

$$\begin{array}{r}
 2 \overline{) 4096} \\
 2 \overline{) 2048} \\
 2 \overline{) 1024} \\
 2 \overline{) 512} \\
 2 \overline{) 256} \\
 2 \overline{) 128} \\
 2 \overline{) 64} \\
 2 \overline{) 32} \\
 2 \overline{) 16} \\
 2 \overline{) 8} \\
 2 \overline{) 4} \\
 2 \overline{) 2} \\
 1
 \end{array}$$

$$= (2)^3 \times (2)^3 \times (2)^3 \times (2)^3 = (16)^3$$

- (i) cubes of an even number are 216, 8000, 4096.
 (ii) cubes of an odd number are 729, 3375, 125, 343, 9261.

7) Find the least number by which 1323 must be multiplied so that the product is a perfect cube.

Ans → The prime factor of 1323 are = $3 \times 3 \times 3 \times 7 \times 7$
 $= (3 \times 3 \times 3) \times 7 \times 7$

clearly, 1323 must be multiplied by 7.

8) Find the smallest number by which 8768 must be divided so that the quotient is a perfect cube.

Ans → The prime factor of 8768 are $2 \overline{) 8768}$

$$\begin{array}{r}
 2 \overline{) 4384} \\
 2 \overline{) 2192} \\
 2 \overline{) 1096} \\
 2 \overline{) 548} \\
 2 \overline{) 274} \\
 137 \overline{) 137} \\
 1
 \end{array}$$

$= 2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 137$
 $= (2 \times 2 \times 2) \times (2 \times 2 \times 2) \times 137$

clearly, 8768 must be divided by 274
 137.

9) Find the smallest number by which 27783 be multiplied to get a perfect square number.

$$\begin{array}{r} \text{Ans} \rightarrow 3 \overline{) 27783} \\ \underline{3 \quad 9261} \\ 3 \quad 3081 \\ \underline{3 \quad 1029} \\ 7 \quad 343 \\ \underline{7 \quad 49} \\ 7 \quad 7 \\ \underline{\quad 1} \end{array}$$

$$= (3 \times 3 \times 3) \times 3 \times (7 \times 7 \times 7)$$

Clearly, 27783 must be multiplied by $3 \times 3 = 9$

10) with what least number must 8640 be divided so that the quotient is a perfect cube?

Ans \rightarrow The prime factors of 8640 are

$$\begin{array}{r} 2 \overline{) 8640} \\ \underline{2 \quad 4320} \\ 2 \quad 2160 \\ \underline{2 \quad 1080} \\ 2 \quad 540 \\ \underline{2 \quad 270} \\ 3 \quad 135 \\ \underline{3 \quad 45} \\ 3 \quad 15 \\ \underline{3 \quad 5} \\ 5 \quad 5 \\ \underline{\quad 1} \end{array}$$

$$= (2 \times 2 \times 2) \times (2 \times 2 \times 2) \times (3 \times 3 \times 3) \times 5$$

Clearly, 8640 must be divided by 5.

11) which is the smallest number that must be multiplied to 77175 to make it a perfect cube?

Ans → The prime factors of 11175 are

$$3 \overline{) 11175}$$

$$3 \overline{) 25725}$$

$$5 \overline{) 8575}$$

$$5 \overline{) 1715}$$

$$7 \overline{) 343}$$

$$7 \overline{) 49}$$

$$7 \overline{) 7}$$

$$= 3 \times 3 \times 5 \times 5 \times (7 \times 7 \times 7)$$

Clearly, 11175 must be multiplied by $3 \times 5 = 15$