

Q23. Write the following set in set-builder notation.

Odd Prime:

- (i)  $B_1 = \{6, 9, 12, 15, \dots\}$   
 $= \{x : x = 3n + 3; n \in \mathbb{N}\}$
- (ii)  $B_2 = \{11, 13, 17, 19\}$   
 $= \{x : x \text{ is a prime number between } 10 \text{ \& } 20\}$
- (iii)  $B_3 = \{\frac{1}{3}, \frac{3}{5}, \frac{5}{7}, \frac{7}{9}, \frac{9}{11}, \dots\}$   
 $= \{x : x = \frac{n}{n+2}, \text{ where } n \text{ is an odd natural no}\}$
- (iv)  $B_4 = \{8, 27, 64, 125, 216\}$   
 $= \{x : x = n^3; n \in \mathbb{N} \text{ and } 2 \leq n \leq 6\}$
- (v)  $B_5 = \{-5, -4, -3, -2, -1\}$   
 $= \{x : x \in \mathbb{Z}, -5 < x < -1\}$
- (vi)  $B_6 = \{-6, -3, 0, 3, 6, \dots\}$   
 $= \{x : x = 3n, n \in \mathbb{Z}\}$

Q3 (i) Is  $\{1, 2, 4, 16, 64\} = \{x : x \text{ is a factor of } 32\}$ ? Give reason.

Ans  $\rightarrow$  No,  $\{1, 2, 4, 16, 64\} \neq \{x : x \text{ is a factor of } 32\}$   
 Because 64 is not a factor of 32

(ii) Is  $\{x : x \text{ is a factor of } 27\} = \{3, 9, 27, 54\}$ ? Give reason.

Ans  $\rightarrow$  No,  $\{x : x \text{ is a factor of } 27\} \neq \{3, 9, 27, 54\}$   
 Because 54 is not a factor of 27

(iii) Write the set of even factors of 124

Ans  $\rightarrow$   $1 \times 124 = 124$   
 $2 \times 62 = 124$   
 $4 \times 31 = 124$

Factors of 124 = 1, 2, 4, 31, 62, 124  
 Set of even factors of 124 =  $\{2, 4, 62, 124\}$



write the set of odd factors of 72.

$$1 \rightarrow 1 \times 72 = 72$$

$$2 \times 36 = 72$$

$$3 \times 24 = 72$$

$$4 \times 18 = 72$$

$$6 \times 12 = 72$$

$$8 \times 9 = 72$$

Factors of 72 = 1, 2, 3, 4, 6, 8, 9, 12, 18, 24, 36, 72

set of odd factors of 72 = {1, 3, 9}

write the set of prime factors of 3234.

$$1 \rightarrow 2 \mid 3234$$

$$3 \mid 1077$$

$$7 \mid 539$$

$$7 \mid 77$$

11

$$3234 = 2 \times 3 \times 7 \times 7 \times 11$$

set of prime factors of 3234 = {2, 3, 7, 11}

$$\text{IS } \{x : x^2 - 7x + 12 = 0\} = \{3, 4\}^?$$

$$1 \rightarrow \Rightarrow x^2 - 4x - 3x + 12 = 0$$

$$\Rightarrow x(x-4) - 3(x-4) = 0$$

$$\Rightarrow (x-4)(x-3) = 0$$

$$\therefore \text{Either } x-4=0 \text{ or } x-3=0$$

$$\Rightarrow x=4 \Rightarrow x=3$$

$\{x : x^2 - 7x + 12 = 0\} = \{3, 4\}$  is true

$$\text{IS } \{x : x^2 - 5x - 6 = 0\} = \{2, 3\}^?$$

$$\Rightarrow x^2 - 6x + x - 6 = 0$$

$$\Rightarrow x(x-6) + 1(x-6) = 0$$

$$\Rightarrow (x-6)(x+1) = 0$$

$$\text{Either } x-6=0 \text{ or } x+1=0$$



i.e.,  $x = 6$  i.e.  $x = -1$

$$\therefore \{x : x^2 - 5x - 6 = 0\} \neq \{2, 3\}$$

In other words  $\{x : x^2 - 5x - 6 = 0\} = \{2, 3\}$  is not true.

Q4) write the following sets in Roster Form:

(i) The set of letters in the word 'MEERUT'.

Ans  $\rightarrow$  Roster Form of the set of letters in the word 'MEERUT' =  $\{m, e, r, u, t\}$

(ii) The set of letters in the word 'UNIVERSAL'.

