

Ex-604

1. We have  $\triangle ABC \sim \triangle DEF$

$$\text{so, } \frac{AB}{DE} = \frac{BC}{EF} = \frac{CA}{FD}$$

$$\Rightarrow \frac{\text{ar. } (\triangle ABC)}{\text{ar. } \triangle DEF} = \left(\frac{BC}{EF}\right)^2$$

$$\Rightarrow \frac{64}{121} = \frac{BC^2}{(15.4)^2}$$

$$\Rightarrow \frac{64}{121} = \frac{BC^2}{237.16}$$

$$\Rightarrow 121 BC^2 = 237.16 \times 64$$

$$\Rightarrow BC^2 = \frac{237.16 \times 64}{121}$$

$$\Rightarrow BC^2 = 125.44$$

$$\Rightarrow BC = \sqrt{125.44}$$

$$\Rightarrow BC = 11.2 \text{ cm}$$

2. Given

ABCD is a trapezium with  $AB \parallel DC$   
 $AB = 2CD$

In  $\triangle AOB$  and  $\triangle COD$ ,

$$\angle AOB = \angle COD \text{ (V.O.A)}$$

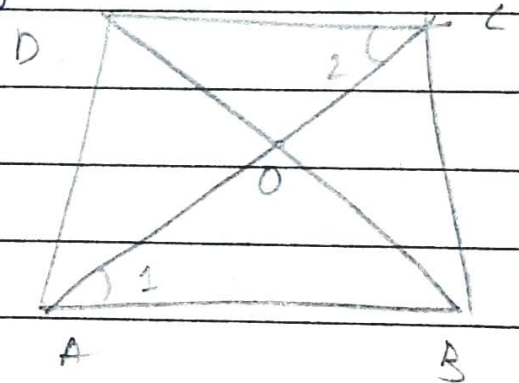
$$\angle 1 = \angle 2 \text{ (alternate angles)}$$

$$\therefore \triangle AOB \sim \triangle COD \text{ (AA)}$$

$$\frac{\text{ar. } \triangle AOB}{\text{ar. } \triangle COD} = \frac{AB^2}{CD^2}$$

$$= \frac{(2CD)^2}{CD^2} = \frac{4CD^2}{CD^2} = \frac{4}{1}$$

$$\therefore \text{ar. } \triangle AOB : \text{ar. } \triangle COD = 4 : 1$$



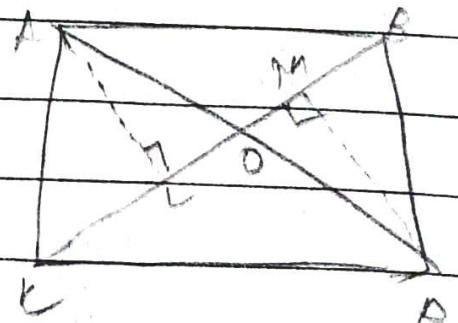
3. Construct<sup>n</sup>

Draw  $AL \perp BC$  and  $DM \perp BC$

In  $\triangle ALO$  &  $\triangle DMO$

$$\angle ALO = \angle DMO \text{ (each } 90^\circ)$$

$$\angle AOL = \angle DOM \text{ (V.O.A)}$$



$$\therefore \triangle ALO \sim \triangle DMO \text{ (AA)}$$

$$\Rightarrow \frac{AL}{DM} = \frac{AO}{DO} \text{ ————— ①}$$

$$\frac{\text{Now, ar. } (\triangle ABC)}{\text{ar. } (\triangle DBC)} = \frac{\frac{1}{2} \times BC \times AL}{\frac{1}{2} \times BC \times DM}$$

$$= \frac{AL}{DM} = \frac{AD}{PD} \quad (\text{from } \textcircled{1})$$

$\therefore$  Proved

4. Given

$$\triangle ABC \sim \triangle DEF$$

$$\text{ar. } \triangle ABC = \text{ar. } \triangle DEF$$

To prove

$$\triangle ABC \cong \triangle DEF$$

Proof

$$\frac{\text{ar. } \triangle ABC}{\text{ar. } \triangle DEF} = \frac{AB^2}{DE^2} = \frac{AC^2}{DF^2} = \frac{BC^2}{EF^2}$$

$$1 = \frac{AB^2}{DE^2} = \frac{AC^2}{DF^2} = \frac{BC^2}{EF^2} \quad (\because \text{ar. } \triangle ABC = \text{ar. } \triangle DEF)$$

$$\Rightarrow AB^2 = DE^2, AC^2 = DF^2, BC^2 = EF^2$$

$$AB = DE, AC = DF, BC = EF$$

$$\therefore \triangle ABC \cong \triangle DEF \text{ (SSS)}$$