

Hw Ex-8(B)

① i) 16 and 35

$$F_{16} = 1, 2, 4, 8, 16$$

$$F_{35} = 1, 5, 7, 35$$

$$CF = 1$$

$$HCF = 1$$

ii) 25 and 20

$$F_{25} = 1, 5, 25$$

$$F_{20} = 1, 2, 4, 5, 10, 20$$

$$CF = 1$$

$$HCF = 1$$

iii) 27 & 75

$$F_{27} = 1, 3, 9, 27$$

$$F_{75} = 1, 3, 5, 15, 25, 75$$

$$HCF = 3$$

iv) 8, 12 & 18

$$F_8 = 1, 2, 4, 8$$

$$F_{12} = 1, 2, 3, 4, 6, 12$$

$$F_{18} = 1, 2, 3, 6, 18$$

$$HCF = 2$$

v) 24, 36, 45, 60

$$F_{24} = 1, 2, 3, 4, 6, 8, 12, 24$$

$$F_{36} = 1, 2, 3, 4, 6, 9, 12, 18, 36$$

$$F_{45} = 1, 3, 5, 9, 15, 45$$

$$F_{60} = 1, 2, 3, 4, 5, 6, 10, 12, 15, 20, 30, 60$$

$$HCF = 3$$

②) 5 and 8

$$\begin{array}{r} 1 \overline{) 5} \\ \underline{5} \\ 0 \end{array}$$

$$\begin{array}{r} 2 \overline{) 8} \\ \underline{4} \\ 4 \\ \underline{4} \\ 0 \end{array}$$

$$5 = 1 \times 5$$

$$8 = 2 \times 2 \times 2 \times 1$$

$$\text{HCF} = 1$$

ii) 24 and 49

$$\begin{array}{r} 2 \overline{) 24} \\ \underline{2} \\ 12 \\ \underline{2} \\ 6 \\ \underline{2} \\ 3 \\ \underline{1} \\ 3 \end{array}$$

$$\begin{array}{r} 7 \overline{) 49} \\ \underline{7} \\ 7 \\ \underline{7} \\ 0 \end{array}$$

$$24 = 3 \times 2 \times 2 \times 2 \times 1$$

$$49 = 7 \times 7 \times 1$$

$$\text{HCF} = 1$$

iii) 40, 60 and 80

$$\begin{array}{r} 2 \overline{) 40} \\ \underline{2} \\ 20 \\ \underline{2} \\ 10 \\ \underline{1} \\ 5 \\ \underline{5} \\ 0 \end{array}$$

$$\begin{array}{r} 2 \overline{) 60} \\ \underline{2} \\ 30 \\ \underline{3} \\ 10 \\ \underline{2} \\ 5 \\ \underline{1} \\ 5 \end{array}$$

$$\begin{array}{r} 2 \overline{) 80} \\ \underline{2} \\ 40 \\ \underline{2} \\ 20 \\ \underline{2} \\ 10 \\ \underline{1} \\ 5 \\ \underline{5} \\ 0 \end{array}$$

$$40 = 2 \times 2 \times 2 \times 1 \times 5$$

$$60 = 2 \times 2 \times 3 \times 5 \times 1$$

$$80 = 2 \times 2 \times 2 \times 2 \times 5 \times 1$$

$$\text{HCF} = 2 \times 2 \times 5 = 20$$

(IV) 48, 84, 88

$$\begin{array}{r}
 2 \overline{) 48} \\
 \underline{2 \overline{) 24}} \\
 2 \overline{) 12} \\
 \underline{2 \overline{) 6}} \\
 1 \overline{) 3} \\
 \underline{ 3} \\
 0
 \end{array}$$

$$\begin{array}{r}
 2 \overline{) 84} \\
 \underline{2 \overline{) 42}} \\
 3 \overline{) 21} \\
 \underline{1 \overline{) 7}} \\
 7 \\
 7
 \end{array}$$

$$\begin{array}{r}
 2 \overline{) 88} \\
 \underline{2 \overline{) 44}} \\
 2 \overline{) 22} \\
 \underline{1 \overline{) 11}} \\
 11 \\
 11
 \end{array}$$

$$48 = 2 \times 2 \times 2 \times 2 \times 3 \times 1$$

$$84 = 2 \times 2 \times 3 \times 1 \times 7$$

$$88 = 2 \times 2 \times 2 \times 1 \times 11$$

$$\text{H.C.F} = 2 \times 2 = 4$$

(V) 12, 16, 28

$$\begin{array}{r}
 2 \overline{) 12} \\
 \underline{2 \overline{) 6}} \\
 3 \overline{) 3} \\
 \underline{ 3} \\
 0
 \end{array}$$

$$\begin{array}{r}
 2 \overline{) 16} \\
 \underline{2 \overline{) 8}} \\
 2 \overline{) 4} \\
 \underline{2 \overline{) 2}} \\
 2 \\
 2
 \end{array}$$

$$\begin{array}{r}
 2 \overline{) 28} \\
 \underline{2 \overline{) 14}} \\
 7 \overline{) 7} \\
 \underline{ 7} \\
 0
 \end{array}$$

$$12 = 2 \times 2 \times 3 \times 1$$

$$16 = 2 \times 2 \times 2 \times 2 \times 1$$

$$28 = 2 \times 2 \times 7 \times 1$$

$$\text{HCF} = 2 \times 2 = 4$$

③ Find HCF using division method

16 and 24

$$\begin{array}{r}
 16 \overline{) 24} \\
 \underline{-16} \quad 8 \\
 8 \overline{) 16} \\
 \underline{-16} \\
 0
 \end{array}$$

$$\text{H.C.F} = 8$$

(ii) 18 and 30

$$\begin{array}{r}
 1 \\
 18 \overline{) 30} \\
 \underline{-18} \\
 12 \\
 12 \overline{) 18} \\
 \underline{-12} \\
 6 \\
 6 \overline{) 12} \\
 \underline{-12} \\
 0
 \end{array}$$

