$$AB = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} = \sqrt{(36 - 0)^2 + (15 - 0)^2}$$

$$= \sqrt{1296 + 225} = \sqrt{1521} = 39 \text{ units.}$$

Q3. $A(1, 5)$.
 $B(2, 3)$.
 $C(-2, -11)$.

$$AB = \sqrt{(2-1)^2 + (3-5)^2} = \sqrt{(1)^2 + (-2)^2}$$
$$= \sqrt{1+4} = \sqrt{5}$$

$$BC = \sqrt{(2-2)^2 + (-11-3)^2} = \sqrt{(-4)^2 + (-14)^2}$$
$$= \sqrt{16+196} = \sqrt{212} = 2\sqrt{53}$$

$$AC = \sqrt{(-2-1)^2 + (-11-5)^2} = \sqrt{(-3)^2 + (-16)^2}$$
$$= \sqrt{9+256} = \sqrt{265}$$

Since $AB + BC \neq AC$.

Q4. $A(5, -2)$.
 $B(6, 4)$.
 $C(7, -2)$.

$$AB = \sqrt{(6-5)^2 + (4+2)^2} = \sqrt{1+36} = \sqrt{37}$$

$$BC = \sqrt{(7-6)^2 + (-2-4)^2} = \sqrt{1+36} = \sqrt{37}$$

$$AC = \sqrt{(7-5)^2 + (-2+2)^2} = \sqrt{4+0} = \sqrt{4} = 2$$