

1) i) 16, 35

ans) Factors of 16 are $\rightarrow 1, 2, 4, 8, 16$.Factors of 35 are $\rightarrow 1, 5, 7, 35$.H.C.F. $\rightarrow 1$

iii) 27, 75

ans) Factors of 27 are $\rightarrow 1, 3, 9, 27$.Factors of 75 are $\rightarrow 1, 3, 5, 15, 25, 75$.Common Factors $\rightarrow 1, 3$.H.C.F. $\rightarrow 3$

iv) 8, 12, 18

ans) Factors of 8 $\rightarrow 1, 2, 4, 8$.Factors of 12 $\rightarrow 1, 2, 3, 4, 6, 12$.Factors of 18 $\rightarrow 1, 2, 3, 6, 9, 18$.

Ex
Tuesday

Common Factor = 1 and 2

H.C.F. = 2

ii) 25 and 20

Ans → Factors of 25 are → 1, 5, 25.

Factors of 20 are → 1, 2, 10, 4, 5, 20.

Common factors = 1, 5

H.C.F. → 5

iv) 24, 36, 45 and 60

Ans → Factors of 24 are → 1, 2, 3, 4, 6, 12, 8, 24.

Factors of 36 are → 1, 2, 3, 4, 6, 18, 12, 9, 36.

Factors of 45 are → 1, 3, 15, 5, 9, 45.

Factors of 60 are → 1, 2, 3, 4, 5, 6, 10, 12, 15, 20, 30, 60.

Common factors = 1, 3

H.C.F. → 3

When two numbers have only 1 as the H.C.F. those numbers are called coprime numbers.

Ans

Tuesday

2. Using the prime factor method, find the H.C.F. of

i) 5 and 8

$$\text{Ans} \rightarrow \begin{array}{r|l} 5 & 5 \\ \hline & 1 \end{array} \quad \begin{array}{r|l} 2 & 8 \\ \hline 2 & 4 \\ \hline & 2 \end{array}$$

$$5 = 5, 1$$

$$8 = 2, 2, 2$$

$$\text{H.C.F.} = 1$$

ii) 24 and 49

$$\begin{array}{r|l} 2 & 24 \\ \hline 2 & 12 \\ \hline 2 & 6 \\ \hline & 3 \end{array} \quad \begin{array}{r|l} 7 & 49 \\ \hline 7 & 7 \\ \hline & 1 \end{array}$$

$$24 = 2, 3, 2, 2$$

$$49 = 7, 7$$

$$\text{H.C.F.} = 1$$

iii) 40, 60, 80

$$\begin{array}{r|l} 2 & 40 \\ \hline 2 & 20 \\ \hline 2 & 10 \\ \hline 5 & 5 \\ \hline & 1 \end{array} \quad \begin{array}{r|l} 2 & 60 \\ \hline 2 & 30 \\ \hline 3 & 15 \\ \hline 5 & 5 \\ \hline & 1 \end{array} \quad \begin{array}{r|l} 2 & 80 \\ \hline 2 & 40 \\ \hline 2 & 20 \\ \hline 2 & 10 \\ \hline 5 & 5 \\ \hline & 1 \end{array}$$

Ans
Tuesday

$$40 = 2, 2, 2, 5, 1$$

$$60 = 2, 2, 3, 5, 1$$

$$80 = 2, 2, 2, 2, 5, 1$$

$$H.C.F. = 2 \times 2 \times 5 \times 1 = 20$$

iii) 48, 84, 88

2 48	2 84	2 88
2 24	2 42	2 44
2 12	3 21	2 22
2 6	7 7	11 11
2 3	1	1
1		

$$48 = 2, 2, 2, 2, 2, 1$$

$$84 = 2, 2, 3, 7, 1$$

$$88 = 2, 2, 2, 11, 1$$

$$H.C.F. = 2 \times 2 \times 1 = 4$$

iv) 12, 16, 28

2 12	2 16	2 28
2 6	2 8	2 14
3 3	2 4	7 7
1	2 2	1
	1	

Ans
Tuesday

$$12 = 2, 2, 3, 1$$

$$16 = 2, 2, 2, 2, 1$$

$$28 = 2, 2, 7, 1$$

$$H.C.F. = 2 \times 2 \times 1 = 4$$

$$12 = 1, 2, 3, 4, 6, 12$$

$$18 = 1, 2, 3, 6, 9, 18$$

Common factors $\rightarrow 1, 2, 3, 6$

$$H.C.F. = 6$$

3) Using the division

i) 16 and 24

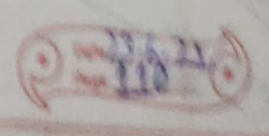
$$\text{Ans} \rightarrow \begin{array}{r} 16 \overline{) 24} \quad (1 \\ \underline{-16} \end{array}$$

$$\begin{array}{r} 8 \overline{) 16} \quad (2 \\ \underline{-16} \\ \hline 0 \end{array}$$

$$H.C.F. = 8$$

ii) 32, 56 and 40

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$$\begin{array}{r} 32 \overline{) 56} (1 \\ \underline{32} \\ 24 \overline{) 32} (1 \\ \underline{24} \\ 8 \overline{) 24} (3 \\ \underline{24} \\ \underline{0} \end{array}$$

$$\begin{array}{r} 8 \overline{) 40} (5 \\ \underline{40} \\ 6 \overline{) 8} (1 \\ \underline{6} \\ 2 \overline{) 6} (3 \\ \underline{6} \\ \underline{0} \end{array}$$

Therefore, the H.C.F. is 2.

