

Exercise: 19 - (B)

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i)
$$\begin{array}{r} 3a + 4b + 7c \\ - 5a + 3b + 6c \\ \hline 4a - 2b - 4c \\ 2a + 5b + 3c \end{array}$$

ii)
$$\begin{array}{r} 2x^2 + xy - y^2 \\ - x^2 + 2xy + 3y^2 \\ \hline 3x^2 - 10xy + 4y^2 \\ 4x^2 - 7xy + 6y^2 \end{array}$$

iii)
$$\begin{array}{r} x^2 - x + 1 \\ - 5x^2 + 2x - 2 \\ \hline + 3x^2 - 3x + 1 \\ \hline -x^2 - 2x \end{array}$$

iv)
$$\begin{array}{r} a^2 - ab + bc \\ - 2a^2 + 2ab + bc \\ + 3a^2 + ab - 3bc \\ \hline 2a^2 + 2ab - bc \end{array}$$

v)
$$\begin{array}{r} 4x^2 + 7 - 3x \\ - x^2 + 8 + 4x \\ + - 2x^2 - 10 + 5x \\ \hline -x^2 + 5 + 6x \end{array}$$

vi)
$$\begin{array}{r} 3x + 4xy - y^2 \\ - 4x + xy + 2y^2 \\ + 6x - xy + 3y^2 \\ \hline 5x + 4xy + 4y^2 \end{array}$$

2) i) $-17x^2 - 2xy + 23y^2$, $-9y^2 + 15x^2 + 7xy$ and $13x^2 + 3y^2 - 4xy$

ans)
$$\begin{aligned} & (-17x^2 - 2xy + 23y^2) + (-9y^2 + 15x^2 + 7xy) + \\ & (13x^2 + 3y^2 - 4xy) \\ & = -17x^2 - 2xy + 23y^2 - 9y^2 + 15x^2 + 7xy + \\ & 13x^2 + 3y^2 - 4xy \\ & = 15x^2 + 13x^2 - 17x^2 + 23y^2 + 3y^2 - 9y^2 + 7xy - \\ & 2xy - 4xy \\ & = 11x^2 + 17y^2 + xy \end{aligned}$$

ii) $-x^2 - 3xy + 3y^2 + 8$, $3x^2 - 5y^2 - 3 + 4xy$ and $-6xy + 2x^2 - 2 + y^2$

ans)
$$\begin{aligned} & (-x^2 - 3xy + 3y^2 + 8) + (3x^2 - 5y^2 - 3 + \\ & 4xy) + (-6xy + 2x^2 - 2 + y^2) \\ & = -x^2 - 3xy + 3y^2 + 8 + 3x^2 - 5y^2 - 3 + 4xy - \\ & 6xy + 2x^2 - 2 + y^2 \\ & = 3x^2 + 2x^2 - x^2 + 3y^2 + y^2 - 5y^2 + 4xy - \\ & 3xy - 6xy + 8 - 3 - 2 \\ & = 4x^2 - y^2 - 5xy + 3 \end{aligned}$$

(iii) $a^3 - 2b^3 + a$, $b^3 - 2a^3 + b$ and $-2b + 2b + 2b^3 - 5a + 4a^3$

and $(a^3 - 2b^3 + a) + (b^3 - 2a^3 + b) + (-2b + 2b^3 - 5a + 4a^3)$
 $= a^3 - 2b^3 + a + b^3 - 2a^3 + b - 2b + 2b^3 - 5a + 4a^3$
 $= a^3 + 4a^3 - 2a^3 + 2b^3 + b^3 - 2b^3 + a - 5a + b - 2b$
 $= 3a^3 + b^3 - 4a - b$

3) (i) $3a - (a + 2b)$

$= 3a - a - 2b$
 $= 2a - 2b$

(ii) $(5x - 3y) - (x + y)$

$= 5x - 3y - x - y$
 $= 5x - x - 3y - y$
 $= 4x - 4y$

(iv) $(8a + 15b) - (3b - 7a)$

$= 8a + 15b - 3b + 7a$
 $= 8a + 7a + 15b - 3b$
 $= 15a + 12b$

(v) $(8x + 7y) - (4y - 3x)$

$= 8x + 7y - 4y + 3x$
 $= 8x + 3x + 7y - 4y$
 $= 11x + 3y$

v) $7 - (4a - 5)$

$= 7 - 4a + 5$
 $= 7 + 5 - 4a$
 $= 12 - 4a$

vi) $(6y - 13) - (4 - 7y)$

$= 6y - 13 - 4 + 7y$
 $= 6y + 7y - 13 - 4$
 $= 13y - 17$

4) i) $5a - 3b + 2c$ from $a - 4b - 2c$

$= a - 4b - 2c - (5a - 3b + 2c)$
 $= a - 4b - 2c - 5a + 3b - 2c$
 $= a - 5a - 4b + 3b - 2c - 2c$
 $= -4a - b - 4c$

