

1. Find the sum of

$$\begin{aligned} \text{i) } & 3a + 4b + 7c \\ & + 5a + 3b - 6c \\ & \underline{4a - 2b - 4c} \\ & 2a + 5b - 3c \end{aligned}$$

$$\begin{aligned} \text{ii) } & 2x^2 + xy - y^2 \\ & + x^2 + 2xy + 3y^2 \\ & + 3x^2 + 10xy + 4y^2 \\ & \underline{\hspace{1.5cm}} \\ & 4x^2 + 13xy + 6y^2 \end{aligned}$$

$$\begin{aligned} \text{iii) } & x^2 - x + 1 \\ & + -5x^2 + 2x - 2 \\ & \underline{3x^2 - 3x + 1} \\ & -x^2 - 2x \end{aligned}$$

$$\begin{aligned} \text{iv) } & a^2 - ab + bc + 2ab + bc \\ & + bc - 2a^2 + (-3bc) + 3a^2 \\ & + ab \\ & = a^2 - 2a^2 + 3a^2 - ab + \\ & 2ab + ab + bc - 3bc \\ & = 2a^2 + 2ab - bc \end{aligned}$$

$$\begin{aligned} \text{v) } & (4x^2 + 7 - 3x) + (4x - x^2 + 8) + (10 + 5x - 2x^2) \\ & = 4x^2 - x^2 - 2x^2 - 3x + 4x + 5x + 7 + 8 - 10 \\ & = x^2 + 6x + 5 \end{aligned}$$

$$\begin{aligned} \text{vi) } & 3x + 4xy - y^2, \quad xy - 4x + 2y^2 \text{ and} \\ & 3y^2 - xy + 6x \\ & = 3x - 4x + 6x + 4xy + xy - xy - y^2 + 2y^2 \\ & + 3y^2 \\ & = 5x + 4xy + 4y^2 \end{aligned}$$

2. Add the following expressions:

$$\begin{aligned} \text{ii) } & -17x^2 - 2xy + 23y^2, \quad -9y^2 + 15x^2 + 7xy \\ & \text{and } 13x^2 + 3y^2 - 4xy \\ & = (-17x^2 - 2xy + 23y^2) + (-9y^2 + 15x^2 + 7xy) \\ & + (13x^2 + 3y^2 - 4xy) \\ & = -17x^2 + 15x^2 + 13x^2 - 2xy + 7xy - 4xy \\ & + 23y^2 - 9y^2 + 3y^2 \end{aligned}$$

$$= 11xy^2 + xy + 17y^2$$

$$\begin{aligned} \text{ii)} & (-x^2 - 3xy + 3y^2 + 8) + (3x^2 - 5y^2 + 3 + 4xy) \\ & + (-6xy + 2x^2 - 2 + y^2) \\ = & -x^2 + 3x^2 + 2x^2 - 3xy + 4xy - 6xy + \\ & + 3y^2 - 5y^2 + y^2 + 8 - 3 - 2 \\ = & 4x^2 - 5xy - y^2 + 3 \end{aligned}$$

$$\begin{aligned} \text{iii)} & (a^3 - 2b^3 + a) + (b^3 - 2a^3 + b) + (-2b + 2b^3 \\ & - 5a + 4a^3) \\ = & a^3 - 2a^3 + 4a^3 - 2b^3 + b^3 + 2b^3 + a - 5a + b \\ & - 2b \\ = & 3a^3 + b^3 + 4a - b \end{aligned}$$

3. Evaluate

$$\begin{aligned} \text{i)} \quad 3a - (a + 2b) &= \text{ii)} \quad (5x - 8y) - (x + y) \\ = 3a - a - 2b &= 5x - 3y - x - y \\ = 2a - 2b &= 5x - x - 3y - y \\ &= 4x - 4y \end{aligned}$$

$$\begin{aligned} \text{iii)} \quad (8a + 15b) - (3b - 7a) & \quad \text{iv)} \quad 7 - (4a - 5) \\ = 8a + 15b - 3b + 7a &= 7 - 4a + 5 \\ = 8a + 7a + 15b - 3b &= 7 + 5 - 4a \\ = 15a + 12b &= 12 - 4a \end{aligned}$$

$$\begin{aligned} \text{v)} \quad (8x + 7y) - (4y - 3x) & \quad \text{vi)} \quad (6y - 13) - (4 - 3y) \\ = 8x + 7y - 4y + 3x &= 6y - 13 - 4 + 3y \\ = 8x + 3x + 7y - 4y &= 6y + 3y - 13 - 4 \\ = 11x + 3y &= 9y - 17 \end{aligned}$$

A. Subtract

$$\begin{aligned} \text{i) } a - 4b - 2c - (5a - 3b + 2c) \\ = a - 5a - 4b + 3b - 2c - 2c \\ = -4a - b - 4c \end{aligned}$$

$$\begin{aligned} \text{ii) } 12x + 7y - 21z - (4x - 6y + 3z) \\ = 12x + 7y - 21z - 4x + 6y - 3z \\ = 12x - 4x + 7y + 6y - 21z - 3z \\ = 8x + 13y - 24z \end{aligned}$$

