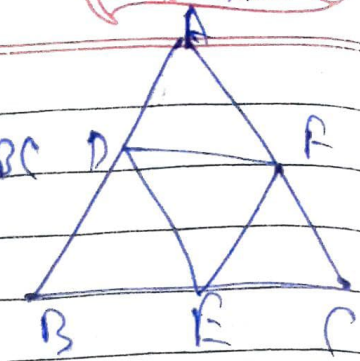


Ques



5A D and E are midpoints of $\triangle ABC$

$\therefore DE \parallel AC$ & $DE = \frac{1}{2} AC$

In $\triangle BED$ & $\triangle BCA$

$\angle BED = \angle BCA$ (Corresponding angle)

$\angle BDE = \angle BAC$

$\angle EBD = \angle CBA$ (Common)

$\therefore \triangle BED \sim \triangle BCA$ (AAA)

or $\frac{\text{ar}(\triangle BED)}{\text{ar}(\triangle BCA)} = \frac{1}{4}$

$\Rightarrow \text{ar}(\triangle BED) = \frac{1}{4} \text{ar}(\triangle BCA)$

$\text{ar}(\triangle CFE) = \frac{1}{4} \text{ar}(\triangle CBA)$

$\text{ar}(\triangle DEF) = \text{ar}(\triangle ABC) - [\text{ar}(\triangle BED) + \text{ar}(\triangle CFE) + \text{ar}(\triangle ADF)]$

$\Rightarrow \text{ar}(\triangle DEF) = \text{ar}(\triangle ABC) - \frac{3}{4} \text{ar}(\triangle ABC) = \frac{1}{4} \text{ar}(\triangle ABC)$

~~$\Rightarrow \text{ar}(\triangle DEF) = \text{ar}(\triangle ABC) - \frac{3}{4} \text{ar}(\triangle ABC)$~~

$\Rightarrow \frac{\text{ar}(\triangle DEF)}{\text{ar}(\triangle ABC)} = \frac{1}{4}$

6A $\frac{\text{ar}(\triangle ABC)}{\text{ar}(\triangle DEF)} = \frac{AB^2}{DE^2}$ — (1)

$\frac{AB}{DE} = \frac{BC}{EF}$

$\Rightarrow \frac{AB}{DE} = \frac{2BP}{2EQ}$

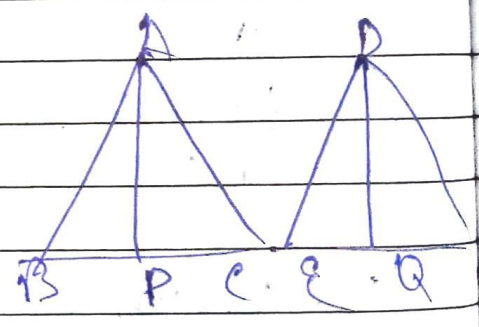
$\Rightarrow \frac{AB}{DE} = \frac{BP}{EQ}$

In $\triangle ABP$ & $\triangle DEQ$

$\frac{AB}{DE} = \frac{BP}{EQ}$

& $\angle B = \angle E$

By SAS $\triangle ABP \sim \triangle DEQ$



$$\Rightarrow \frac{AB}{DE} = \frac{AP}{DQ}$$

$$\Rightarrow \frac{AB^2}{DE^2} = \frac{AP^2}{DQ^2} \quad \text{--- (1)}$$

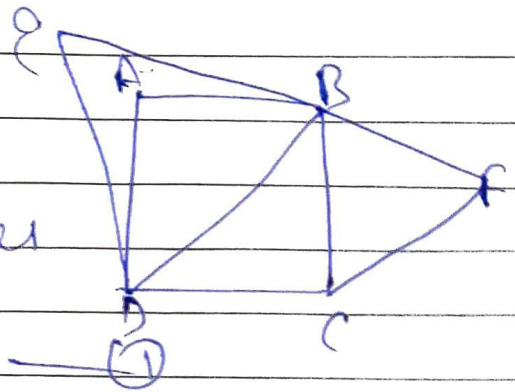
Comparing (1) & (2)

$$\frac{\text{ar}(\triangle ABC)}{\text{ar}(\triangle DEF)} = \frac{AP^2}{DQ^2}$$

* In $\triangle DEB$ & $\triangle CBF$ are equilateral Δ

\therefore Their corresponding sides are in equal ratio

In square ABCD $DB = BC\sqrt{2}$ --- (1)



$$\therefore \frac{A(\triangle CBF)}{A(\triangle DEB)} = \frac{\frac{\sqrt{3}}{4} \times (BC)^2}{\frac{\sqrt{3}}{4} \times (DB)^2}$$

$$\therefore \frac{A(\triangle CBF)}{A(\triangle DEB)} = \frac{\frac{\sqrt{3}}{4} \times (BC)^2}{\frac{\sqrt{3}}{4} \times (BC\sqrt{2})^2}$$

$$\therefore \frac{A(\triangle CBF)}{A(\triangle DEB)} = \frac{1}{2}$$

8. $\triangle ABC$ & $\triangle BDE$ are two equilateral Δ , D is mid point of BC. Ratio of areas of $\triangle ABC$ & $\triangle BDE$ is

$$A : (C) 4:1$$

9. Sides of two similar Δ are in ratio 4:9. Areas of these Δ are in ratio

$$A. (d) 16:81$$