Q) 45, 75, 135

$$\begin{array}{r} 45 \overline{) 75} (1 \\ \underline{45} \\ 30 \overline{) 45} (1 \\ \underline{30} \\ 15 \overline{) 30} (2 \\ \underline{30} \\ \underline{0} \end{array}$$

$$\begin{array}{r} 15 \overline{) 135} (9 \\ \underline{135} \\ \underline{0} \end{array}$$

H.C.F. = 15

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ii) 18 and 30

$$\begin{array}{r}
 18 \overline{) 30} \quad (1 \\
 \underline{-18} \\
 12 \overline{) 18} \quad (1 \\
 \underline{-12} \\
 6 \overline{) 12} \quad (2 \\
 \underline{-12} \\
 0
 \end{array}$$

H.C.F. = 6

iii) 7, 14 and 24

$$\begin{array}{r}
 7 \overline{) 14} \quad (2 \\
 \underline{-14} \\
 0 \\
 \\
 7 \overline{) 24} \quad (3 \\
 \underline{-21} \\
 3 \overline{) 7} \quad (2 \\
 \underline{-6} \\
 1 \overline{) 3} \quad (3 \\
 \underline{-3} \\
 0
 \end{array}$$

H.C.F. = 1.

iv) 70, 80, 120 and 150

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$$\begin{array}{r} 70 \overline{) 80} (1 \\ \underline{-70} \\ 0 \end{array}$$

$$\begin{array}{r} 10 \overline{) 70} (7 \\ \underline{-70} \\ 0 \end{array}$$

$$\begin{array}{r} 10 \overline{) 120} (12 \\ \underline{-120} \\ 0 \end{array}$$

$$\begin{array}{r} 10 \overline{) 150} (15 \\ \underline{-150} \\ 0 \end{array}$$

H.C.F. = 10

4) ii) 48, 36 and 96

Ans \rightarrow $\begin{array}{r} 36 \overline{) 48} (1 \\ \underline{-36} \end{array}$

$$\begin{array}{r} 12 \overline{) 36} (3 \\ \underline{-36} \\ 0 \end{array}$$

$$\begin{array}{r} 12 \overline{) 96} (8 \\ \underline{-96} \\ 0 \end{array}$$

H.C.F. = 12

iii) 66, 33 and 132

Ans
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$$\begin{array}{r} 33 \overline{) 66} (2 \\ \underline{-66} \\ 0 \end{array}$$

$$\begin{array}{r} 33 \overline{) 132} (4 \\ \underline{-132} \\ 0 \end{array}$$

H.C.F. = 33

iv) 24, 36, 60 and 132

Ans →	$\begin{array}{r} 2 \overline{) 24} \\ \underline{2 \overline{) 12}} \\ \underline{2 \overline{) 6}} \\ 3 \end{array}$	$\begin{array}{r} 2 \overline{) 36} \\ \underline{2 \overline{) 18}} \\ \underline{3 \overline{) 9}} \\ 3 \end{array}$	$\begin{array}{r} 2 \overline{) 60} \\ \underline{2 \overline{) 30}} \\ \underline{3 \overline{) 15}} \\ 5 \end{array}$	$\begin{array}{r} 2 \overline{) 132} \\ \underline{2 \overline{) 66}} \\ \underline{3 \overline{) 33}} \\ 11 \end{array}$
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$$24 = 2 \times 2 \times 2 \times 3$$

$$36 = 2 \times 2 \times 3 \times 3$$

$$60 = 2 \times 2 \times 3 \times 5$$

$$132 = 2 \times 2 \times 3 \times 11$$

H.C.F. = $2 \times 2 \times 3 = 12$

v) 30, 60, 90 and 105

$\begin{array}{r} 2 \overline{) 30} \\ \underline{3 \overline{) 15}} \\ 5 \end{array}$	$\begin{array}{r} 2 \overline{) 60} \\ \underline{2 \overline{) 30}} \\ \underline{3 \overline{) 15}} \\ 5 \end{array}$	$\begin{array}{r} 2 \overline{) 90} \\ \underline{3 \overline{) 45}} \\ \underline{3 \overline{) 15}} \\ 5 \end{array}$	$\begin{array}{r} 3 \overline{) 105} \\ \underline{5 \overline{) 35}} \\ 7 \end{array}$
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Ans
Wednesday

$$30 = 2 \times 3 \times 5$$

$$60 = 2 \times 3 \times 5 \times 2$$

$$90 = 2 \times 3 \times 5 \times 3$$

$$105 = 3 \times 5 \times 7$$

$$\text{H.C.F.} = 5 \times 3 = 15$$

5) Find the greatest number that divides each of 180, 225 and 315 completely.

