

ASSIGNMENT

1) i) The last digit of $332 + 3331$ is 1

The cube of 1 is 1

So, the last digit of the cube of 3331 is 1

ii) The last digit of 8888 is 8

The cube of 8 is 512

So, the last digit of the cube of 888 is 2

iii) The last digit of 149 is 9

The cube of 9 is 729

So, the last digit of the cube of 149 is 9

iv) The last digit of 1005 is 5

The cube of 5 is 125

So, the last digit of the cube of 1005 is 5

v) The last digit of 1024 is 4

The cube of 4 is 64

So, the last digit of the cube of 1024 is 4

vi) The last digit of 77 is 7

The cube of 7 is 343

So, the last digit of the cube of 77 is 3

vii) The last digit of 5022 is 2

The cube of 2 is 8

So, the last digit of the cube of 5022 is 8

viii) The last digit of the no. 53 is 3

The cube of 3 is 27

So, the last digit of the cube of 53 is 7

2) a) $6^3 = 216 = 31 + 33 + 35 + 37 + 39 + 41$

b) ~~$7^3 = 343 = 43 + 45 + 53 + 59 + 61 + 67 + 71 + 47 + 49 + 51 + 53 + 55$~~

c) $8^3 = 512 = 57, 59, 61, 63, 65, 67, 69, 71$

3) a) No e) No

b) Yes, $15^3 = 3375$ f) Yes, $19^3 = 6859$

c) Yes, $20^3 = 8000$

d) Yes, $25^3 = 15625$

4. On finding the prime factors of 392,
 we get : $392 = 2 \times 2 \times 2 \times 7 \times 7$

Clearly, 392 is not a perfect cube and it must be multiplied by 7 so that the product is a perfect cube.

$$\begin{aligned} 392 \times 7 &= (2 \times 2 \times 2 \times 7 \times 7) \times 7 \\ &= (2 \times 7) \times (2 \times 7) \times (2 \times 7) \\ &= 14^3 \end{aligned}$$

5. On finding the prime factors of 53240,

we get : $2 \times 2 \times 2 \times 5 \times 11 \times 11 \times 11$

Clearly, 53240 is not a perfect cube and it must be divided by 5 so that the quotient is a perfect cube.

$$\begin{aligned} 53240 \div 5 &= (2 \times 2 \times 2 \times 5 \times 11 \times 11 \times 11) \div 5 \\ &= 2 \times 2 \times 2 \times 11 \times 11 \times 11 \\ &= (2 \times 11) (2 \times 11) (2 \times 11) \\ &= 22^3 \end{aligned}$$

6. On finding the prime factor of 1188,

we get : $1188 = 2 \times 2 \times 3 \times 3 \times 3 \times 11$

Clearly, 1188 is not a perfect cube and it must be divided by 11 so that the quotient is a perfect cube.

$$\begin{aligned} 1188 \div 11 &= (2 \times 2 \times 3 \times 3 \times 3 \times 11) \div 11 \\ &= 2 \times 2 \times 3 \times 3 \times 3 \\ &= 2 \times 3^3 \end{aligned}$$

7. On finding the prime factor of 68600,

we : $68600 = 2 \times 2 \times 2 \times 5 \times 7 \times 7 \times 7 \times 7$

Clearly, 68600 is not a perfect cube and it must be divided by 5 so that the product will be a perfect cube.

$$\begin{aligned} 68600 \times 5 &= (2 \times 2 \times 2 \times 5 \times 5 \times 7 \times 7 \times 7) \times 5 \\ &= (2 \times 5) (2 \times 5 \times 7) (2 \times 5 \times 7) (2 \times 5 \times 7) \\ &= 170^3 \end{aligned}$$