

Exercise 7.1

1. (i) $(2, 3), (4, 1)$

$x_1 = 2 \quad y_1 = 3$

$x_2 = 4 \quad y_2 = 1$

(ii) $(-5, 7), (-1, 3)$

$x_1 = -5 \quad y_1 = 7$

$x_2 = -1 \quad y_2 = 3$

(iii) $(a, b), (-a, -b)$

$x_1 = a \quad y_1 = b$

$x_2 = -a \quad y_2 = -b$

$$\Rightarrow \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} \Rightarrow \sqrt{(x_2 - x_1) + (y_2 - y_1)} \Rightarrow \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$\Rightarrow \sqrt{(4-2)^2 + (1-3)^2} \Rightarrow \sqrt{(-1+5)^2 + (3-7)^2} \Rightarrow \sqrt{(a-a)^2 + (-b-b)^2}$$

$$\Rightarrow \sqrt{(2)^2 + (-2)^2} \Rightarrow \sqrt{(4)^2 + (4)^2} = \sqrt{4a^2 + 4b^2}$$

$$\Rightarrow \sqrt{4+4} \Rightarrow \sqrt{16+16} = \sqrt{32} = \sqrt{4(a^2+b^2)}$$

$$= \sqrt{8} = \sqrt{2 \times 2 \times 2} = 2\sqrt{2} \Rightarrow \sqrt{32} = 4\sqrt{2} = 2\sqrt{a^2+b^2}$$

2. $(0, 0), (36, 15)$

$$\text{Distance} = \sqrt{(x^2 - x')^2 + (y^2 - y')^2}$$

$$= \sqrt{(36-0)^2 + (15-0)^2}$$

$$= \sqrt{(36)^2 + (15)^2}$$

$$= \sqrt{1296 + 225} = \sqrt{1521} = 39 \text{ units}$$

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3. $A(1, 5), B(2, 3), C(-2, -11)$

$$AB = \sqrt{(2-1)^2 + (3-5)^2}$$

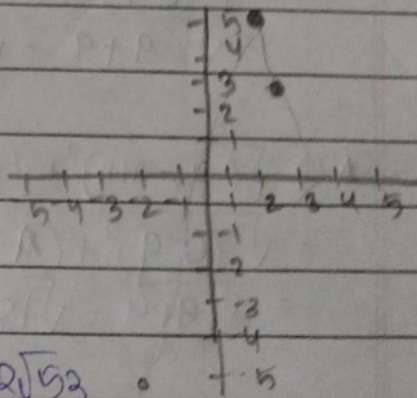
$$= \sqrt{(1)^2 + (-2)^2} = \sqrt{1+4} = \sqrt{5}$$

$$BC = \sqrt{(-2-2)^2 + (-11-3)^2}$$

$$= \sqrt{(-4)^2 + (-14)^2} = \sqrt{16+196} = \sqrt{212} = 2\sqrt{53}$$

$$CA = \sqrt{(-2-1)^2 + (-11-5)^2}$$

$$= \sqrt{(-3)^2 + (-16)^2} = \sqrt{9+256} = \sqrt{265}$$

 $AB + BC \neq CA$ hence not collinear

4. $A(5, -2)$ $B(6, 4)$ $C(7, -2)$

$$\begin{aligned} AB &= \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} \\ &= \sqrt{(6 - 5)^2 + (4 + 2)^2} \\ &= \sqrt{1 + 36} = \sqrt{37} \end{aligned}$$

$$\begin{aligned} BC &= \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} \\ &= \sqrt{(7 - 6)^2 + (-2 - 4)^2} \\ &= \sqrt{1 + 36} = \sqrt{37} \end{aligned}$$

$$\begin{aligned} AC &= \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} \\ &= \sqrt{(7 - 5)^2 + (-2 + 2)^2} \\ &= \sqrt{4} = 2 \end{aligned}$$

As $AB = BC$ therefore it is an isosceles triangle.