$$\begin{array}{r} \text{Ans} \rightarrow 180 \overline{) 225} \quad (1) \\ \underline{-180} \\ 45 \end{array}$$
$$\begin{array}{r} 45 \overline{) 180} \quad (4) \\ \underline{-180} \\ 0 \end{array}$$

$$\begin{array}{r} 45 \overline{) 315} \quad (7) \\ \underline{-315} \\ 0 \end{array}$$

$$\text{H.C.F.} = 45$$

Therefore, the greatest number that divides each of 180, 225 and 315 completely that number is 45.

6) Show that 45 and 56 are co-prime numbers.

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wednesday

$$\begin{array}{r} \text{Ans} \rightarrow 45 \overline{) 56} (1 \\ \underline{-45} \\ 11 \overline{) 45} (4 \\ \underline{-44} \\ 1 \overline{) 11} (11 \\ \underline{-11} \\ 0 \end{array}$$

$$\text{H.C.F.} = 1$$

Therefore, the H.C.F. of 56 and 45 is 1. The numbers which have the H.C.F. as 1 are called co-prime numbers. Therefore, 56 and 45 are also co-prime as their H.C.F. is 1.

7) Out of 15, 16, 21 and 28, find out all the pairs of co-primes.

Ans \rightarrow H.C.F. of 15 and 16.

$$\begin{array}{r} 15 \overline{) 16} (1 \\ \underline{-15} \\ 1 \overline{) 15} (15 \\ \underline{-15} \\ 0 \end{array}$$

$$\text{H.C.F.} = 1$$

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Therefore, 15 and 16 are co-primes.

2) H.C.F. of 15 and 21

$$\begin{array}{r}
 15 \overline{) 21} (1 \\
 \underline{-15} \\
 6 \overline{) 15} (2 \\
 \underline{-12} \\
 3 \overline{) 6} (2 \\
 \underline{-6} \\
 0
 \end{array}$$

Therefore, 15 and 21 are not co-primes.

3) H.C.F. of 15 and 28.

$$\begin{array}{r}
 15 \overline{) 28} (1 \\
 \underline{-15} \\
 13 \overline{) 15} (1 \\
 \underline{-13} \\
 2 \overline{) 13} (6 \\
 \underline{-12} \\
 1 \overline{) 2} (2 \\
 \underline{-2} \\
 0
 \end{array}$$

Therefore, 15 and 28 are co-primes.

4) H.C.F. of 16 and 21.

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$$\begin{array}{r} \text{Ans} \rightarrow 16 \overline{) 21} (1 \\ \underline{-16} \\ 5 \overline{) 11} (3 \\ \underline{-15} \\ 1 \overline{) 5} (5 \\ \underline{-5} \\ 0 \end{array}$$

Therefore, 16 and 21 are co-primes.

5) H.C.F. of 16 and 28

$$\begin{array}{r} 16 \overline{) 28} (1 \\ \underline{-16} \\ 12 \overline{) 16} (1 \\ \underline{-12} \\ 4 \overline{) 12} (3 \\ \underline{-12} \\ 0 \end{array}$$

Therefore, 16 and 28 are not co-primes.

6) H.C.F. of 21 and 28

$$\begin{array}{r} 21 \overline{) 28} (1 \\ \underline{-21} \\ 7 \overline{) 21} (3 \\ \underline{-21} \\ 0 \end{array}$$

Therefore, 21 and 28 are not co-primes.

Ans
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Therefore, all the pairs of co-primes are 15 and 16;
15 and 28; 16 and 21.

8) Find the greatest number that will divide 93, 111 and 129, leaving a remainder 3 in each case of the given numbers in above line.

Ans \rightarrow Since, the greatest number that will divide 93, 111 and 129, leaving a remainder of 3 in each case = $93 - 3 = 90$, $111 - 3 = 108$, $129 - 3 = 126$.

Therefore, the H.C.F. of 90, 108 and 126 is:

$$\begin{array}{r} 90 \overline{) 108} \quad (1 \\ \underline{- 90} \\ 18 \end{array} \quad \begin{array}{r} 18 \overline{) 90} \quad (5 \\ \underline{- 90} \\ 0 \end{array}$$

$$\begin{array}{r} 18 \overline{) 126} \quad (7 \\ \underline{- 126} \\ 0 \end{array}$$

H.C.F. = 18

Therefore, the greatest number is 18.

Shua