Ans  $\rightarrow$  Roster Form of the set of letters in the word 'UNIVERSAL' =  $\{u, n, i, v, e, r, s, a, l\}$

(iii)  $A = \{x : x = y + 3, y \in \mathbb{N} \text{ and } y > 3\}$

Ans  $\rightarrow$   ~~$A = \{x : x = y + 3, y \in \mathbb{N} \text{ and } y > 3\}$~~

$$x = y + 3$$

when  $y = 4$

(iv)  ~~$B = \{p : p \in \mathbb{W} \text{ and } p^2 < 20\}$~~

when  $y = 5$

$$x = 4 + 3 = 7$$

when  $y = 6$

$$x = 5 + 3 = 8$$

when  $y = 7$

$$x = 6 + 3 = 9$$

when  $y = 8$

$$x = 7 + 3 = 10$$

$$x = 8 + 3 = 11$$

$\therefore$  Roster Form of the given set  $A = \{7, 8, 9, 10, 11\}$

(iv)  $B = \{p : p \in \mathbb{W} \text{ and } p^2 < 20\}$

Ans  $\rightarrow$  when  $p^2 = 0$

$$p = \sqrt{0} = 0$$

when  $p^2 = 1$

$$p = \sqrt{1} = 1$$



$$\text{when } p^2 = 4$$

$$p = \sqrt{4} = 2$$

$$\text{when } p^2 = 9$$

$$p = \sqrt{9} = 3$$

$$\text{when } p^2 = 16$$

$$p = \sqrt{16} = 4$$

$\therefore$  Roster Form of the given set  $B = \{0, 1, 2, 3, 4\}$

(v)  $C = \{x : x \text{ is composite number and } 5 \leq x \leq 21\}$

Ans  $\rightarrow 5 \leq x \leq 21$  means  $x = 5, 6, 7, 8, 9, 10, \dots, 21$

But we are given that  $x$  is a composite no

$$\therefore x = 6, 8, 9, 10, 12, 14, 15, 16, 18, 20, 21$$

$\therefore$  Roster Form of the given set  $C = \{6, 8, 9, 10, 12, 14, 15, 16, 18, 20, 21\}$

Note: Composite number: The natural numbers (greater than 1), which are not prime, are called composite no.

Q6) List the elements of the following sets:

(i)  $\{x : x^2 - 2x - 3 = 0\}$

$$x^2 - 2x - 3 = 0$$

$$\Rightarrow x^2 - 3x + x - 3 = 0$$

$$\Rightarrow x(x-3) + 1(x-3) = 0$$

$$\Rightarrow (x+1)(x-3) = 0$$

$$\therefore \text{Either } x-3 = 0 \text{ or } x+1 = 0$$

$$x = 3$$

$$x = -1$$

$\therefore$  Elements of the set  $\{x : x^2 - 2x - 3 = 0\}$  are 3 and -1

(ii)  $\{x : x = 2y + 5; y \in \mathbb{N} \text{ and } 2 \leq y \leq 6\}$

$$x = 2y + 5$$

when  $y = 2,$

$$x = 2 \times 2 + 5$$

$$= 4 + 5 = 9$$



$$\text{when } y = 3$$

$$x = 2 \times 3 + 5 \\ = 6 + 5 = 11$$

$$\text{when } y = 4$$

$$x = 2 \times 4 + 5 \\ = 8 + 5 = 13$$

$$\text{when } y = 5$$

$$x = 2 \times 5 + 5 \\ = 10 + 5 = 15$$

$\therefore$  Elements of the given set  $\{x : x = 2y + 5; y \in \mathbb{N} \text{ and } 2 < y < 6\}$  are 9, 11, 13, 15

(iii)  $\{x : x \text{ is a factor of } 24\}$

$$24 = 1 \times 24$$

$$24 = 2 \times 12$$

$$24 = 3 \times 8$$

$$24 = 4 \times 6$$

$\therefore$  Elements of the given set  $\{x : x \text{ is a factor of } 24\}$  are 1, 2, 3, 4, 6, 8, 12, 24

(iv)  $\{x : x \in \mathbb{Z} \text{ and } x^2 \leq 4\}$

$$\text{when } x^2 = 4$$

$$x = \pm \sqrt{4} = \pm 2$$

$$\text{when } x^2 = 1$$

$$x = \pm \sqrt{1} = \pm 1$$

$$\text{when } x^2 = 0$$

$$x = \sqrt{0} = 0$$

$\therefore$  Elements of the given set  $\{x : x \in \mathbb{Z} \text{ and } x^2 \leq 4\}$

$$\Rightarrow 3x \leq 12$$

$$\Rightarrow x \leq \frac{12}{3}$$

$$\Rightarrow x \leq 4$$

$\therefore$  Elements of the given set  $\{x: 3x-2 \leq 10, x \in \mathbb{N}\}$  are 1, 2, 3 and 4

$$ii) \{x: 4-2x \geq -6, x \in \mathbb{Z}\}$$

$$4-2x \geq -6$$

$$-4+4-2x \geq -6-4$$

[Subtracting 4 from both sides]

$$-2x \geq -10$$

$$-2x+2x+10 \geq -10+2x+10$$

[Adding  $2x+10$  to both sides]

$$+10 \geq 2x$$

$$\frac{10}{2} \geq x$$

$$5 \geq x$$

$\therefore$  Elements of the given set  $\{x: 4-2x \geq -6, x \in \mathbb{Z}\}$  are 4, 3, 2, 1, 0, -1, ...