~~$$\begin{aligned} \text{iii) } (5 - a - 4b + 4c) - (5a - 7b + 2c) \\ = 5 - a - 4b + 4c - 5a + 7b - 2c \\ = 5 - 5a - 4b + 7b + 4c - 2c \\ = 5 - 6a + 3b + 2c \end{aligned}$$~~

$$\begin{aligned} \text{iv) } (5a - 7b + 2c) - (5 - a - 4b + 4c) \\ = 5a - 7b + 2c - 5 + a + 4b - 4c \\ = 5a + a - 7b + 4b + 2c - 4c - 5 \\ = 6a - 3b - 2c - 5 \end{aligned}$$

$$\begin{aligned} \text{v) } (x - y - z) - (-8x - 12y + 17z) \\ = x - y - z + 8x + 12y - 17z \\ = x + 8x - y + 12y - z - 17z \\ = 9x + 11y - 18z \end{aligned}$$

$$\begin{aligned} \text{vi) } (ab - 2cd + 2ac + bd) - (2ab + cd - ac) - 2c \\ = ab - 2cd + 2ac + bd - 2ab - cd + ac + ab \\ = ab - 2ab - 2cd - cd + 2ac + ac + bd \\ = -ab - 3cd + 3ac + bd \end{aligned}$$

$$\begin{aligned}
 & 5. (bc - ca + ab) - (-ab + bc - ca) \\
 & = bc - ca + ab + ab - bc + ca \\
 & = bc - bc - ca + ca + ab + ab \\
 & = 2ab
 \end{aligned}$$

$$\begin{aligned}
 & \text{ii) } (3x + 5y - 4z) - (5x + 6y - 3z) \\
 & = 3x + 5y - 4z - 5x - 6y + 3z \\
 & = 3x - 5x + 5y - 6y - 4z + 3z \\
 & = -2x - y - z
 \end{aligned}$$

$$\begin{aligned}
 & \text{iii) } \left(\frac{1}{2}p - \frac{1}{3}q - \frac{3}{2}r\right) - \left(-\frac{3}{2}p + q - r\right) \\
 & = \frac{1}{2}p - \frac{1}{3}q - \frac{3}{2}r + \frac{3}{2}p - q + r \\
 & = \frac{1}{2}p + \frac{3}{2}p - \frac{1}{3}q - q - \frac{3}{2}r + r \\
 & = \frac{p + 3p}{2} - \frac{q - 3q}{3} - \frac{3r + 2r}{2} \\
 & = \frac{4p}{2} - \frac{4q}{3} - \frac{5r}{2} \\
 & = 2p - \frac{4}{3}q - \frac{5}{2}r
 \end{aligned}$$

$$\begin{aligned}
 & 6. (a^2 + a + 1) - (1 - a + a^2) \\
 & = a^2 + a + 1 - 1 + a - a^2 \\
 & = a^2 - a^2 + a + a + 1 - 1 \\
 & = 2a
 \end{aligned}$$

$$\begin{aligned}
 & \text{Sum of } (x + y - 2z) + (2x - y + z) \\
 & = x + 2x + y - y - 2z + z \\
 & = 3x - z
 \end{aligned}$$

$$\begin{aligned}
 & \text{Difference of } (x + y + z) - (3x - y - z) \\
 & = x + y + z - 3x + y + z
 \end{aligned}$$

$$= x - 3x + z + z + y$$
$$= 2z + 2z + y$$

$$\text{Difference of } (3x - z) - (x + y + z)$$
$$= 3x - z - x - y - z$$
$$= 3x - x - z - z - y$$
$$= 2x - 2z - y$$

$$\text{7.ii) Sum of } (3a - 2b + 4c) + (2b - 2c)$$
$$= 3a - 2b + 3b + 4c - 2c$$
$$= 3a + b + 2c$$

$$\text{Difference of } (3a + b + 2c) - (a - b - c)$$
$$= 3a + b + 2c - a + b + c$$
$$= 3a - a + b + b + 2c + c$$
$$= 2a + 2b + 3c$$

$$\text{8. Sum of } (3x - y + z) + (x + y - 3z)$$
$$= 3x + x - y + y + z - 3z$$
$$= 4x - 2z$$

$$\text{Difference of } (4x - 2z) - (x - 2y - z)$$
$$= 4x - 2z - x + 2y + z$$
$$= 4x - x - 2z + z + 2y$$
$$= 3x - z + 2y$$
$$= 3x + 2y - z$$

$$\text{9. Sum of } (x + y) + (x - z)$$
$$= x + x + y - z$$
$$= 2x + y - z$$

$$\text{Sum of } (x - 2z) + (x + y + z)$$
$$= x + x + y - 2z + z$$
$$= 2x + y - z$$

$$\text{Difference of } (2x + y - z) - (2x + y - z)$$

$$= 2x + y - z - 2x - y + z$$

$$= 2x - 2x + y - y - z + z$$

$$= 0$$

