

Q.50
A. Prime factors of 50 are 2 and 5

2	50
5	25
5	5
	1

EX 8(B)

Using the common method find the HCF

(i) 16 and 35
Common factors of 16 and 35 are as follows:

$F(16) = 1, 2, 4, 8, 16$

$F(35) = 1, 5, 7, 35$

The common factors of ~~25~~ are between 16 and 35 = 1

\therefore The H.C.F of 16 and 35 = 1

(ii) 25 and 20
Common factors of 25 and 20 are as follows:

$F(25) = 1, 5, 25$

$F(20) = 1, 2, 4, 5, 10, 20$

CF = 1, 5

HCF = 5

(11)

Common factors between 27 and 75 are as follows:-

$$F(27) = 1, 3, 9, 27$$

$$F(75) = 1, 3, 5, 15, 25, 75$$

The common factors between 27 and 75 = 1, 3

∴ The H.C.F of 27 and 75 = 3

(12) 8, 12 & 18

A: Common factors between 8, 12 & 18 are as follows:-

$$F(8) = 1, 2, 4, 8$$

$$F(12) = 1, 2, 3, 4, 6, 12$$

$$F(18) = 1, 2, 3, 6, 9, 18$$

$$CF = 1, 2$$

The H.C.F = 2

v) 24, 36, 45 & 60

A: Common factors between 24, 36, 45, & 60 are as follows:-

$$F(24) = 1, 2, 3, 4, 6, 8, 12, 24$$

$$F(36) = 1, 2, 3, 4, 6, 12, 18, 36$$

$$F(45) = 1, 3, 5, 9, 15, 45$$

$$F(60) = 1, 2, 3, 4, 5, 6, 10, 12, 15, 20, 30, 60.$$

Common factors between 24, 36, 45, and 60 = 1, 3

\therefore The H.C.F. of 24, 36, 45 & 60 = 3

2) The Prime factors of 5 and 8 are as follows:

$$P_5 = 5$$

$$P_8 = 2 \times 2 \times 2$$

No. Common Prime factors between 5 & 8

$$\therefore \text{H.C.F. of } 5 \text{ \& } 8 = 1$$

ii) The Prime factors of 24 & 49 are as follows:

$$P_{24} = 2 \times 2 \times 2 \times 3$$

$$P_{49} = 7 \times 7$$

No. Common Prime factors between 24 & 49

$$\text{Hence H.C.F. of } 24 \text{ and } 49 = 1$$

(iii) 40, 60 and 80

$$P(40) = 2 \times 2 \times 2 \times 5$$

$$P_{60} = 2 \times 2 \times 3 \times 5$$

$$P_{80} = 2 \times 2 \times 2 \times 2 \times 5$$

$$\text{C.F.} = 2 \times 2 \times 5$$

$$\text{Hence H.C.F. } 40, 60 \text{ and } 80 = 20$$

(IV) 48, 84 and 88
A
 $48 = 2 \times 2 \times 2 \times 2 \times 3$
 $84 = 2 \times 2 \times 3 \times 7$
 $88 = 2 \times 2 \times 2 \times 11$

Common Prime Factors = 2×2
H.C.F. of 48, 84 & 88 = $2 \times 2 = 4$

(V) 12, 16 and 28
 $12 = 2 \times 2 \times 3$
 $16 = 2 \times 2 \times 2 \times 2$
 $28 = 2 \times 2 \times 7$

Common Prime Factors between 12, 16 & 28 = 2×2
Hence, H.C.F. of 12, 16 & 28 = $2 \times 2 = 4$

3.
i) 16 & 24

Ans Using division method, we can get,

H.C.F. of 16 & 24

	16		24	
			2	
			-16	2
			08	16
			-16	
			0	

last divisor = 8
H.C.F. = 8

(i) 18 & 30

Ans: H.C.F. of 18, 30 by division method,

$$\begin{array}{r|l} 18 & 30 \\ \hline & 18 \\ \hline & 12 \\ & 18 & | & 1 \\ & 12 & | & \\ \hline & & & 6 \end{array}$$

(ii) 7, 14 & 24
Ans: using division method, we get

$$\begin{array}{r|l} 7 & 14 \\ \hline & - 14 \\ \hline & 00 \end{array}$$

Here, last division is 1

Hence, H.C.F. of 7, 14 & 24 = 1

Q. iv) 70, 80, 120 & 150

Ans: Using division method

$$\begin{array}{r} 1 \\ \hline 70 \overline{) 80} \\ \underline{-70} \quad 10 \\ 10 \overline{) 120} \\ \underline{-100} \quad 20 \\ 20 \\ \underline{-20} \\ 000 \end{array}$$
$$\begin{array}{r} 15 \\ \hline 10 \overline{) 150} \\ \underline{-100} \\ 50 \\ \underline{-50} \\ 000 \end{array}$$

Hence the last division is 10.