ii) $4x - 6y + 3z$ from $12x + 7y - 2z$

$= 12x + 7y - 2z - (4x - 6y + 3z)$
 $= 12x + 7y - 2z - 4x + 6y - 3z$
 $= 12x - 4x + 7y + 6y - 2z - 3z$
 $= 8x + 13y - 5z$

$$\begin{aligned}
 \text{ii) } & 5 - a - 4b + 4c \text{ from } 5a - 7b + 2c \\
 &= 5a - 7b + 2c - (5 - a - 4b + 4c) \\
 &= 5a - 7b + 2c - 5 + a + 4b - 4c \\
 &= 5a + a + 4b - 7b + 2c - 4c - 5 \\
 &= 6a - 3b - 2c - 5
 \end{aligned}$$

$$\begin{aligned}
 \text{iv) } & -8x - 12y + 17z \text{ from } x - y - z \\
 &= x - y - z - (-8x - 12y + 17z) \\
 &= x - y - z + 8x + 12y - 17z \\
 &= x + 8x + 12y - y - z - 17z \\
 &= 9x + 11y - 18z
 \end{aligned}$$

$$\begin{aligned}
 \text{v) } & 2ab + cd - ac - 2bd \text{ from } ab - 2cd + 2ac + bd \\
 &= ab - 2cd + 2ac + bd - (2ab + cd - ac - 2bd) \\
 &= ab - 2cd + 2ac + bd - 2ab - cd + ac + 2bd \\
 &= ab - 2ab - 2cd - cd + 2ac + ac + bd + 2bd \\
 &= -ab - 3cd + 3ac + 3bd
 \end{aligned}$$

$$\begin{aligned}
 \text{5) i) } & \text{Take } -ab + bc - ca \text{ from } bc - ca + ab \\
 &= bc - ca + ab - (-ab + bc - ca) \\
 &= bc - ca + ab + ab - bc + ca \\
 &= bc - bc + ca - ca + ab + ab \\
 &= 2ab
 \end{aligned}$$

$$\begin{aligned}
 \text{ii) } & \text{Take } 5x + 6y - 3z \text{ from } 3x + 5y - 4z \\
 &= 3x + 5y - 4z - (5x + 6y - 3z) \\
 &= 3x + 5y - 4z - 5x - 6y + 3z \\
 &= 3x - 5x + 5y - 6y - 4z + 3z \\
 &= -2x - y - z
 \end{aligned}$$

iii) Take $-\frac{3}{2}p + q - r$ from $\frac{1}{2}p - \frac{1}{3}q - \frac{3}{2}r$

$$= \frac{1}{2}p - \frac{1}{3}q - \frac{3}{2}r - (-\frac{3}{2}p + q - r)$$

$$= \frac{p}{2} - \frac{q}{3} - \frac{3r}{2} + \frac{3p}{2} - q + r$$

$$= \frac{p}{2} + \frac{3p}{2} - \frac{q}{3} - q + r - \frac{3r}{2}$$

$$= \frac{p+3p}{2} - \frac{q-3q}{3} + \frac{2r-3r}{2}$$

$$= \frac{4p}{2} - \frac{4q}{3} - \frac{r}{2}$$

$$= 2p - \frac{4}{3}q - \frac{1}{2}r$$

iv) Take $1-a+a^2$ from a^2+a+1

$$= a^2 + a + 1 - (1 - a + a^2)$$

$$= a^2 + a + 1 - 1 + a - a^2$$

$$= a^2 - a^2 + a + a + 1 - 1$$

$$= 2a$$

6) from the sum of $x+y-2z$ and $2x-y+z$ subtract $x+y+z$

$$= (x+y-2z) + (2x-y+z) - (x+y+z)$$

$$= x+y-2z + 2x-y+z - x-y-z$$

$$= x+2x-x+y-y-y-z-z-z$$

$$= 2x-y-2z$$

7) From the sum of $3a - 2b + 4c$ and $5b - 2c$ subtract $a - b - c$

$$\begin{aligned} & (3a - 2b + 4c) + (5b - 2c) - (a - b - c) \\ & 3a - 2b + 4c + 5b - 2c - a + b + c \\ & 3a - a + 3b + b - 2b + 4c + c - 2c \\ & 2a + 2b + 3c \end{aligned}$$

8) Subtract $x - 2y - z$ from the sum of $3x - y + z$ and $x + y - 3z$

$$\begin{aligned} & (3x - y + z) + (x + y - 3z) - (x - 2y - z) \\ & = 3x - y + z + x + y - 3z - x + 2y + z \\ & = 3x + x - x + 2y + y - y + z + z - 3z \\ & = 3x + 2y - z \end{aligned}$$

9) Subtract the sum of $x + y$ and $x - z$ from the sum of $x - 2z$ and $x + y + z$.

$$\begin{aligned} & (x - 2z) + (x + y + z) - \{(x + y) + (x - z)\} \\ & = x - 2z + x + y + z - (x + y + x - z) \\ & = x + x + y + z - 2z - (x + x + y - z) \\ & = 2x + y - z - (2x + y - z) \\ & = 2x + y - z - 2x - y + z \\ & = 2x - 2x + y - y + z - z \\ & = 0 \end{aligned}$$

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