

QUADRILATERALSExercise → 8.1

Q1) The angles of quadrilateral are in ratio 3:5:9:13.
Find all the angles of the quadrilateral.
The angles be $3x, 5x, 9x, 13x$.

$$\therefore 3x + 5x + 9x + 13x = 360^\circ$$

$$\Rightarrow 30x = 360^\circ$$

$$x = \frac{360}{30} = 12^\circ$$

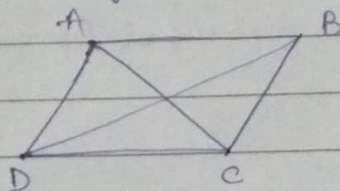
$$3x = 36^\circ$$

$$5x = 60^\circ$$

$$9x = 108^\circ$$

$$13x = 156^\circ$$

Q2) Let ABCD is a parallelogram such that
 $AC = BD$



In $\triangle ABC$ & $\triangle DCB$

$$AC = DB \text{ (given)}$$

$$AB = DC \text{ (opposite sides of a parallelogram)}$$

$$BC = CB \text{ (common)}$$

$$\therefore \triangle ABC \cong \triangle DCB \text{ (By SSS congruency)}$$

$$\Rightarrow \angle ABC = \angle DCB \text{ (By C.P.C.T)}$$

Now $AB \parallel DC$ and BC is a transversal
($\therefore ABCD$ is a parallelogram)

$\therefore \angle ABC + \angle DCB = 180^\circ$ (co-interior angles)

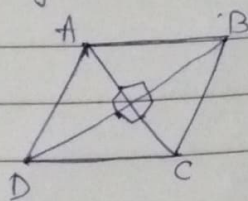
From 1 & 2 we have

$$\angle ABC = \angle DCB = 90^\circ$$

i.e., $ABCD$ is a parallelogram having an equal angle to 90° .

$\therefore ABCD$ is a rectangle.

Q3) Let $ABCD$ be a quadrilateral such that the diagonals AC and BD bisect each other at right angles at O .



\therefore In $\triangle AOB$ and $\triangle AOD$, we have

$$AO = AO \text{ (common)}$$

$$OB = OD \text{ (O is the midpoint of BD)}$$

$$\angle AOB = \angle AOD \text{ (each } 90^\circ)$$

$$\therefore \triangle AOB \cong \triangle AOD \text{ (By SAS)}$$

$$\therefore AB = AD \text{ (By CPCT)}$$

Similarly, $AB = BC$ (2)

$$BC = CD$$

$$CD = DA$$

\therefore From (1) & (2), (3) & (4) we have

$$AB = BC = CD = DA$$

\therefore Quadrilateral $ABCD$ is a rhombus.