∴ H.C.F. of 70, 80, 120 & 150 = 10

v) 32, 56 & 46

Ans: Using division method

$$\begin{array}{r} 1 \\ \hline 32 \overline{) 56} \\ \underline{-32} \quad 24 \\ 24 \overline{) 46} \\ \underline{-24} \\ 22 \end{array}$$
$$\begin{array}{r} 1 \\ \hline 56 \overline{) 32} \end{array}$$

$$\begin{aligned} \text{ii) } 45, 75 \text{ \& } 135 \\ \text{Ans } 45 &= 3 \times 3 \times 5 \\ 75 &= 3 \times 5 \times 5 \\ 135 &= 3 \times 3 \times 5 \end{aligned}$$

The C.F. of 45, 75 & 135 = 3×5

\therefore H.C.F. of 45, 75 and 135 = 15

$$\begin{aligned} \text{ii) } 48, 36, 96 \\ \text{Ans } 48 &= 2 \times 2 \times 2 \times 2 \times 3 \\ 36 &= 2 \times 2 \times 3 \times 3 \\ 96 &= 2 \times 2 \times 2 \times 2 \times 3 \end{aligned}$$

The C.F. of 48, 36 & 96 = $2 \times 2 \times 3$

$$\begin{aligned} \text{iii) } 66, 33 \text{ and } 132 \\ \text{Ans } 66 &= \\ 33 &= \\ 132 &= \end{aligned}$$

H.C.F. of 48, 36 & 96 = 12

$$\begin{aligned} \text{iv) } 30, 60, 90 \text{ \& } 105 \\ \text{Ans } 30 &= \\ 60 &= \\ 90 &= \\ 105 &= \end{aligned}$$

H.C.F. of 30, 60, 90 & 105

$$\begin{array}{r} 30 \overline{) 60} \quad 2 \\ \underline{60} \\ 0 \end{array} \quad \begin{array}{r} 30 \overline{) 90} \quad 3 \\ \underline{90} \\ 0 \end{array}$$

22-06-21
H.C.F.
5.

H.C.F. of 30, 60 & 90 = 30

H.C.F. of 30, 60, 90 & 105 = H.C.F. of 30 & 105

Ans: The greatest number that divides each of 180, 225 & 315 will be the H.C.F. of 180, 225 and 315

Using division method, the H.C.F. of H.C.F. of 180 and 225

$$\begin{array}{r|l}
 180 & 225 \\
 \hline
 180 & 180 \quad | \quad 1 \\
 \hline
 & 45 & | \quad 180 & | \quad 4 \\
 & & \hline
 & & 180 & \\
 & & \hline
 & & 0 &
 \end{array}$$

H.C.F. of 180 and 225 = 45

H.C.F. of 180, 225 & 315 = H.C.F. of 45 & 315

$$\begin{array}{r}
 45 \overline{) 315} \\
 \underline{- 315} \\
 0
 \end{array}$$

Required H.C.F. 45

Since last division is 45

∴ H.C.F. of 180, 225 and 315 = 45

(6) Show that 45 and 56 co-prime number

Q. 108) Show that 45 and 56 are co-prime

$$\begin{array}{r}
 45 \overline{) 56} \\
 \underline{-45} \quad 9 \\
 11 \overline{) 45} \\
 \underline{-44} \quad 11 \\
 \quad 1 \overline{) 11} \\
 \quad \underline{-11} \\
 \quad \quad 0
 \end{array}$$

HCF of 45 & 56 = 1

\therefore 45 and 56 are co-prime.

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15, 16, 21 and 28 co prime =

$$15 = 1, 3, 5$$

$$16 = 1, 2, 4, 8, 16$$

$$21 = \cancel{1, 2, 3, 4, 5, 6, 7}, 1, 3, 7, 21$$

$$28 = 1, 2, 4, 7, 14, 28$$

15 and 16 are common factor = 1

16 and 21 common factor = 1

is they are co-prime

15 and 28 common factor is = 1

factor one only they have no common factor other there.

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⑧ Find the greatest number that divide, 93, 111 and 129 leaving remainder 3 in each case

Solution:-

First decrease the leaving remainder 3 from numbers 93, 111 and 129 to required number

$$93 - 3 = 90$$

$$111 - 3 = 108$$

$$129 - 3 = 126$$

In each case the HCF of ~~90, 111~~ ~~and 108~~ 90, 108 and 126 will be the greatest number that will divided 93, 111 and 129 leaving remainder 3

Using division method the

HCF of 90, 108 and 126 is given below

$$\begin{array}{r|l} 2 & 90 \\ \hline 3 & 45 \\ \hline 3 & 15 \\ \hline & 5 \end{array}$$

$$\begin{array}{r|l} 2 & 108 \\ \hline 2 & 54 \\ \hline 3 & 27 \\ \hline 3 & 9 \\ \hline & 3 \\ \hline & 1 \end{array}$$

$$\begin{array}{r|l} 2 & 126 \\ \hline 3 & 63 \\ \hline 3 & 21 \\ \hline 7 & 7 \\ \hline & 1 \end{array}$$

Common factor = 2, 3, 3

$$\text{H.C.F.} = 2 \times 3 \times 3 = 18$$