

HOME ASSIGNMENT

MAGNETISM AND MATTER

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1) No of turns in solenoid $(n) = 800$
Area $(A) = 2.5 \times 10^{-4} \text{ m}^2$
Current $(I) = 30 \text{ A}$

$$\Rightarrow M = nIA$$

$$\Rightarrow 800 \times 30 \times 2.5 \times 10^{-4} = M = 0.6 \text{ JT}^{-1}$$

\therefore Hence, the magnetic moment is 0.6 JT^{-1}

2) Magnetic field $(B) = 0.25 \text{ T}$
Torque $(T) = 4.5 \times 10^{-2} \text{ J}$
Angle $(\theta) = 30^\circ$

We know,

$$\therefore M = T / B \sin \theta$$

$$\Rightarrow M = \frac{4.5 \times 10^{-2}}{0.25 \times \sin 36}$$

$$= 0.36 \text{ JT}^{-1}$$

\therefore Hence, the magnetic moment of the magnet is 0.36 JT^{-1} .

3) Moment of the Bar Magnet (M) = 0.32 JT^{-1}
 External magnetic field (B) = 0.15 T
 Angle (θ) = 0° (stable)

(a) Potential energy of the system = $-MB \cos \theta$
 = $-0.32 \times 0.15 \times \cos 0^\circ$

$$= -4.8 \times 10^{-2} \text{ J}$$

(b) Angle (unstable) = 180°

Potential Energy = $-M \cdot B \cdot \cos \theta$

$$= -0.32 \times 0.15 \times \cos 180^\circ$$

$$= 4.8 \times 10^{-2} \text{ J}$$

4) a) magnetic moment (M) = 1.5 JT^{-1}
 Magnetic field (B) = 0.22 T

i) Initial angle $\theta_1 = 0^\circ$
 final angle $\theta_2 = 90^\circ$

The work required (W) = $-MB (\cos \theta_2 - \cos \theta_1)$

$$= -1.5 \times 0.22 (\cos 90^\circ - \cos 0^\circ)$$

$$= -0.33 (0 - 1)$$

$$= 0.33 \text{ J}$$

(iv) Initial angle between the axis $\theta_1 = 0^\circ$
final angle $\theta_2 = 180^\circ$

$$\text{The work required (w)} = -MB (\cos\theta_2 - \cos\theta_1)$$

$$= -1.5 \times 0.22 (\cos 180^\circ - \cos 0^\circ)$$

$$= -0.33 (-1 - 1)$$

$$= 0.66 \text{ J}$$

(b) For case (i) :-

$$\Rightarrow \theta = \theta_2 = 90^\circ$$

$$\therefore \tau = MB \sin \theta$$

$$= MB \sin 90^\circ$$

$$= 1.5 \times 0.22 \sin 90^\circ$$

$$= 0.33 \text{ J}$$

\therefore The torque tends to align the magnitude moment vector along B.

For case (ii)

$$\Rightarrow \theta = \theta_2 = 180^\circ$$

$$\therefore \tau = MB \sin \theta$$

$$= 1.5 \times 0.22 \sin 180^\circ$$

$$= 0 \text{ J}$$

5) No. of turns (n) = 2000
 Area of cross-section (A) = $1.6 \times 10^{-4} \text{ m}^2$
 Current (I) = 4.0 A

(a) Magnetic moment (M) = nIA
 $= 2000 \times 4 \times 1.6 \times 10^{-4}$
 $= 1.28 \text{ Am}^2$

(b) Magnetic field (B) = $7.5 \times 10^{-2} \text{ T}$
 Angle (θ) = 30°
 Torque (τ) = $MB \sin \theta$

$= M \cdot B \cdot \sin \theta$
 $= 1.28 \times 7.5 \times 10^{-2} \sin 30^\circ$
 $= 0.048 \text{ J}$

\therefore The force on solenoid is zero. The torque on the solenoid is 0.048 J.

6) No. of turns (n) = 16
 Radius (r) = 0.1 m
 Cross-section (A) = $\pi \times (0.1)^2 \text{ m}^2$
 Current (I) = 0.75 A
 Magnetic field (B) = $5.0 \times 10^{-2} \text{ T}$
 Frequency (ν) = 2.0 s^{-1}

\therefore Magnetic moment $\Rightarrow M = NIA$
 $= N I \pi r^2$
 $= 16 \times 0.75 \times \pi \times (0.1)^2$
 $= 0.377 \text{ JT}^{-1}$

$$\text{frequency } (\nu) = \frac{1}{2\pi} \sqrt{\frac{MB}{I}}$$

$$\Rightarrow I = \frac{MB}{4\pi^2 \nu^2}$$

$$= \frac{0.377 \times 5 \times 10^{-2}}{4\pi^2 \times (2)^2}$$

$$= 1.2 \times 10^{-4} \text{ kgm}^2 \text{ [moment of inertia]}$$

7) Angle of declination (θ) = 12°

Angle of dip, (δ) = 60°

Earth's magnetic field (B_H) = 0.16 G

B and BH as :-

$$\Rightarrow B_H = B \cos \delta$$

$$\therefore B = \frac{B_H}{\cos \delta}$$

$$\Rightarrow \frac{0.16}{\cos 60^\circ} = 0.32 \text{ G [magnitude]}$$

8) Earth's (B) at place (H) = 0.36 G

$$\Rightarrow B_1 = \frac{\mu_0 2M}{4\pi d^3} = H \rightarrow (1)$$

Permittibility of free space = μ_0

Magnetic moment = M

$$B_2 = \frac{\mu_0 M}{4\pi d^3} = \frac{H}{2} \rightarrow (2)$$

$$\begin{aligned} \therefore \text{Total Magnetic field (B)} &= B_1 + B_2 \\ &= H + H/2 \\ &= 0.36 + 0.18 \\ &= 0.54 \text{ G} \end{aligned}$$

a) Current in wire (I) = 2.5 A

B at a location = $0.33 \times 10^{-4} \text{ T}$

Angle of dip $\theta = 0$

Horizontal $B_H = B \cos \theta = 0.33 \times 10^{-4} \cos 0 = 0.33 \times 10^{-4}$

B current carrying conductor $B_C = \frac{\mu_0}{2\pi} \times \frac{I}{r}$

$$B_C = \frac{4\pi \times 10^{-7}}{2\pi} \times \frac{2.5}{r}$$

$$= \frac{5 \times 10^{-7}}{r}$$

$\Rightarrow B_H = B_C$

$\Rightarrow 0.33 \times 10^{-4} = \frac{5 \times 10^{-7}}{r}$

$\Rightarrow r = \frac{5 \times 10^{-7}}{0.33 \times 10^{-4}}$

$= 0.015 \text{ m}$

$= 1.5 \text{ cm}$

\therefore Hence, neutral points lie on a straight line \perp to the cable at \perp distance = 1.5 cm