

*** EQUAL SETS:**

Two sets are said to be equal if the elements of the two sets are the same.

EX: $A = \{1, 2, 3, 4\}$

$B = \{1, 2, 3, 4\}$

$SETA = SETB$

*** EQUIVALENT SETS:**

Two sets are said to be equivalent if the elements in both the set are equal.

EX: $A = \{1, 5, 7\}$

$B = \{A, B, C\}$

EXERCISE 10(D)

1. (i) $\{3, 5, 7, \dots\}$ Infinite

(ii) $\{1, 2, 3, 4\}$ Finite

(iii) $\{\dots, -3, -2, -1, 0, 1, 2\}$ Infinite

(iv) $\{20, 30, 40, 50, \dots, 20\}$ Finite

2. (i) Set of counting numbers between 5 and 6. yes

(ii) Set of odd nos. between 7 and 19. No

(iii) Set of odd nos. between 7 and 9. yes

(iv) Set of even no. that are not divisible by 2. yes

(v) $\{0\}$. ~~yes~~ No

3. (i) $\{3, 5, 7\}$ & $\{5, 3, 7\}$ Equal & Equivalent both
- (ii) $\{8, 6, 10, 2\}$ & $\{3, 2, 4, 6\}$ Equivalent but not equal
- (iii) $\{7, 7, 2, 12\}$ and $\{1, 2, 7\}$ Equal but not equivalent
- (iv) $\{2, 4, 6, 8, 10\}$ and $\{a, b, d, e, m\}$ Equivalent but not equal
4. (i) Set of integers = infinite
- (ii) {Multiples of 5} = infinite
- (iii) {Fractions between 1 and 2} = infinite
- (iv) {No. of people in India} = ~~infinite~~
- (v) {Set of trees in the world} = infinite
- (vi) Set of leaves on a tree = ~~infinite~~
- (vii) Set of ~~children~~ children in all the schools of Delhi = ~~infinite~~
- (viii) $\{\dots, -4, -2, 0, 2, 4, 6, 8\}$ = infinite
- (ix) $\{-12, -9, -6, -3, 0, 3, 6, \dots\}$ = infinite
- (x) {No. of points in a line segment 4cm long} = infinite

5. (i) {Prime nos. divisible by 2} = No

(ii) {Negative natural nos.} = Yes

(iii) {Women with height 5 metre} = No

(iv) {Integers less than 5} = No

(v) {Prime numbers between 17 and 23} = No

(vi) {Set of even nos. less than divisible by 2} = Yes

(vii) {Set of multiples of 3 that are more than 9 & less than 19.} = No

6. (i) {Natural no. less than five} & {letters of the word 'BOAT'} = Equivalent

(ii) {2, 4, 6, 8, 10} & {even natural no. less than 12} = Equal & Equivalent

(iii) {1, 3, 5, 7, ...} and {set of odd natural nos.} = Equal and equivalent

(iv) {letters of the word 'MEMBER'} and {letters of the word 'REMEMBER'} = equal and equivalent

(v) {Negative natural no.} & {30th day of a month} = Equal

(vi) {Even natural no.} & {Odd natural no.} = equivalent

* Disjoint Sets:

If two given sets have no element in common, they are disjoint sets.

EX: $A = \{1, 3, 7\}$

$B = \{6, 9, 10\}$

A and B are disjoint sets.

* OVERLAPPING SETS:

If two given sets have at least one element in common, they are said to be overlapping sets.

EX: $A = \{1, 3, 7\}$

$C = \{1, 2, 5, 9\}$

A and C are overlapping sets.

7. (i) $\{2, 4, 6, 8, \dots, 800\} = \text{Finite}$

(ii) $\{\dots, -5, -4, -3, -2\} = \text{Infinite}$

(iii) $\{x : x \text{ is an integer between } -60 \text{ and } 60\} = \text{Finite}$

(iv) $\{\text{No. of electrical appliances working in your house}\} = \text{Finite}$

(v) $\{x : x \text{ is a whole no. less than } 20\} = \text{Finite}$

(vi) $\{x : x \text{ is a whole no. less than } 20\} = \text{Finite}$

8. (i) $A = \{\text{birds with age below } \{ \dots, -8, -4, 0, 4, 8 \}\}$ is a finite set. = ~~Infinite~~ false

(ii) $\{-32, -28, -24, -20, \dots, 0, 4, 8, 16\}$ is a infinite set. = false

(iii) $\{x: x \text{ is a natural no. less than } 1\}$ is the empty set. = True

(iv) $\{ \text{Whole nos. between } 15 \text{ and } 16 \} = \{ \text{Natural nos. between } 5 \text{ and } 6 \} = \text{True}$

(v) $\{ \text{Odd nos. divisible by } 2 \}$ is the empty set = ~~False~~ True

(vi) $\{ \text{Even natural nos. divisible by } 3 \}$ is the empty set = False

(vii) $\{x: x \text{ is positive and } x < 0\}$ is the empty set = True

(viii) $\{ \dots, -5, -3, -1, 1, 3, 5, \dots \}$ is a finite set = False

9. (i) $A = \{ \text{Girls with ages below } 19 \text{ years} \}$
 $B = \{ \text{Girls with ages above } 19 \text{ years} \}$

As there is no common element in these 2 sets therefore set A and B are disjoint set.

(ii) $C = \{ \text{Boys with age above } 20 \text{ years} \}$
 $D = \{ \text{Boys with ages above } 27 \text{ years} \}$

Boys above 27 years are also above 20 years therefore set C and D are overlapping sets.

(iii) $A = \{ \text{Natural nos. between } 35 \text{ and } 60 \}$
 $B = \{ \text{Natural nos. between } 50 \text{ and } 80 \}$

Natural Nos. from 51 to 59 are common

in both sets therefore set A & B are overlapping sets.

- (iv) $P = \{ \text{Students of class IX studying in ICSE Board} \}$
 $Q = \{ \text{Students of class IX} \}$ studying

As students of class IX studying in ICSE Board are common in both sets, therefore P and Q are overlapping sets.

- (v) $A = \{ \text{Natural nos. that are multiples of 3 and less than 30} \} = \{ 3, 6, 9, 12, 15, 18, 21, 24, 27 \}$
 $B = \{ \text{Natural nos. divisible by 4 and lying between 20 and 45} \} = \{ 24, 28, 32, 36, 40, 44 \}$

As 24 is common in both the sets, therefore set A and B are overlapping set.

- (vi) $P = \{ \text{letters in the word 'ALLAHABAD'} \} = \{ A, L, H, B, D \}$
 $Q = \{ \text{letters in the word 'MUSSOORIE'} \} = \{ M, U, S, O, R, I, E \}$

No letter is common in both the sets so set P and Q are disjoint sets.