

$$6. \quad a = 17 \quad a_n = 350 \quad d = 9$$

$$a_n = a + (n-1)d$$

$$350 = 17 + (n-1)9$$

$$350 = 17 + 9n - 9$$

$$342 = 8 + 9n$$

$$342 = 9n$$

$$38 = n$$

$$S_n = \frac{n}{2} \{ 2a + (n-1)d \}$$

$$= \frac{38}{2} \{ 34 + 37 \times 9 \}$$

$$= 19 \{ 34 + 333 \}$$

$$= 19 \times 367$$

$$= 6973$$

$$7. \quad d = 7 \quad n = 22 \quad a_n = 149$$

$$a_n = a + (n-1)d$$

$$149 = a + 21 \times 7$$

$$149 = a + 147$$

$$2 = a$$

$$S_n = \frac{n}{2} \{ 2a + (n-1)d \}$$

$$= 11 \{ 2 + 21 \times 7 \}$$

$$= 11 \{ 2 + 147 \}$$

$$= 11 \times 151$$

$$= 1661$$

$$8. \quad a_2 = 14 \quad a_3 = 18$$

$$a + d = 14 \quad a + 2d = 18$$

$$d = 4$$

$$a = 10$$

$$S_{51} = \frac{n}{2} \{ 2a + (n-1)d \}$$

$$= \frac{51}{2} \{ 20 + 200 \}$$

$$= \frac{51}{2} \times 220$$

$$= 51 \times 110$$

$$= 5610$$

$$q. \quad S_7 = 49$$

$$S_n = \frac{n}{2} \{ 2a + (n-1)d \}$$

$$49 = \frac{7}{2} \{ 2a + 6d \}$$

$$49 = 7 \{ a + 3d \}$$

$$7 = a + 3d$$

$$a + 8d = 17$$

$$a + 3d = 7$$

$$\hline 5d = 10$$

$$d = 2$$

$$a = 1$$

$$S_{17} = 289$$

$$S_n = \frac{n}{2} \{ 2a + (n-1)d \}$$

$$289 = \frac{17}{2} \{ 2a + 16d \}$$

$$289 = 17 \{ a + 8d \}$$

$$17 = a + 8d$$

$$S_n = \frac{n}{2} \{ 2a + (n-1)d \}$$

$$S_n = \frac{n}{2} \{ 2 + (n-1)2 \}$$

$$S_n = \frac{n}{2} \{ 2 + 2n - 2 \}$$

$$S_n = \frac{n}{2} \{ 2n \}$$

$$S_n = n^2$$

10 (i)  $a_n = 3 + 4n$

let  $n = 1$

$a_1 = 3 + 4(1) = 3 + 4 = 7$

$a_2 = 3 + 4(2) = 3 + 8 = 11$

$a_3 = 3 + 4(3) = 3 + 12 = 15$

$a_4 = 3 + 4(4) = 3 + 16 = 19$

$a_5 = 3 + 4(5) = 3 + 20 = 23$

$\{7, 11, 15, 19, 23, \dots\}$

$$S_n = \frac{n}{2} \{2a + (n-1)d\}$$
  
$$= \frac{15}{2} \{14 + 14 \times 4\}$$
  
$$= \frac{15}{2} \{14 + 56\}$$
  
$$= \frac{15}{2} \times 70$$
  
$$= 15 \times 35$$
  
$$= 525$$

(ii)  $a_n = 9 - 5n$

let  $n = 1$

$a_1 = 9 - 5(1) = 9 - 5 = 4$

$a_2 = 9 - 5(2) = 9 - 10 = -1$

$a_3 = 9 - 5(3) = 9 - 15 = -6$

$a_4 = 9 - 5(4) = 9 - 20 = -11$

$a_5 = 9 - 5(5) = 9 - 25 = -16$

$\{4, -1, -6, -11, -16\}$

$$S_n = \frac{n}{2} \{2a + (n-1)d\}$$
  
$$= \frac{15}{2} \{8 + 14 \times -5\}$$
  
$$= \frac{15}{2} \{8 - 70\}$$
  
$$= \frac{15}{2} \times -62$$
  
$$= -465$$

11.  $S_n = 4n - n^2$

$S_1 = 4 - 1 = 3$

$S_2 = 8 - 4 = 4$

$S_3 = 12 - 9 = 3$

$S_4 = 16 - 16 = 0$

$S_5 = 20 - 25 = -5$

$S_6 = 24 - 36 = -12$

$a_4 = S_4 - S_3$

$a_3 = S_3 - S_2$

$a_2 = S_2 - S_1$

$a_1 = S_1 - S_0 = 3$

$a_2 = S_2 - S_1 = 1$

$a_3 = 3 - 4 = -1$

$a_4 = 0 - 3 = -3$

$a_5 = -5 - 0 = -5$

$a_6 = -12 + 5 = -7$

$\{3, 1, -1, -3, -5, -7, \dots\}$

$a = 3 \quad d = -2$

10.  $\{6, 12, 18, 24, 30, \dots, 240\}$

$$a = 6 \quad d = 6$$

$$S_n = \frac{n}{2} \{ 2a + (n-1)d \}$$

$$S_{40} = \frac{40}{2} \{ 12 + 39 \times 6 \}$$

$$S_{40} = 20 \{ 12 + 234 \}$$

$$S_{40} = 20 \{ 246 \}$$

$$S_{40} = 4920$$