H.C.F = 6

(iii) 7, 14, 24

$$\begin{array}{r}
 2 \\
 7 \overline{) 14} \\
 \underline{-14} \\
 0
 \end{array}
 \qquad
 \begin{array}{r}
 3 \\
 7 \overline{) 24} \\
 \underline{-21} \\
 3 \\
 3 \overline{) 7} \\
 \underline{-6} \\
 1 \\
 1 \overline{) 3} \\
 \underline{-3} \\
 0
 \end{array}$$

H.C.F = 1

(iv) 70, 80, 120 and 150

$$\begin{array}{r}
 1 \\
 70 \overline{) 80} \\
 \underline{-70} \\
 10 \overline{) 70} \\
 \underline{-70} \\
 0
 \end{array}
 \qquad
 \begin{array}{r}
 1 \\
 120 \overline{) 150} \\
 \underline{120} \\
 30 \overline{) 120} \\
 \underline{-120} \\
 0
 \end{array}$$

$$\begin{array}{r}
 3 \\
 10 \overline{) 30} \\
 \underline{-30} \\
 0
 \end{array}$$

H.C.F = 10

(v) $32, 56, 48$

$$\begin{array}{r} 32 \overline{) 56} \\ \underline{-32} \\ 24 \end{array} \quad \begin{array}{r} 1 \\ 32 \\ \underline{-24} \\ 8 \end{array} \quad \begin{array}{r} 3 \\ 24 \\ \underline{-24} \\ 0 \end{array}$$

$8, 46, 40$

$$\begin{array}{r} 8 \overline{) 46} \\ \underline{-40} \\ 6 \end{array} \quad \begin{array}{r} 1 \\ 8 \\ \underline{-6} \\ 2 \end{array} \quad \begin{array}{r} 3 \\ 6 \\ \underline{-6} \\ 0 \end{array}$$

H.C.F = 2

(*) Find H.C.F by using own method

(a) $5, 45, 75, 135$

$$\begin{array}{r} 5 \overline{) 45, 75, 135} \\ 3 \overline{) 9, 15, 27} \\ 3, 5, 9 \\ \text{H.C.F} = 5 \times 3 = 15 \end{array}$$

(ii) $2, 48, 36, 96$

$$\begin{array}{r} 2 \overline{) 48, 36, 96} \\ 2 \overline{) 24, 18, 48} \\ 3 \overline{) 12, 9, 24} \\ 4, 3, 8 \\ \text{H.C.F} = 2 \times 2 \times 3 = 12 \end{array}$$

(iii) $3, 66, 33, 132$

$$\begin{array}{r} 3 \overline{) 66, 33, 132} \\ 11 \overline{) 22, 11, 44} \\ 2, 1, 4 \\ \text{H.C.F} = 11 \times 3 = 33 \end{array}$$

(iv) $2, 24, 36, 60, 132$

$$\begin{array}{r} 2 \overline{) 24, 36, 60, 132} \\ 2 \overline{) 12, 18, 30, 66} \\ 3 \overline{) 6, 9, 15, 33} \\ 2, 3, 5, 11 \\ \text{H.C.F} = 2 \times 2 \times 3 = 12 \end{array}$$

(iv) 30, 60, 90, 105

$$\begin{array}{l} 5 \overline{) 30, 60, 90, 105} \\ 3 \overline{) 6, 12, 18, 21} \\ 2, 4, 6, 7 \end{array} \quad \text{H.C.F} = 5 \times 3 = 15$$

5) The greatest number that divides 180, 225, 315

$$= 45$$

$$\begin{array}{l} 5 \overline{) 180, 225, 315} \\ 3 \overline{) 36, 45, 63} \\ 3 \overline{) 12, 15, 21} \\ 4, 5, 7 \end{array}$$

$$\text{H.C.F} = \cancel{3} \times \cancel{3} \times 5 = 45$$

$$\begin{array}{r} 90 \\ 2 \overline{) 180} \\ \underline{180} \\ 0 \end{array} \quad \begin{array}{r} 1 \\ 180 \overline{) 225} \\ \underline{180} \\ 45 \\ 45 \overline{) 45} \\ \underline{45} \\ 0 \end{array} \quad \begin{array}{r} 7 \\ 315 \\ \underline{315} \\ 0 \end{array}$$

6) 45 = 1, 3, 5, 9, 15, 45

56 = 1, 2, 4, 7, 8, 14, 28, 56

HCF (45, 56) = 1, So, 45 and 56 are co-prime

These have only 1 common factor that is 1. So they are co-prime number.

7) 15 = 1, 3, 5, 15

16 = 1, 2, 4, 8, 16

21 = 1, 3, 7, 21

28 = 1, 2, 4, 7, 14, 28

15 & 16, 21 & 28, 16 & 28, 15 & 28, 21 & 15,

15 & 21, are co-prime no

⑧ $93 - 3 = 90$

$111 - 3 = 108$

$129 - 3 = 126$

$$\begin{array}{r} 90 \overline{) 108} \\ \underline{- 90} \\ 18 \\ 18 \overline{) 126} \\ \underline{- 126} \\ 0 \end{array}$$

H.C.F = 18